

# **Effect of systematics in T2HK, T2HKK, DUNE**

**Osamu Yasuda  
Tokyo Metropolitan University**

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**Based on**

**PRD 96 ('17) 013001, Monojit Ghosh & OY**

**PTEP 2018 ('18) 063C01, § 7.1, Monojit Ghosh  
& OY et al. (Hyper-Kamiokande Proto-  
Collaboration)**

# Outline of this talk

1. Introduction
2. Sensitivity of T2HK, DUNE, T2HKK for std case
3. Sensitivity of T2HK, DUNE, T2HKK for NSI
4. Conclusions



# 1. Introduction

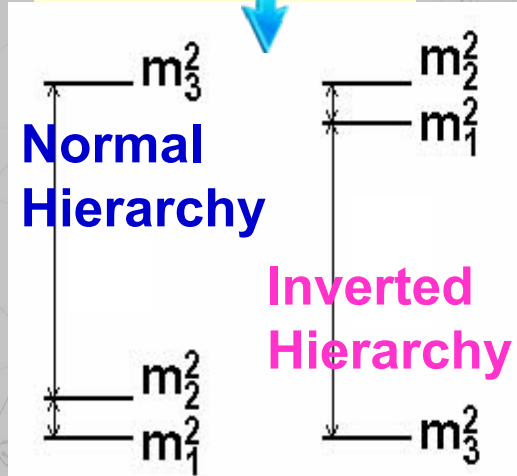
## Framework of 3 flavor $\nu$ oscillation

### Mixing matrix

Functions of mixing angles  $\theta_{12}, \theta_{23}, \theta_{13}$ , and CP phase  $\delta$

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Both hierarchy patterns are allowed



All 3 mixing angles have been measured (2012):

$\nu_{\text{solar}}$  + KamLAND (reactor)

$$\theta_{12} \cong \frac{\pi}{6}, \Delta m_{21}^2 \cong 8 \times 10^{-5} \text{ eV}^2$$

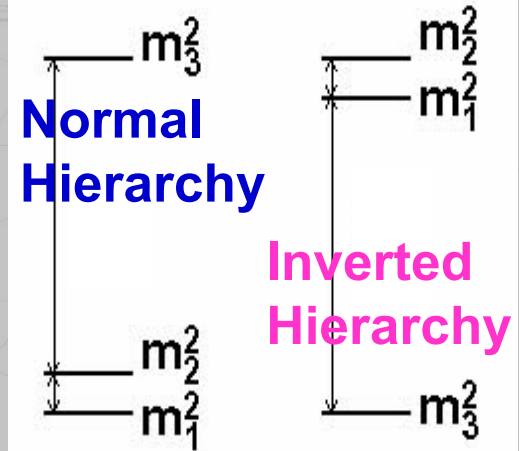
$\nu_{\text{atm}}$  + K2K, MINOS (accelerators)

$$\theta_{23} \cong \frac{\pi}{4}, |\Delta m_{32}^2| \cong 2.5 \times 10^{-3} \text{ eV}^2$$

DCHOOZ + Daya Bay + Reno (reactors), T2K + MINOS + Nova etc

$$\theta_{13} \cong \pi / 20$$

Next task is to measure  $\text{sign}(\Delta m^2_{31})$  (Mass Hierarchy),  $\pi/4 - \theta_{23}$  (Octant) and  $\delta$  (CP)



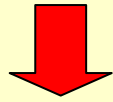
## Proposed experiments

- T2HK (JP, JPARC  $\rightarrow$  HK)  $L=295\text{km}$ ,  $E \sim 0.6\text{GeV}$
- T2HKK (JP, JPARC  $\rightarrow$  Korea)  $L=1100\text{km}$ ,  $E \sim 1\text{GeV}$
- DUNE (US, FNAL  $\rightarrow$  Homestake, SD),  $L=1300\text{km}$ ,  $E \sim 2\text{GeV}$

$$\overline{\nu}_\mu \rightarrow \overline{\nu}_\mu + \overline{\nu}_\mu \rightarrow \overline{\nu}_e$$

These experiments are expected to measure  $\text{sign}(\Delta m^2_{31})$ ,  $\pi/4 - \theta_{23}$  and  $\delta$

**In these long baseline experiments with intensive beams, systematic errors become important to sensitivity.**



**In this talk, we examine dependence of the sensitivity on the systematic errors.**



## 2. Sensitivity of T2HK, DUNE, T2HKK for std case

### 2.1 Preliminary

The parameters assumed here:

#### T2HK

(L=295km, 187 kton fiducial volume) x2

$\nu$ :anti- $\nu$  = 1:3

Total exposure:  $27 \times 10^{21}$  POT

#### DUNE

L=1300km, 1.2MW, 40 kt LiAr detector,

$\nu$ :anti- $\nu$  = 1:1

Total exposure:  $10 \times 10^{21}$  POT

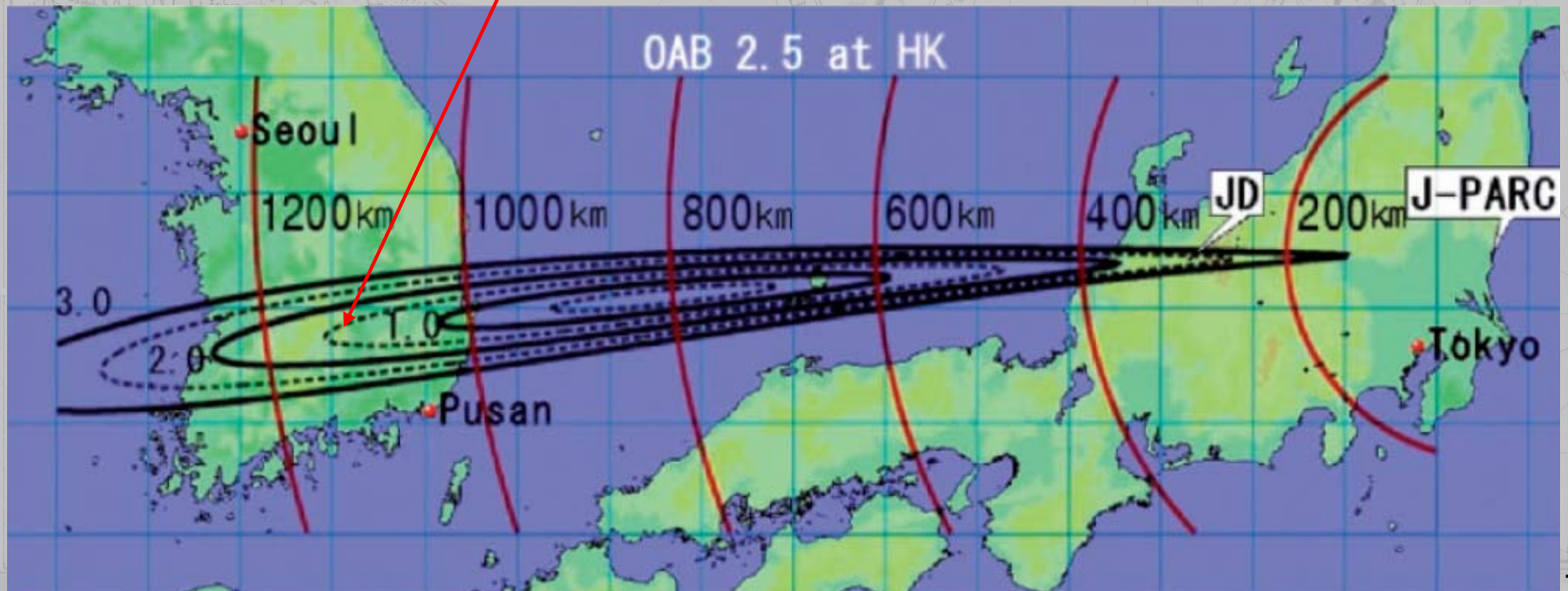
# T2HKK

(L=295km, 187 kton fiducial volume)  
+ (L=1100km, 187 kton fiducial volume)

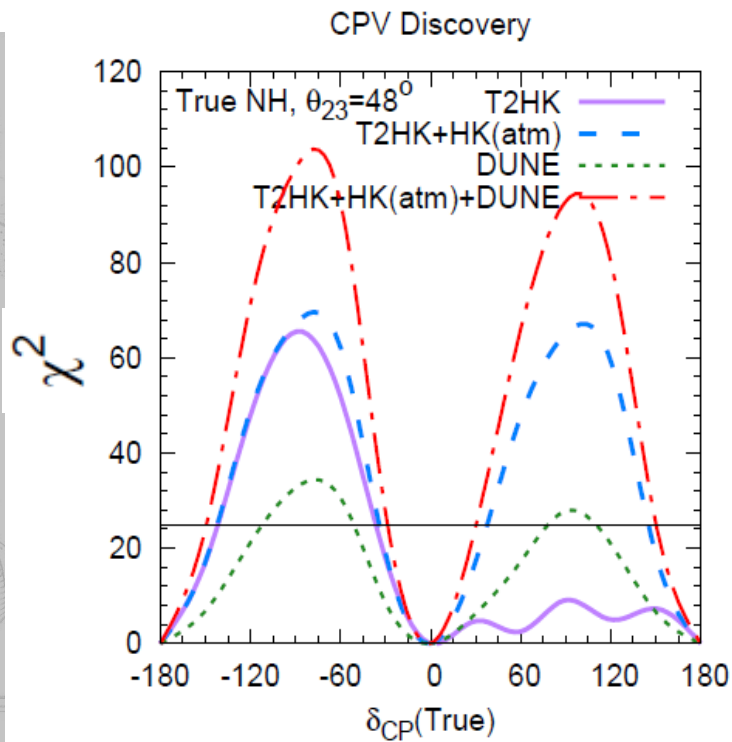
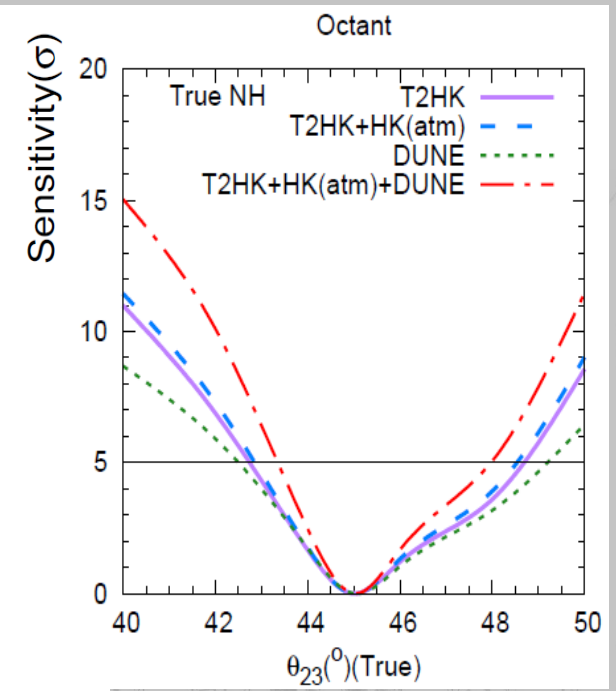
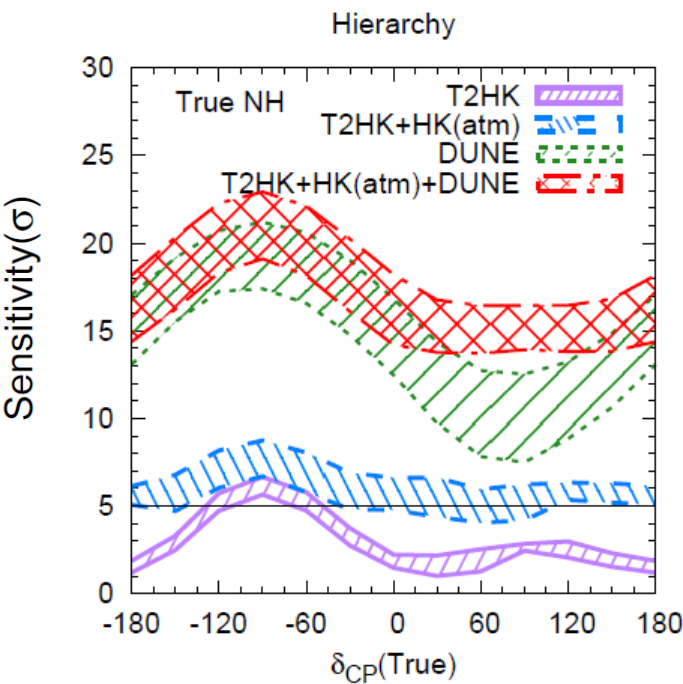
$\nu$ :anti- $\nu$  = 1:3

Total exposure:  $27 \times 10^{21}$  POT

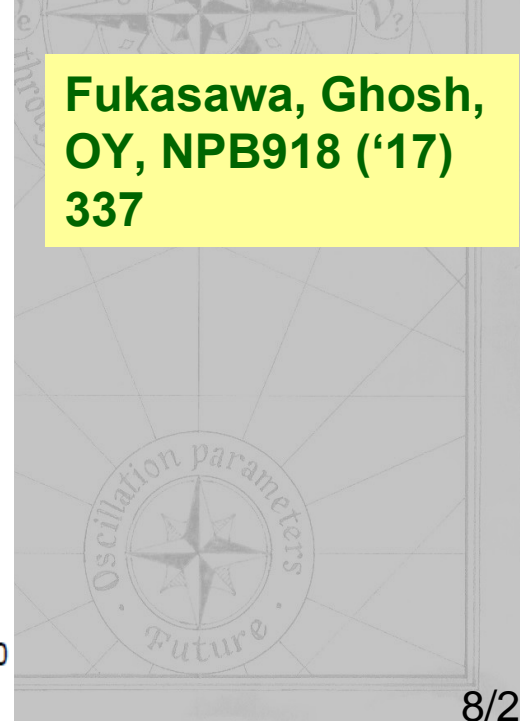
Off axis Angle =  $1.5^\circ$  is the best (w/ max #(events))



# Sensitivity to Mass Hierarchy, Octant, CP has been studied in the past



**Fukasawa, Ghosh, OY, NPB918 ('17) 337**



# Outline of our Analysis

Start with  $\chi^2$  with statistical errors:

$$\chi^2_{\text{stat}} = \sum_i 2 \left[ N_i^{\text{test}} - N_i^{\text{true}} - N_i^{\text{true}} \log \left( \frac{N_i^{\text{test}}}{N_i^{\text{true}}} \right) \right]$$

## Sensitivity to Mass Hierarchy

$$\begin{aligned} N_i^{\text{true}} &= N_i^{\text{true}} (\Delta m_{\mu\mu}^2) \\ N_i^{\text{test}} &= N_i^{\text{test}} (-\Delta m_{\mu\mu}^2) \end{aligned}$$

## Sensitivity to Octant

$$\begin{aligned} N_i^{\text{true}} &= N_i^{\text{true}} (\theta_{23}) \\ N_i^{\text{test}} &= N_i^{\text{test}} (\pi/4 - \theta_{23}) \end{aligned}$$

## Sensitivity to CP

$$\begin{aligned} N_i^{\text{true}} &= N_i^{\text{true}} (\delta) \\ N_i^{\text{test}} &= N_i^{\text{test}} (\delta=0) \end{aligned}$$

+

$$\begin{aligned} N_i^{\text{true}} &= N_i^{\text{true}} (\delta) \\ N_i^{\text{test}} &= N_i^{\text{test}} (\delta=\pi) \end{aligned}$$

**Then introduce the systematic errors:**

**normalization error**

$$N_i^{\text{test}} \rightarrow N_i^{\text{test}} \left( 1 + \sum_k c_i^k \xi_k \right)$$

**tilt error**

$$N_i^{\text{test}} \rightarrow N_i^{\text{test}} \left( 1 + \sum_k c_i^k \xi_k \frac{E_i - E_{\text{av}}}{E_{\text{max}} - E_{\text{min}}} \right)$$

**Final  $\chi^2$  we work with:**

$$\chi^2 = \min_{\{\text{osc. param.}, \xi_k\}} \left[ \chi_{\text{stat}}^2 + \sum_k \xi_k^2 \right]$$

# Reference values of the systematic errors

HK arXiv:1412.4673

DUNE arXiv:1512.06148

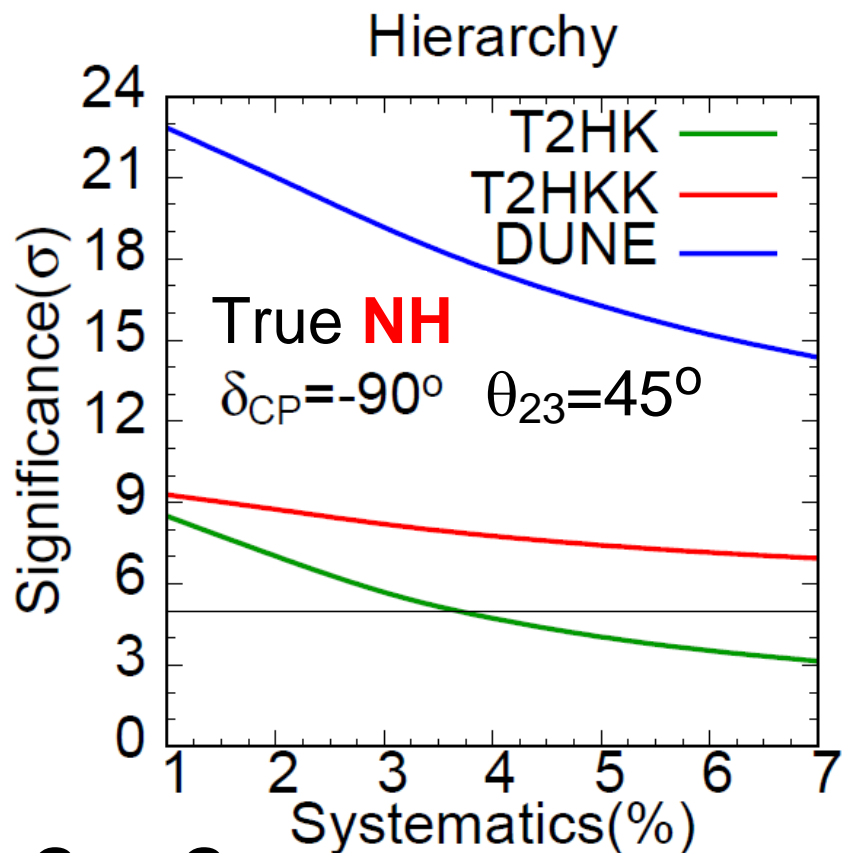
	channel	HK	DUNE
$\nu$	disappearance	3.3%	5%
	appearance	3.3%	2%
$\bar{\nu}$	disappearance	4.5%	5%
	appearance	6.2%	2%

$c_1$  = signal normalization error  
 $c_2$  = background normalization error  
 $c_3$  = signal tilt error  
 $c_4$  = background tilt error

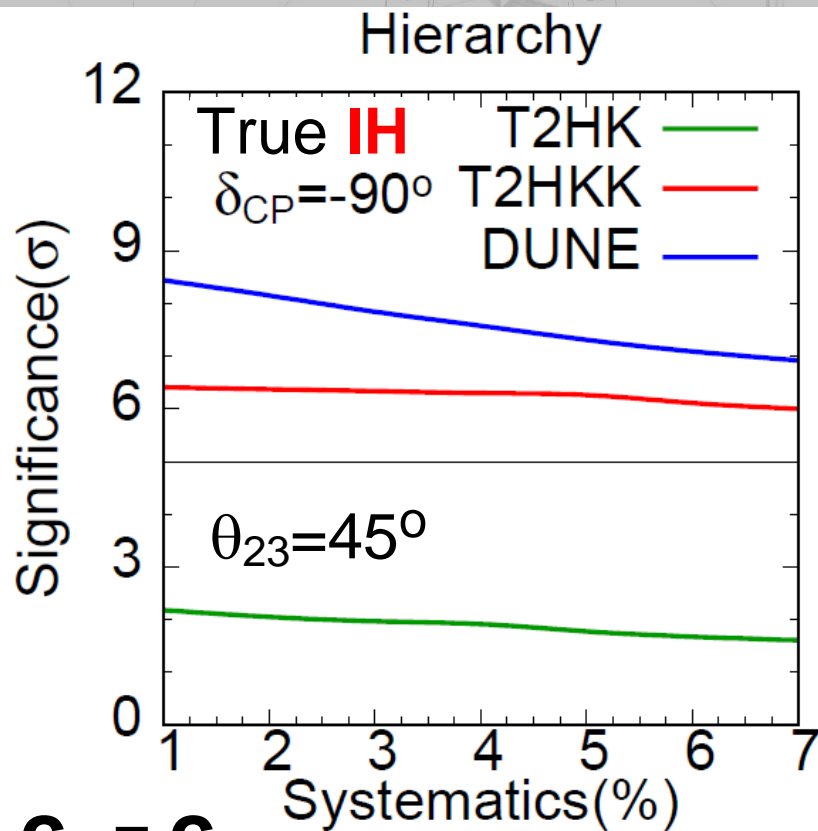
For simplicity we assume  $C_1 = C_2$  for all channels and vary only  $C_1$  &  $C_2$ ;  $C_3 = C_4 = 10\%$  (2.5%) for T2HK(K) (DUNE)

## 2.2 Sensitivity to Mass Hierarchy

PRD 96 ('17) 013001,  
Monojit Ghosh & OY



$$C_1 = C_2$$



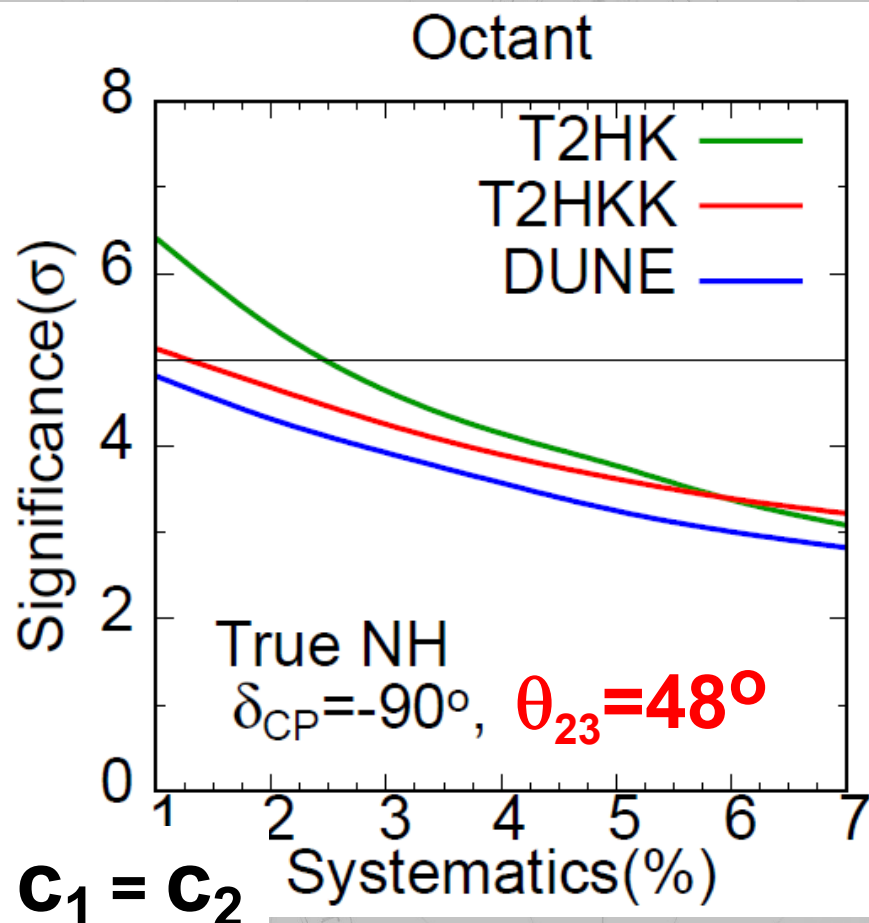
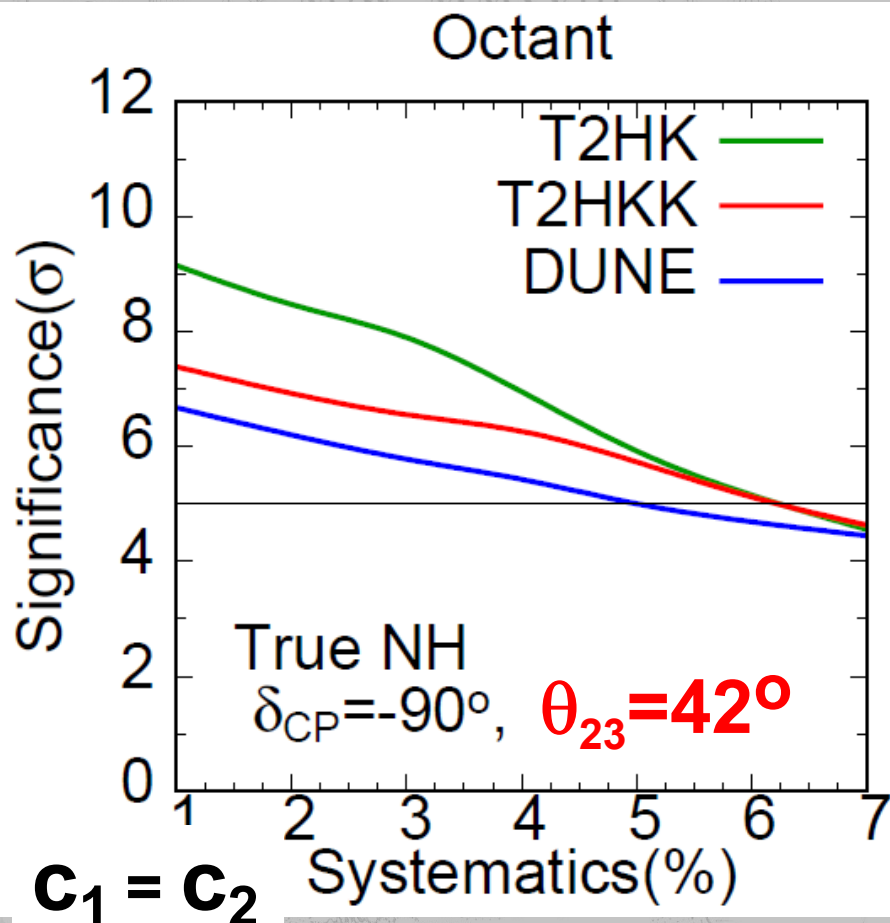
$$C_1 = C_2$$

• Dependence of T2HK & DUNE stronger than that of T2HKK

• If true MH is NH &  $\delta = -90^\circ$  &  $c_1 < 3.5\%$  then T2HK is sufficient to determine MH at  $5\sigma$

## 2.3 Sensitivity to Octant

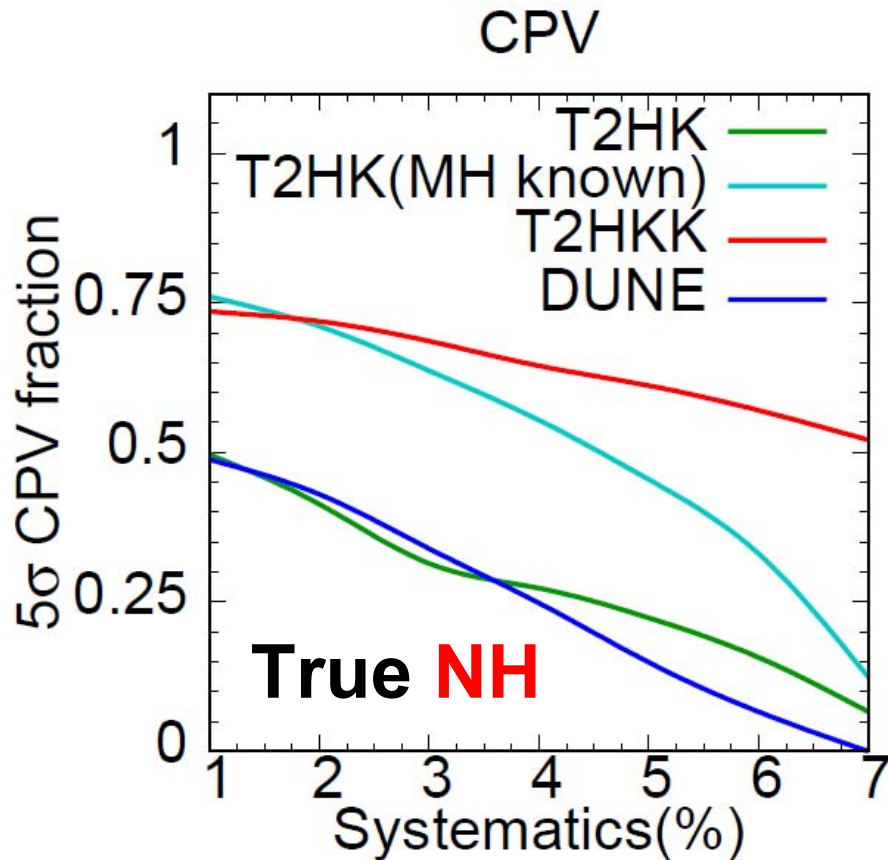
PRD 96 ('17) 013001,  
Monojit Ghosh & OY



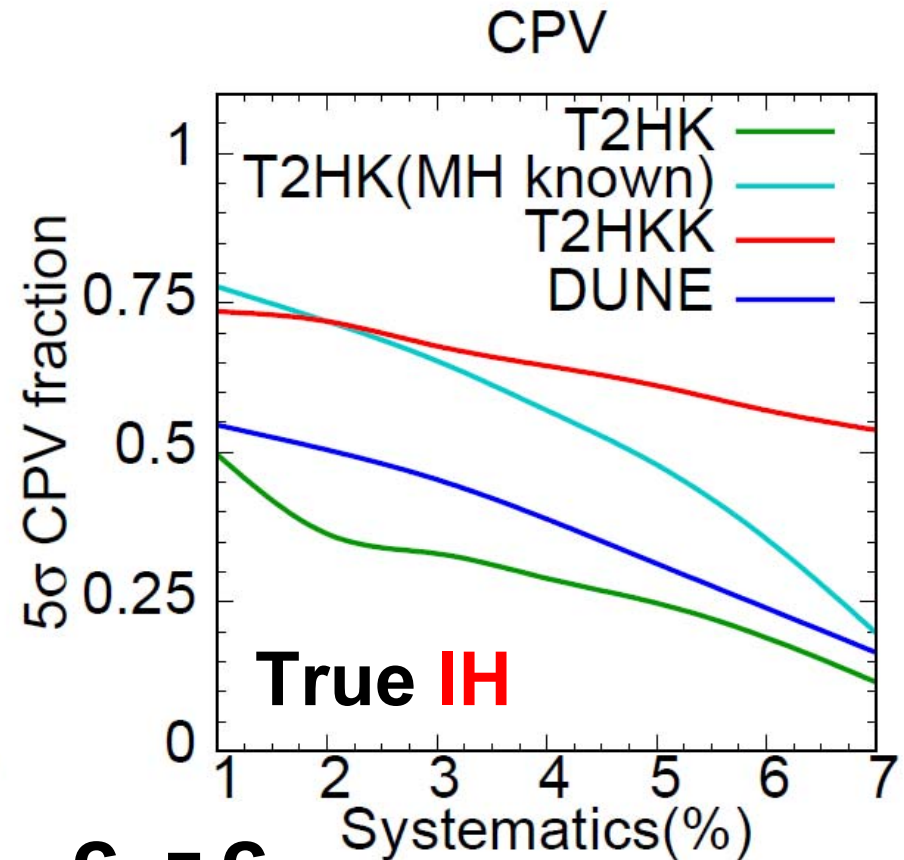
- Dependence of T2HK stronger than that of others
- Significance of Lower Octant ( $\theta_{23} < 45^\circ$ ) larger than that of Higher Octant ( $\theta_{23} > 45^\circ$ )

## 2.4 Sensitivity to CP

PRD 96 ('17) 013001,  
Monojit Ghosh & OY



$$C_1 = C_2$$



$$C_1 = C_2$$

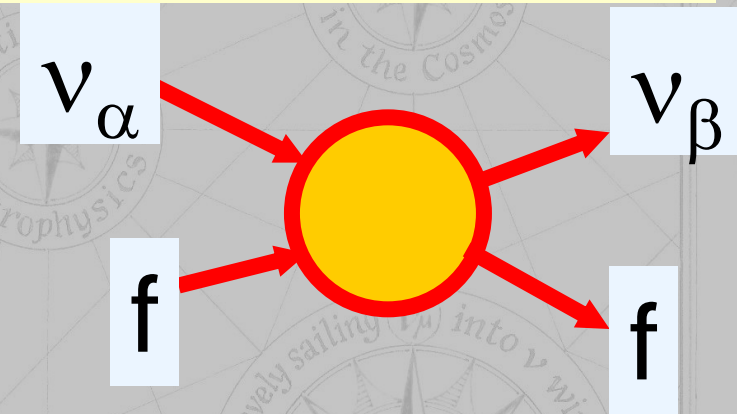
- Dependence of T2HK stronger than that of T2HKK
- If MH is known then T2HK w/  $c_1 < 2\%$  is better than T2HKK

# 3. Sensitivity of T2HK, DUNE, T2HKK for NSI in $\nu$ propagation

## 3.1 Preliminary

Phenomenological **New Physics** considered in this talk: 4-fermi **Non Standard Interactions**:

$$\mathcal{L}_{eff} = G_{NP}^{\alpha\beta} \bar{\nu}_\alpha \gamma^\mu \nu_\beta \bar{f} \gamma_\mu f'$$



neutral current  
non-standard  
interaction

## Modification of matter effect

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left[ U \text{diag}(E_1, E_2, E_3) U^{-1} + A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$$A \equiv \sqrt{2} G_F N_e \quad N_e \equiv \text{electron density}$$

**NP**

- Constraints on  $\epsilon_{\alpha\beta}$

- Various non-oscillation  $\nu$  experiments

Davidson et al., JHEP 0303:011,2003; Berezhiani, Rossi, PLB535 ('02) 207; Barranco et al., PRD73 ('06) 113001; Barranco et al., arXiv:0711.0698

Biggio et al., JHEP 0908, 090 (2009) w/o 1-loop arguments

$\mu$ -components are all small

$$\left( \begin{array}{l} |\epsilon_{ee}| \lesssim 4 \times 10^0 \\ |\epsilon_{e\mu}| \lesssim 3 \times 10^{-1} \\ |\epsilon_{\mu\mu}| \lesssim 7 \times 10^{-2} \\ |\epsilon_{e\tau}| \lesssim 3 \times 10^0 \\ |\epsilon_{\mu\tau}| \lesssim 3 \times 10^{-1} \\ |\epsilon_{\tau\tau}| \lesssim 2 \times 10^1 \end{array} \right)$$

- High energy behavior of  $\nu_{\text{atm}}$  data

$$|\epsilon_{\tau\tau} - |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee})| \ll 1$$

Friedland-Lunardini,  
PRD72:053009,'05

- **Ansatz of our analysis on  $\epsilon_{\alpha\beta}$**

**To a good approximation, we are left with 3 independent variables  $\epsilon_{ee}$ ,  $|\epsilon_{e\tau}|$ ,  $\arg(\epsilon_{e\tau})=\phi_{31}$ :**

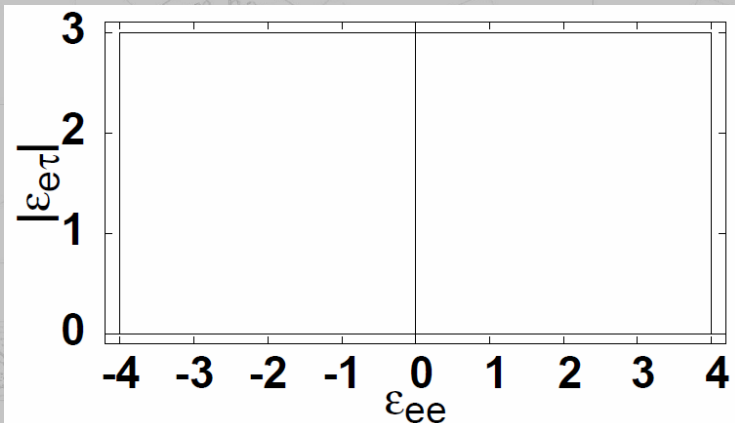
$$A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\mu} & \epsilon_{e\tau} \\ \epsilon_{\mu e} & \epsilon_{\mu\mu} & \epsilon_{\mu\tau} \\ \epsilon_{\tau e} & \epsilon_{\tau\mu} & \epsilon_{\tau\tau} \end{pmatrix} \simeq A \begin{pmatrix} 1 + \epsilon_{ee} & 0 & \epsilon_{e\tau} \\ 0 & 0 & 0 \\ \epsilon_{e\tau}^* & 0 & |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee}) \end{pmatrix}$$

**We perform analysis with 3 independent variables  $\epsilon_{ee}$ ,  $|\epsilon_{e\tau}|$ ,  $\phi_{31}=\arg(\epsilon_{e\tau})$  and give the allowed region in the  $(\epsilon_{ee}, |\epsilon_{e\tau}|)$  plane by marginalizing w.r.t.  $\phi_{31}=\arg(\epsilon_{e\tau})$**

$$-4 \lesssim \epsilon_{ee} \lesssim 4,$$

$$|\epsilon_{e\tau}| \lesssim 3,$$

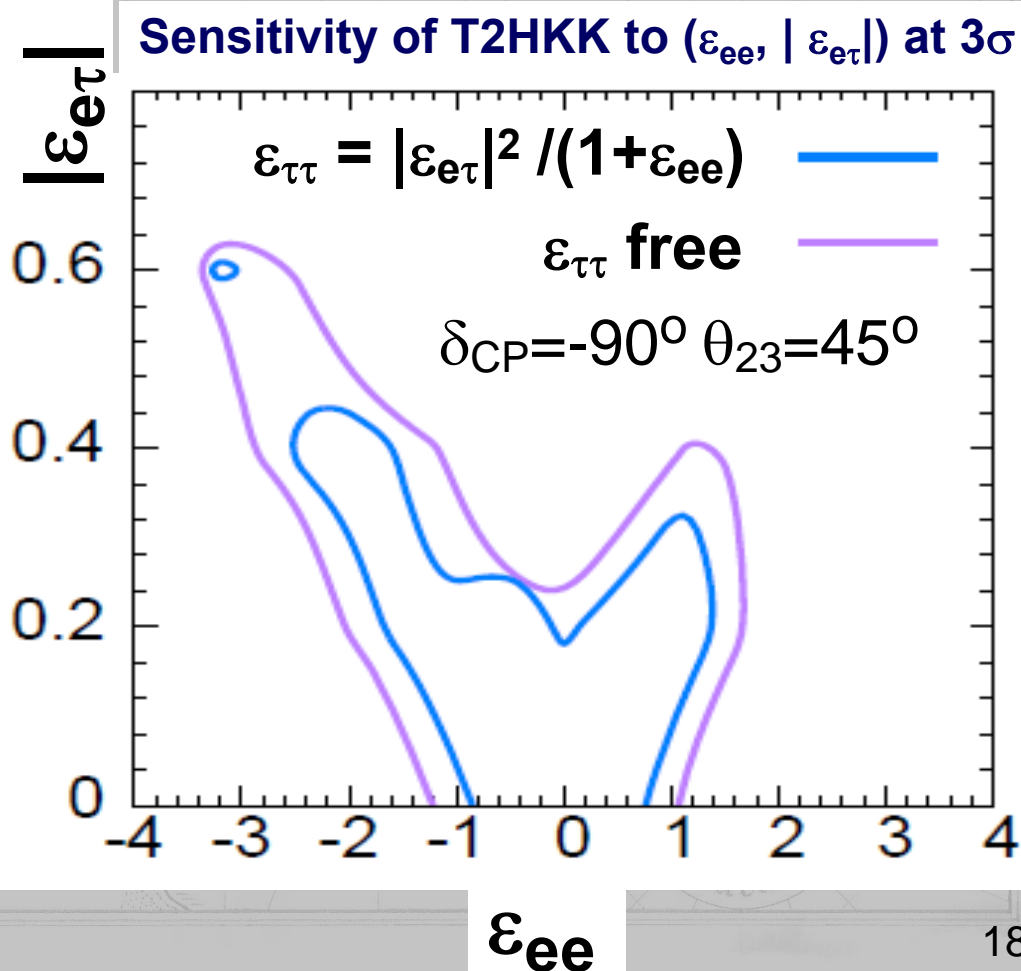
$$|\epsilon_{\tau\tau}| = \frac{|\epsilon_{e\tau}|^2}{|1 + \epsilon_{ee}|}$$



# Comment on the approximation $\varepsilon_{\tau\tau} = |\varepsilon_{e\tau}|^2 / (1 + \varepsilon_{ee})$

The sensitivity to  $(\varepsilon_{ee}, |\varepsilon_{e\tau}|)$  w/ or w/o this approximation is slightly different.

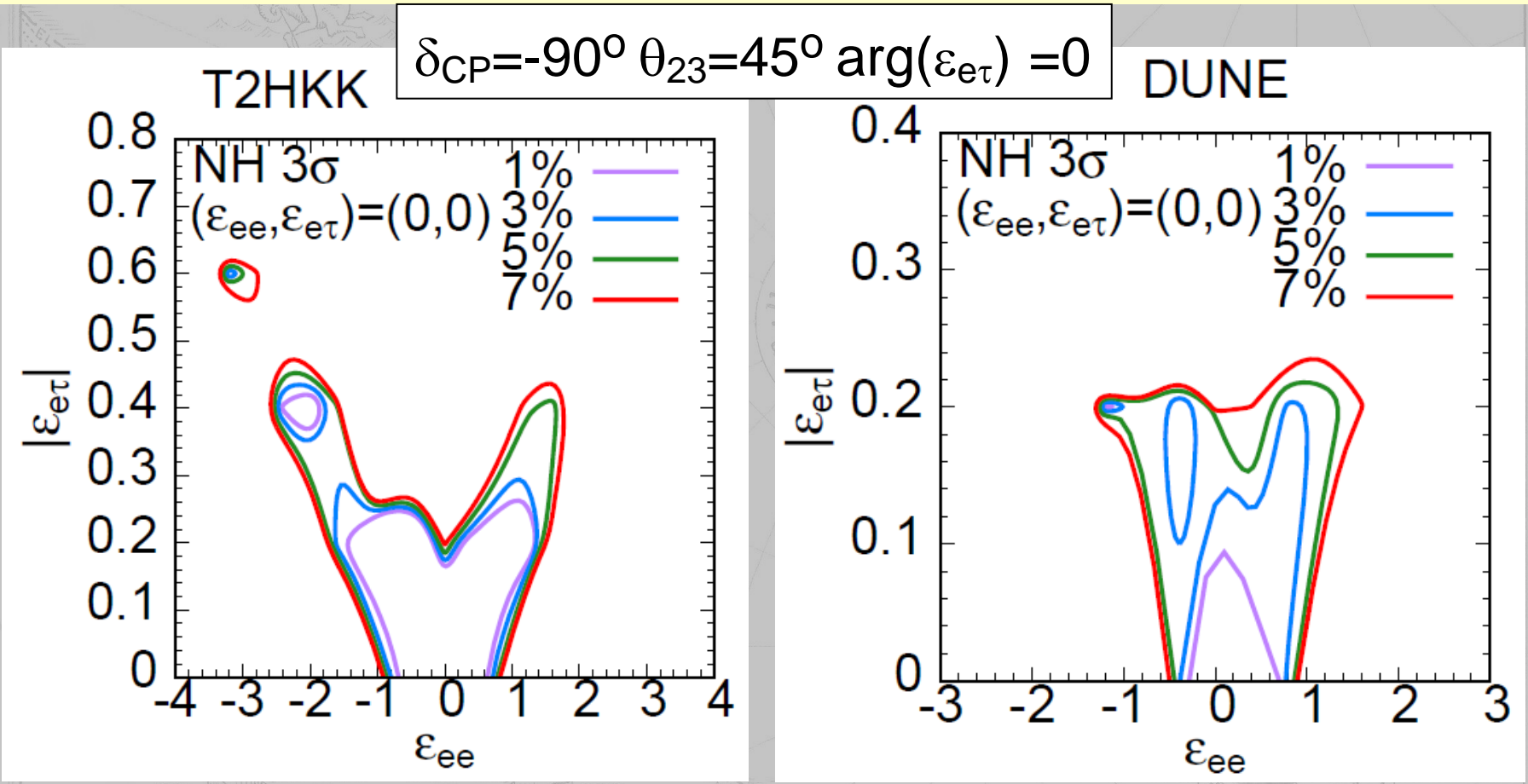
PTEP 2018 ('18) 063C01,  
§ 7.1, Monojit Ghosh &  
OY et al. (Hyper-  
Kamiokande Proto-  
Collaboration)



### 3.1 Sensitivity to $(\epsilon_{ee}, |\epsilon_{e\tau}|)$

PRD 96 ('17) 013001,  
Monojit Ghosh & OY

T2HK (not plotted) has too short baseline length  
( $L=295\text{km}$ )-> Sensitivity to NSI is much worse than others

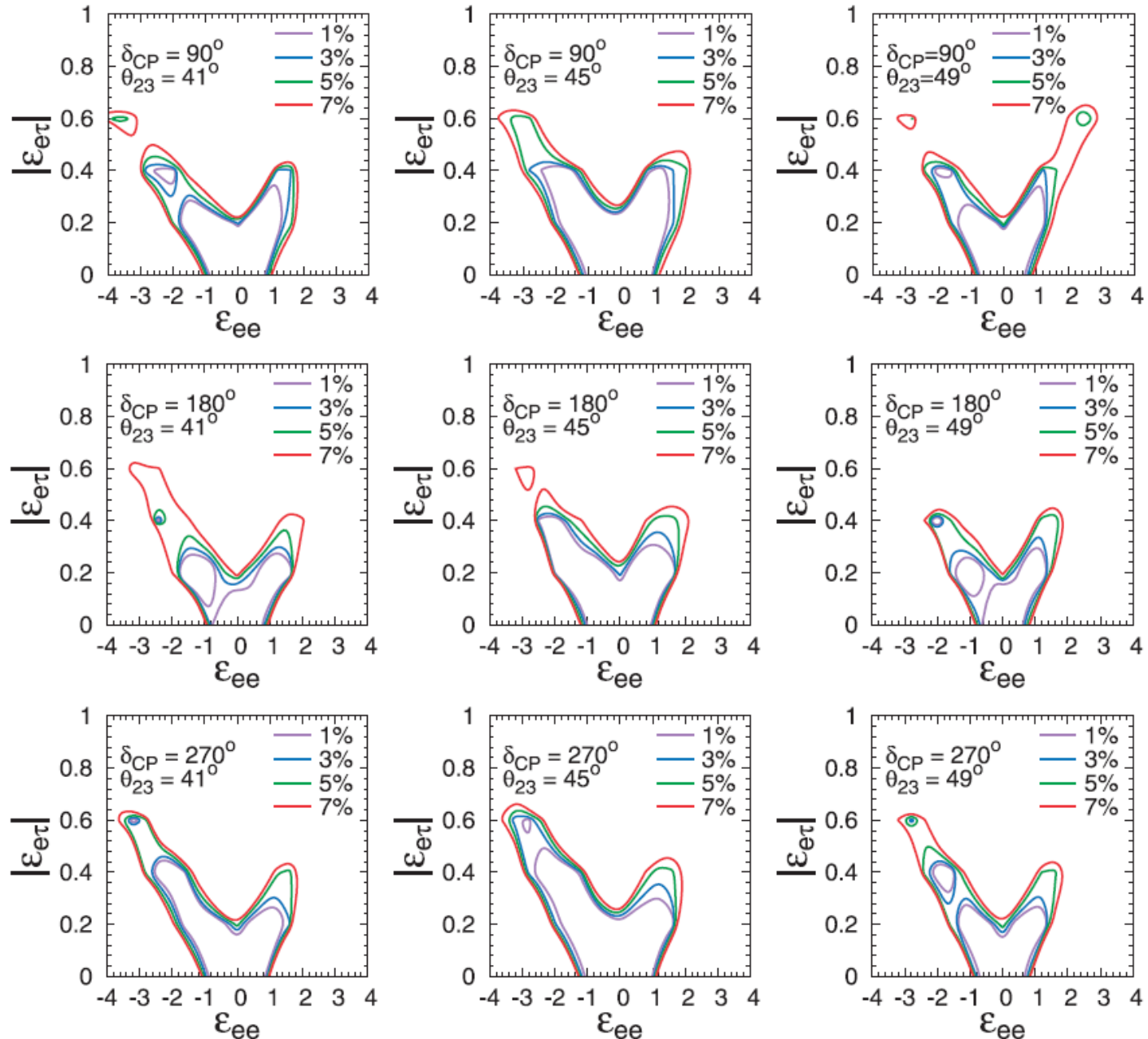


**DUNE better than T2HKK; Reduction from 5% to 3% enhances sensitivity to NSI in both experiments**

# Sensitivity of T2HKK to $(\epsilon_{ee}, |\epsilon_{e\tau}|)$ for various values of $\theta_{23}$ and $\delta_{CP}$

NH  $3\sigma$

PTEP 2018 ('18) 063C01, § 7.1, Monojit Ghosh & OY et al. (Hyper-Kamiokande Proto-Collaboration)

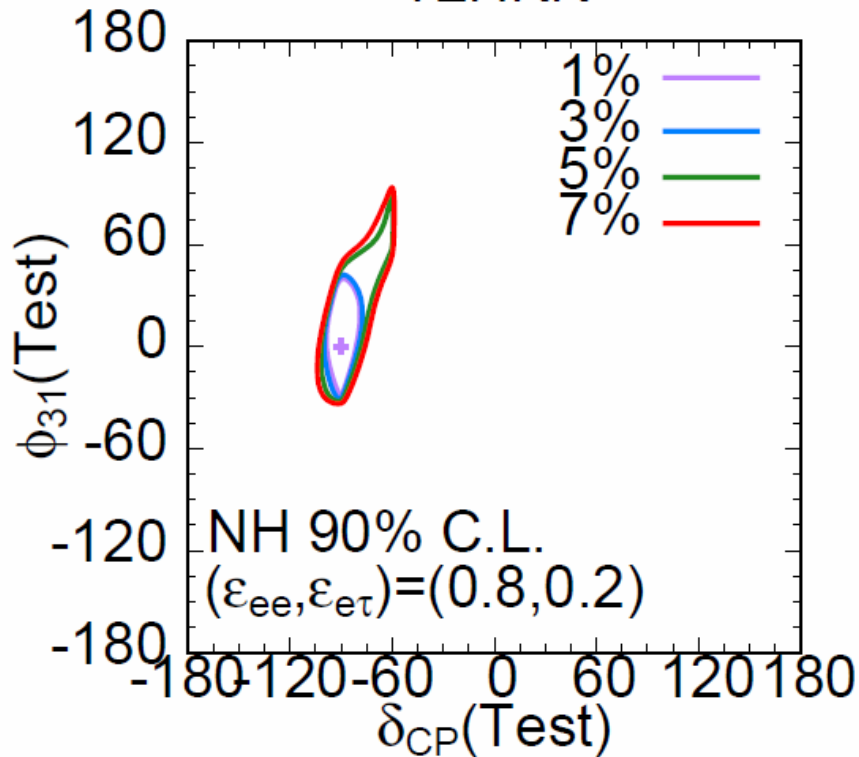


The behaviors w.r.t. the systematic errors are similar.

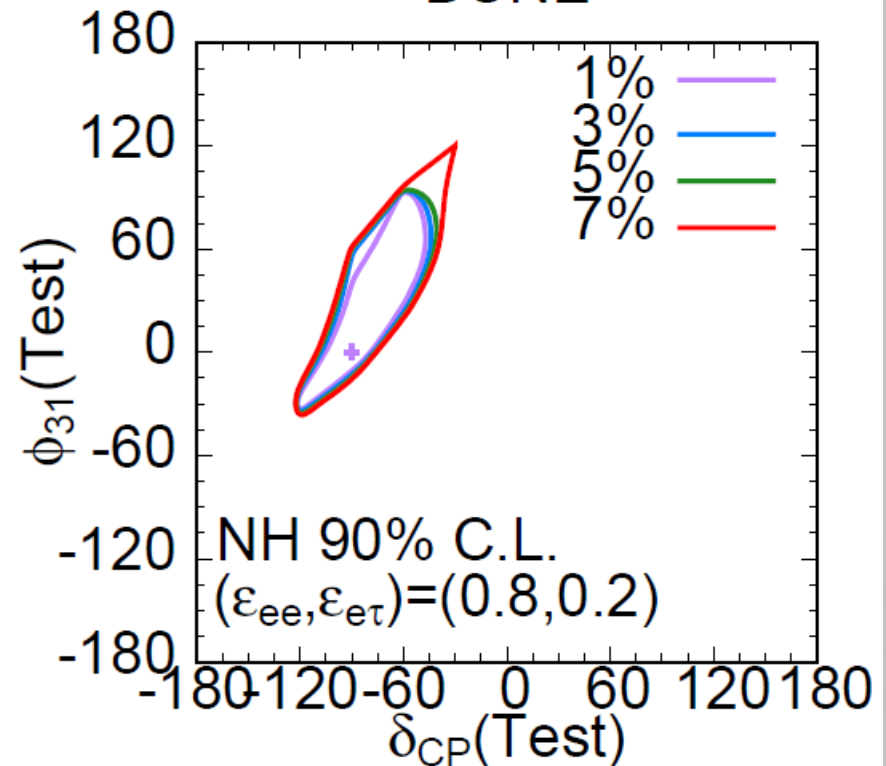
## 3.2 Sensitivity to $\phi_{31} \equiv \arg(\epsilon_{e\tau})$ & $\delta_{CP}$

PRD 96 ('17) 013001, Monojit Ghosh & OY

T2HKK



DUNE



**T2HKK better than DUNE; Reduction from 5% to 3% in T2HKK enhances sensitivity to the phases**

## 4. Conclusion

- Measurements of the oscillation parameters at the future LBL experiments are sensitive to the systematic errors in the standard 3 flavor case as well as in the NSI case.

- [Standard case]

If Mass Hierarchy is known & systematic error can be reduced to  $< 2\%$ , then T2HK has the best sensitivity to CP.

- [NSI case]

T2HK has much poorer sensitivity to NSI than other two;

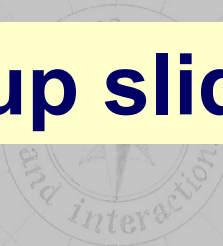
For  $(\varepsilon_{ee}, |\varepsilon_{e\tau}|)$ , DUNE w/  $c_1 < 5\%$  is the best;

For  $(\delta_{CP}, \arg(\varepsilon_{e\tau}))$ , T2HKK w/  $c_1 < 3\%$  is the best.

NOW MMXVIII



# Backup slides



v Compass Rose

# Hierarchy degeneracy in the three-flavor scenario

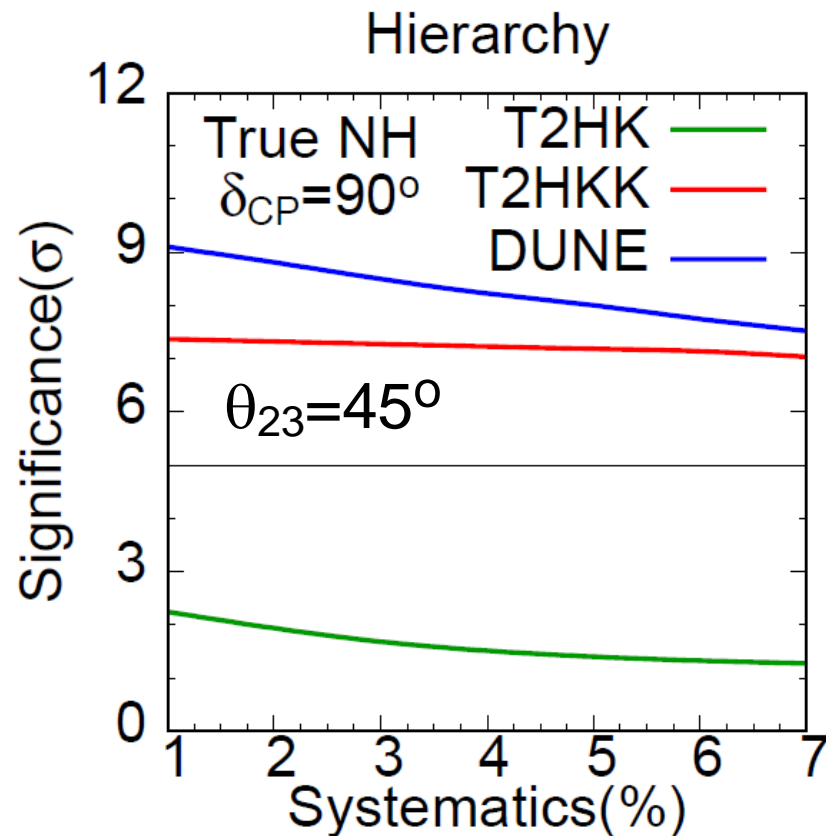
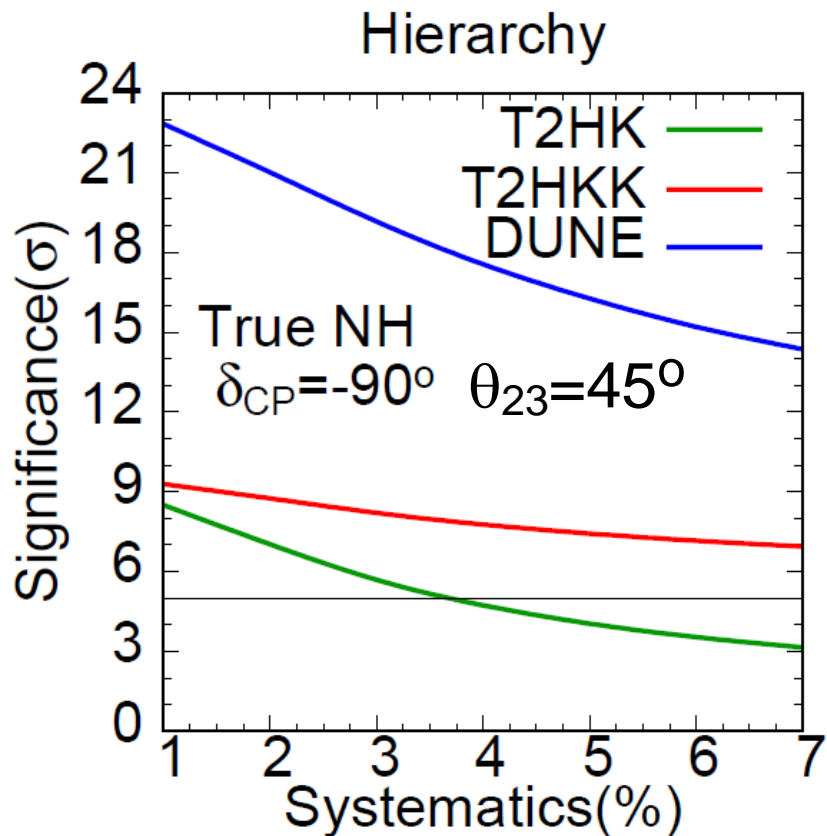
H. Nunokawa, S. J. Parke, R. Zukanovich  
Funchal, PRD 72, 013009 (2005)

$$P_{\mu\mu}(\Delta m_{\mu\mu}^2) = P_{\mu\mu}(-\Delta m_{\mu\mu}^2)$$

$$\Delta m_{31}^2 = \Delta m_{\mu\mu}^2 + (\cos^2 \theta_{12} - \cos \delta_{CP} \sin \theta_{13} \sin 2\theta_{12} \tan \theta_{23}) \Delta m_{21}^2$$

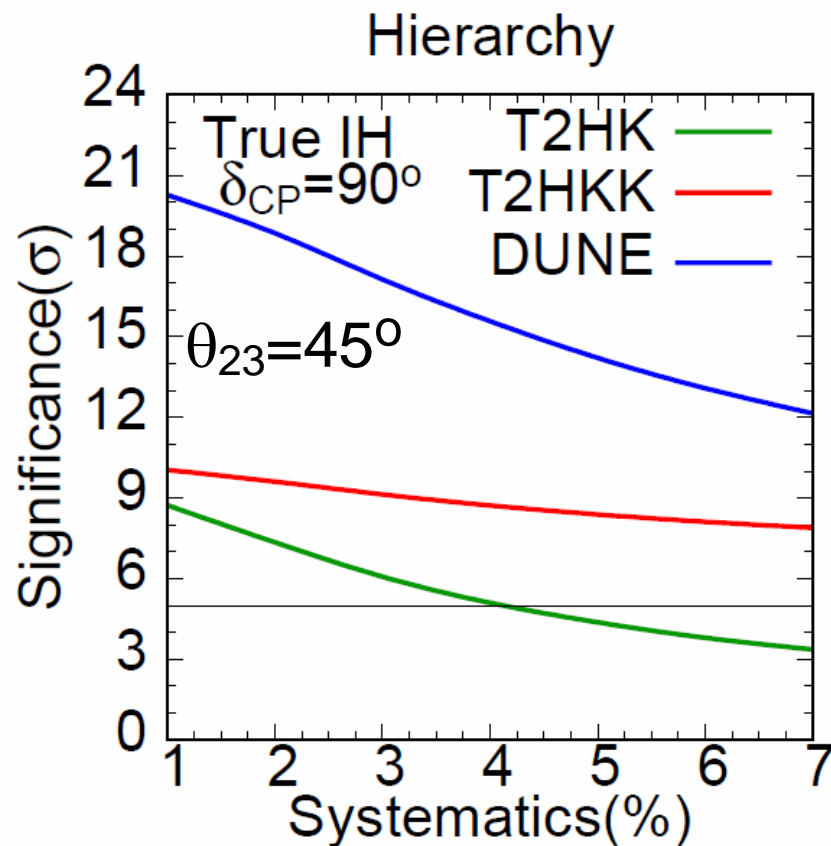
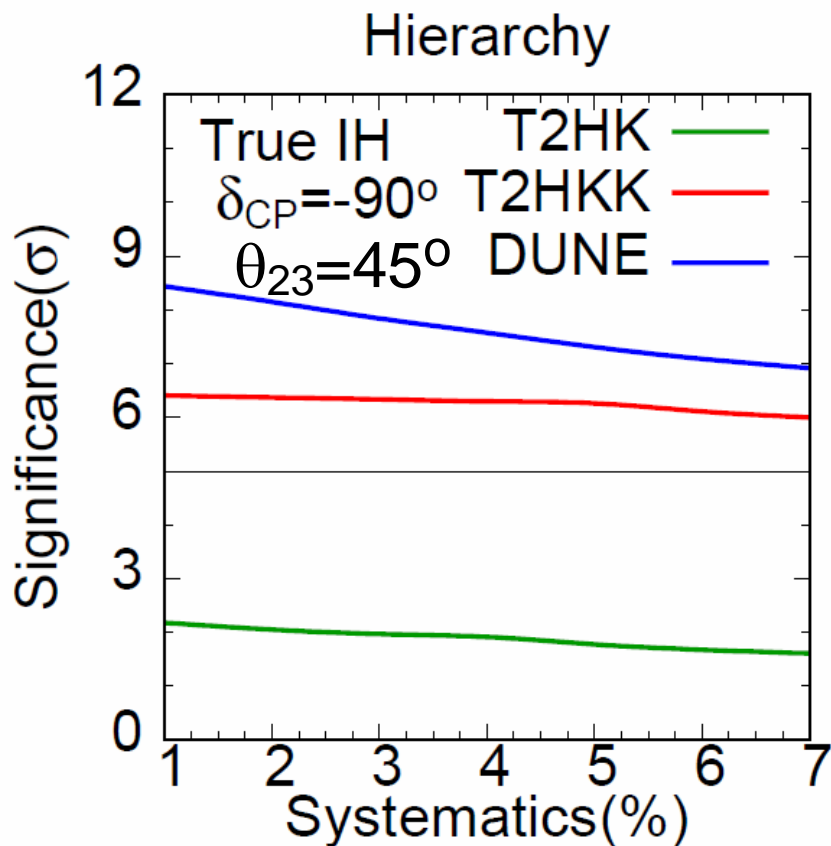
# Sensitivity to Mass Hierarchy

PRD 96 ('17) 013001, Monojit Ghosh & OY



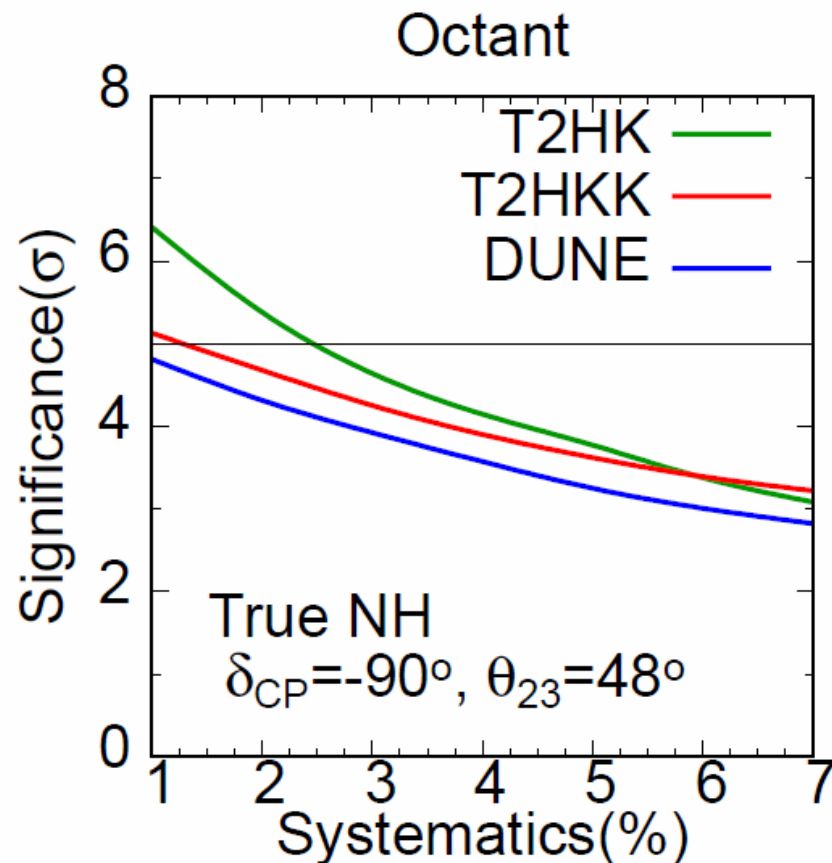
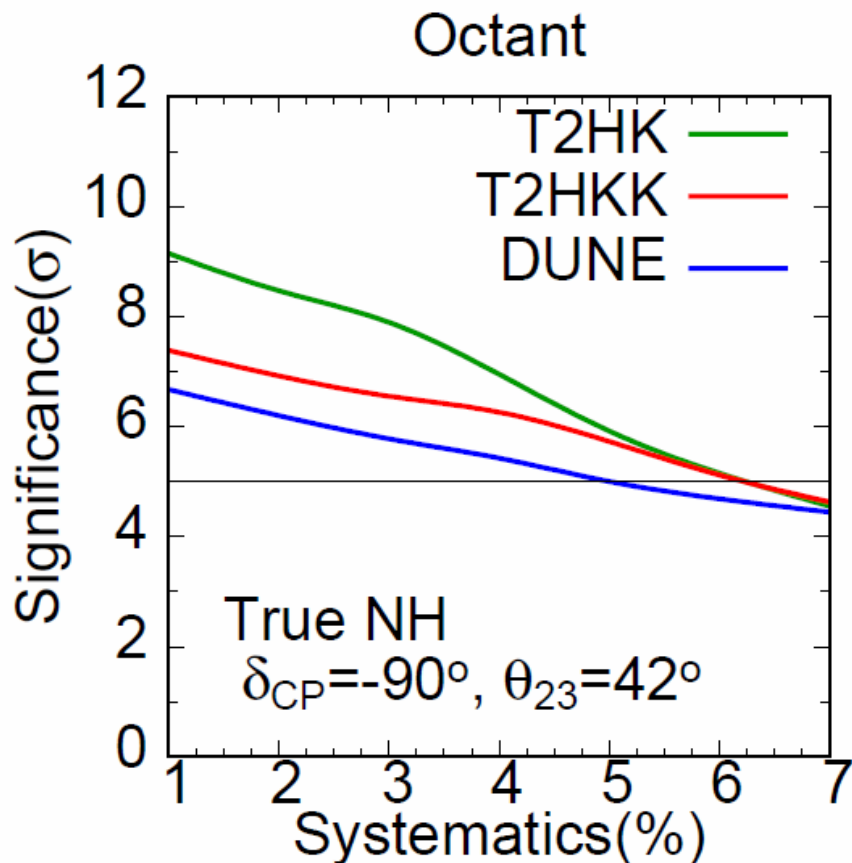
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PRD 96 ('17) 013001, Monojit Ghosh & OY



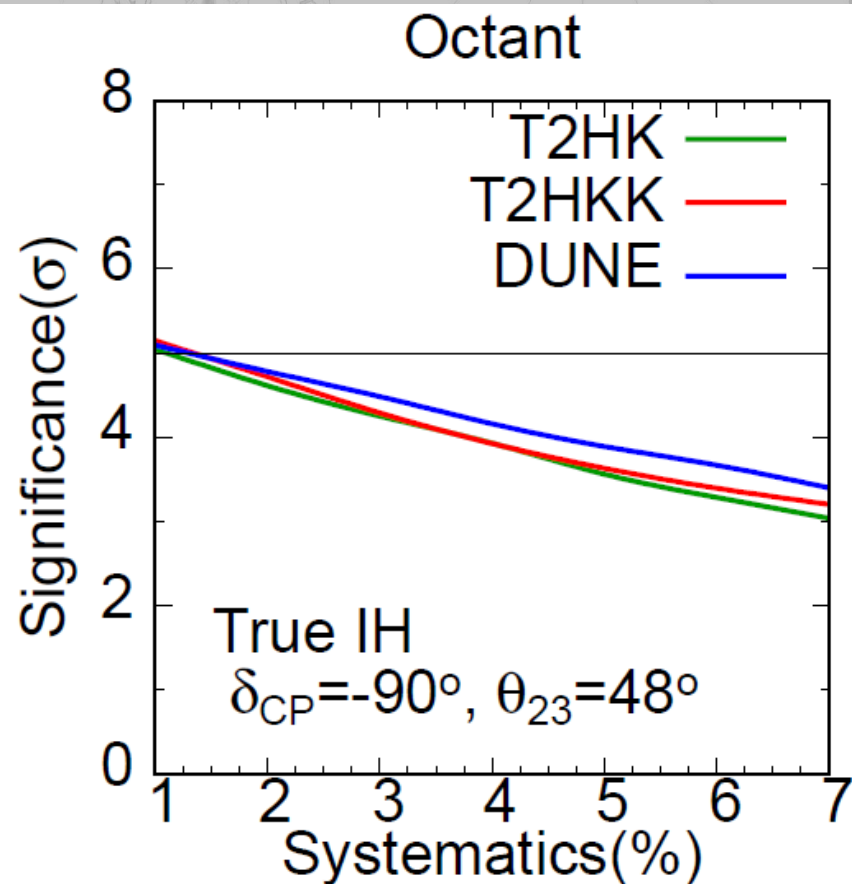
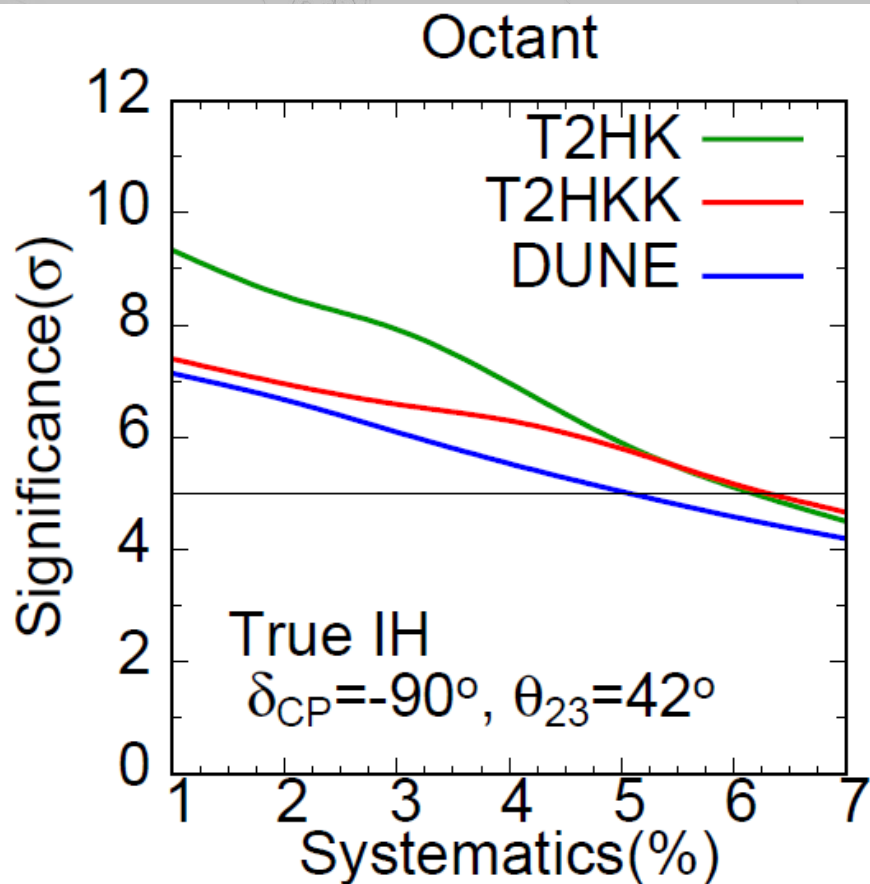
# Sensitivity to Octant

PRD 96 ('17) 013001, Monojit Ghosh & OY



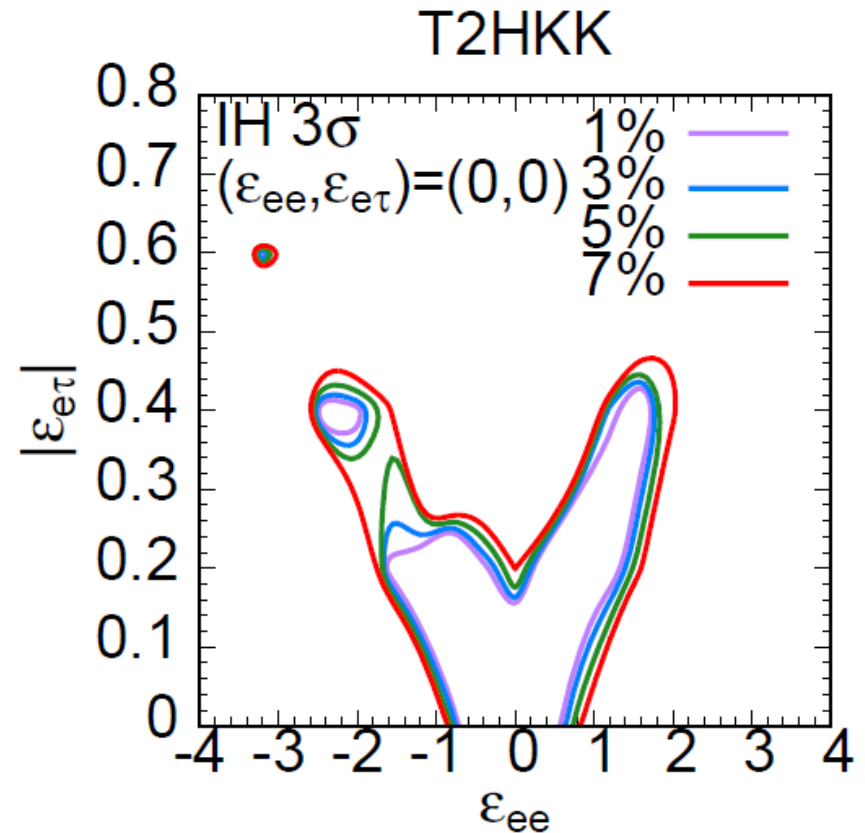
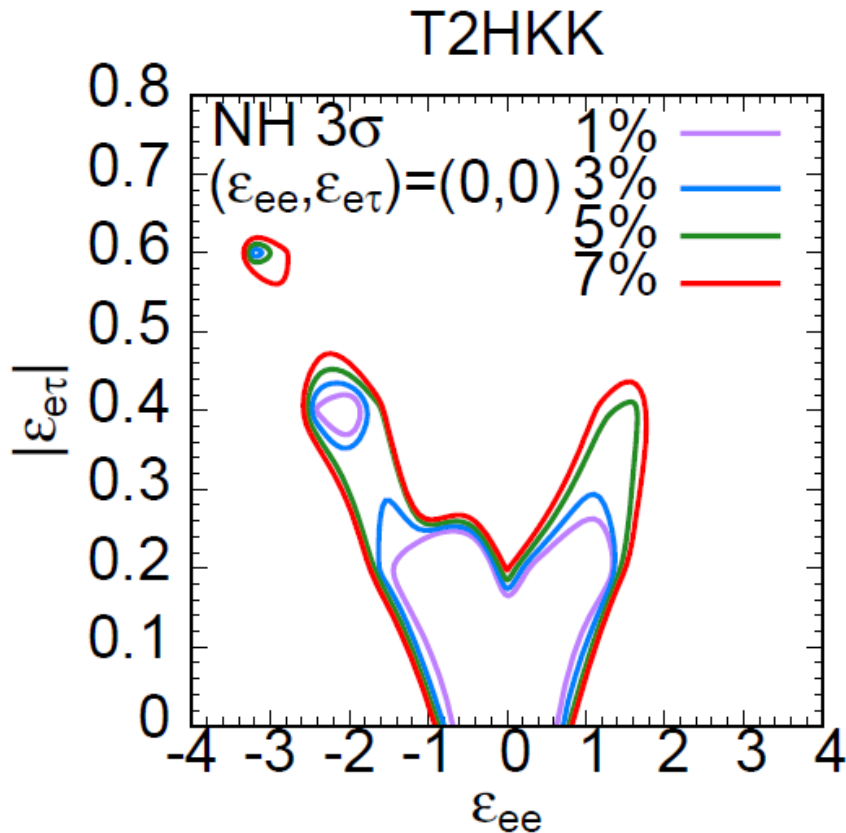
# Sensitivity to Octant

PRD 96 ('17) 013001, Monojit Ghosh & OY



# Sensitivity to $(\epsilon_{ee}, |\epsilon_{e\tau}|)$

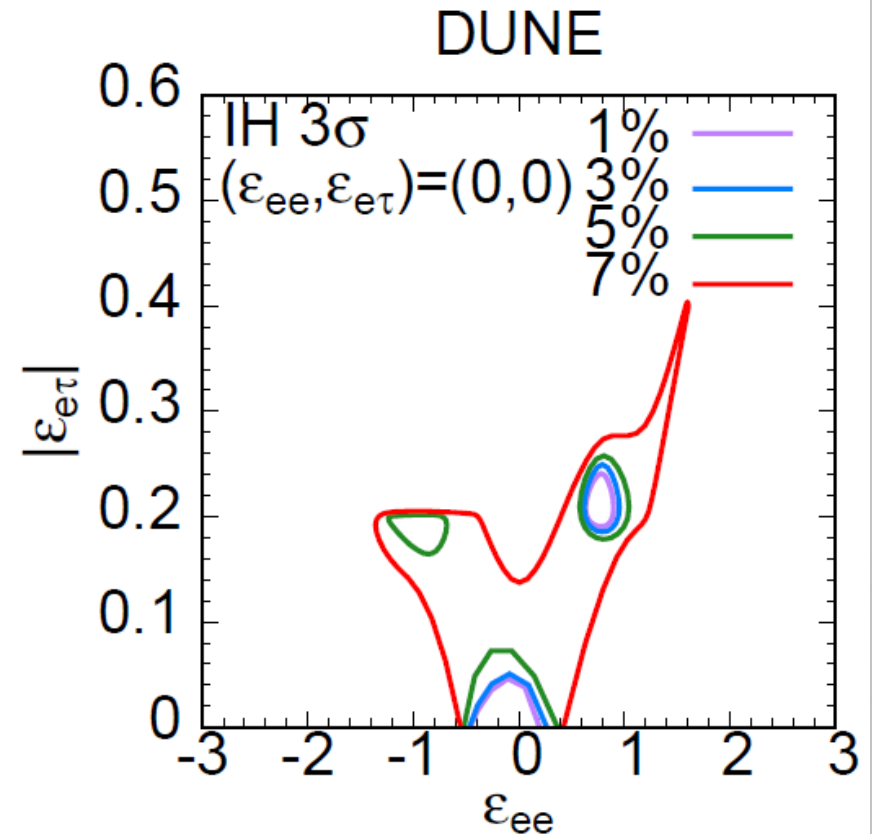
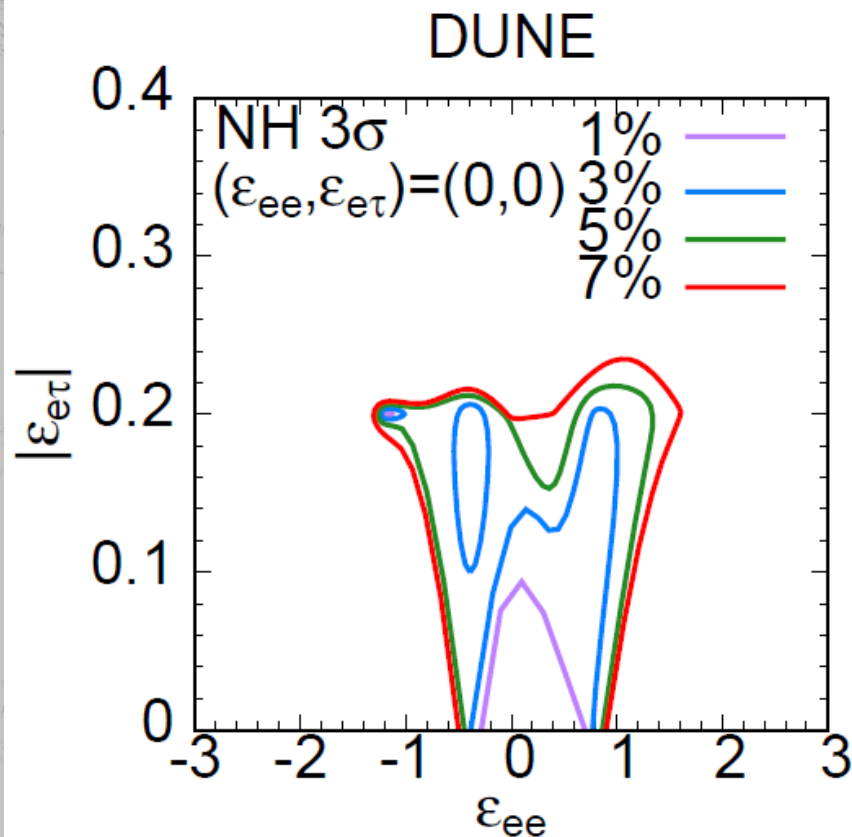
PRD 96 ('17) 013001, Monojit Ghosh & OY



True  $\delta_{CP} = -90^\circ$   $\theta_{23} = 45^\circ$   $\phi_{31} = 0$

# Sensitivity to $(\epsilon_{ee}, |\epsilon_{e\tau}|)$

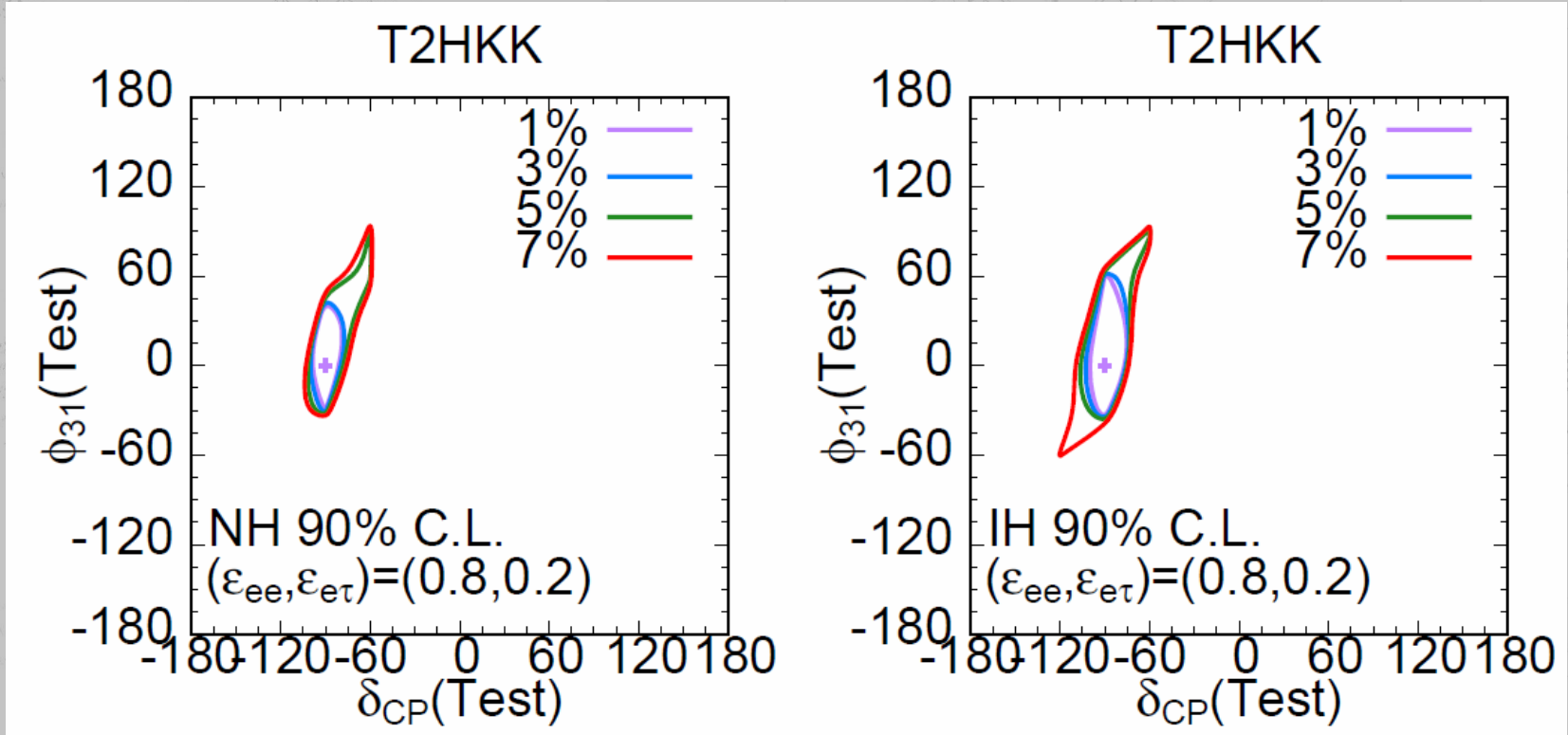
PRD 96 ('17) 013001, Monojit Ghosh & OY



True  $\delta_{CP} = -90^\circ$   $\theta_{23} = 45^\circ$   $\phi_{31} = 0$

# Sensitivity to $\phi_{31} \equiv \arg(\varepsilon_{e\tau})$ & $\delta_{CP}$

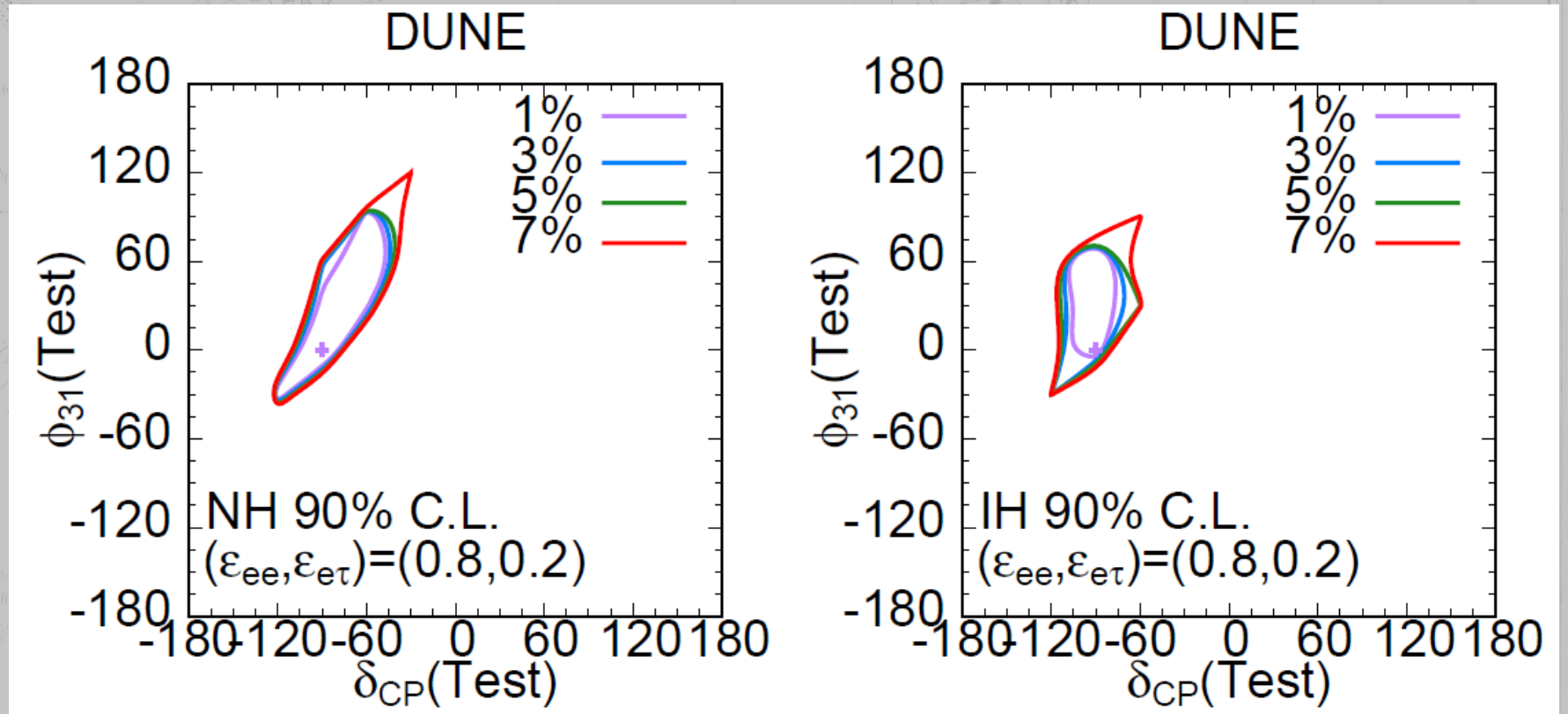
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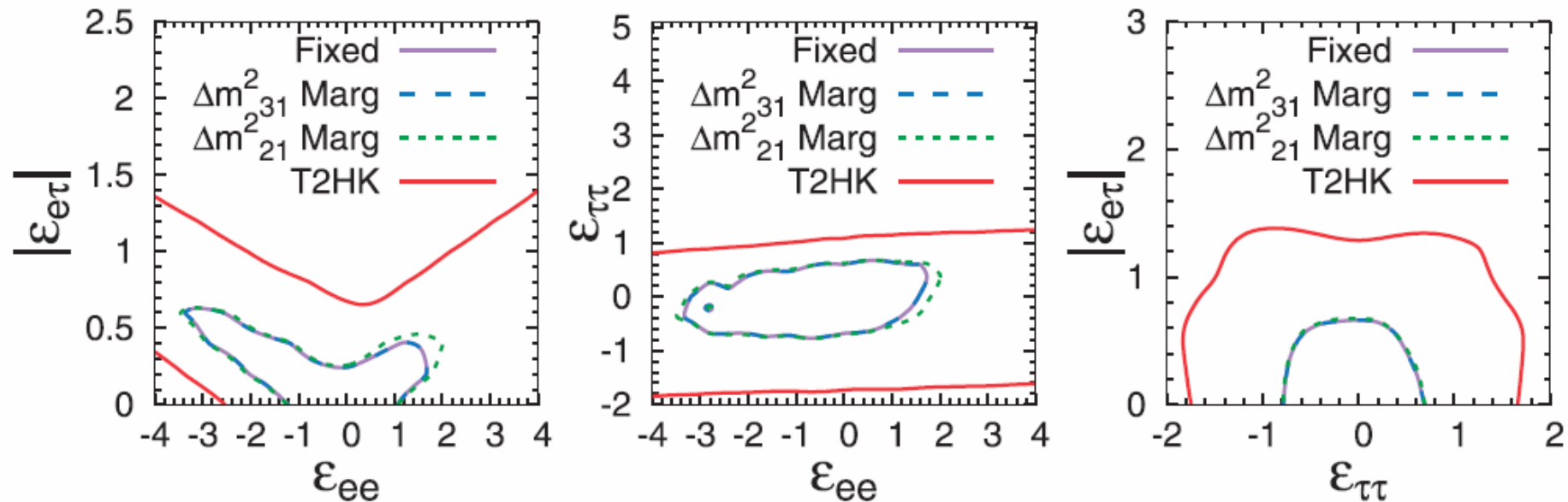
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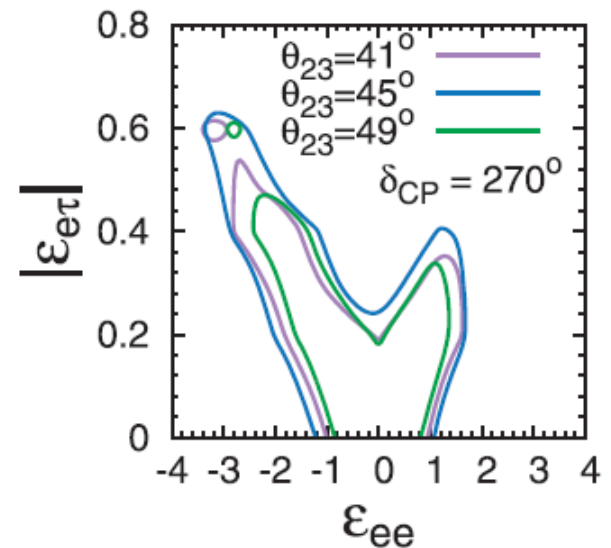
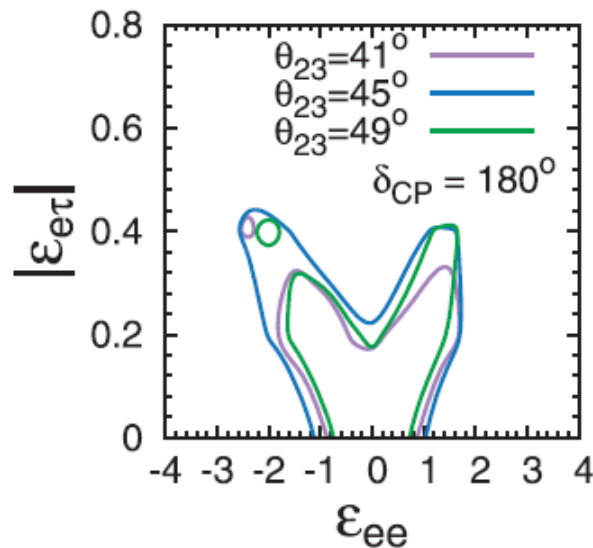
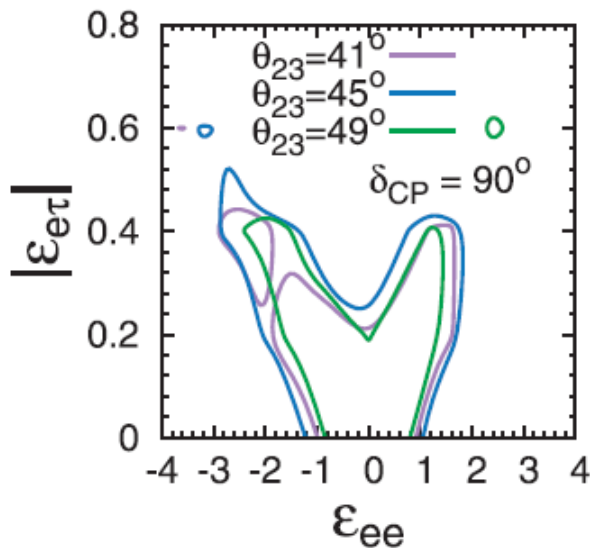
# Sensitivity of T2HKK to $(\epsilon_{ee}, |\epsilon_{e\tau}|)$ w/ or w/o marginalization w.r.t. each $\Delta m^2_{jk}$

PTEP 2018 ('18) 063C01, § 7.1, Monojit Ghosh & OY et al. (Hyper-Kamiokande Proto-Collaboration)



# Sensitivity of T2HKK to $(\epsilon_{ee}, |\epsilon_{e\tau}|)$ for various values of $\theta_{23}$ and $\delta_{CP}$

PTEP 2018 ('18) 063C01, § 7.1, Monojit Ghosh & OY et al.  
(Hyper-Kamiokande Proto-Collaboration)



**Sensitivity of T2HKK to  $(\epsilon_{ee}, |\epsilon_{e\tau}|)$  for various values of  $\theta_{23}$  w/o the condition  $\epsilon_{\tau\tau} = |\epsilon_{e\tau}|^2 / (1 + \epsilon_{ee})$**

**PTEP 2018 ('18) 063C01,  
§ 7.1, Monojit Ghosh &  
OY et al. (Hyper-  
Kamiokande Proto-  
Collaboration)**

