

# LONG RANGE SPIN GLASS FROM SHORT RANGE ANTIFERROMAGNETS

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in collaboration with

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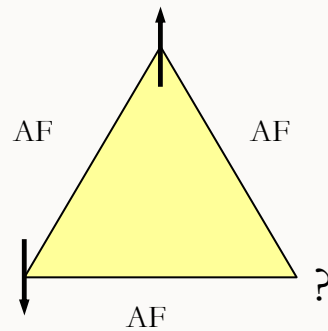


# OVERVIEW

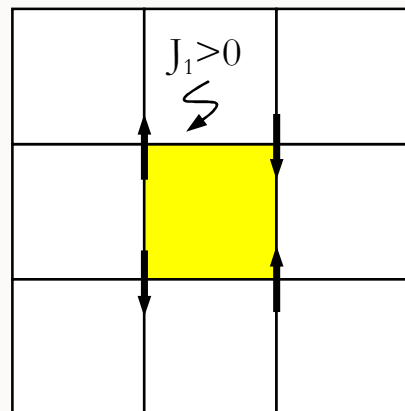
- Frustrated magnets at low temperatures
- Doping and orphan spins
- A two-dimensional, long range spin glass

# FRUSTRATED MAGNETS

## Classical Spins

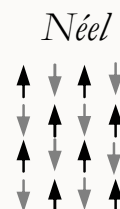


Antiferromagnetic interactions can create frustration



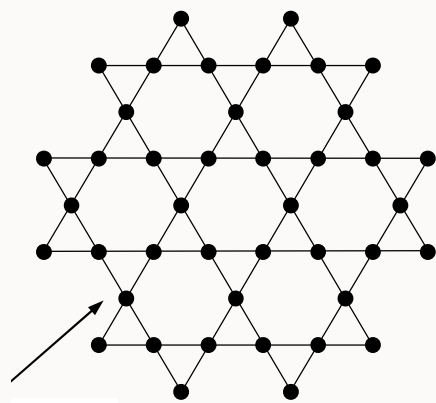
Some AF order to Neel states at  $T=0 K$

(a)



# FRUSTRATED MAGNETS

Some AF models *do not* order even at  $T=0$  K



Kagome lattice

Is a *spin liquid*, where the ground state is macroscopically degenerate but no order exists

$$\text{Ising} \quad \langle S_i S_j \rangle \sim e^{-r_{ij}/\xi}$$

It all depends on the lattice!

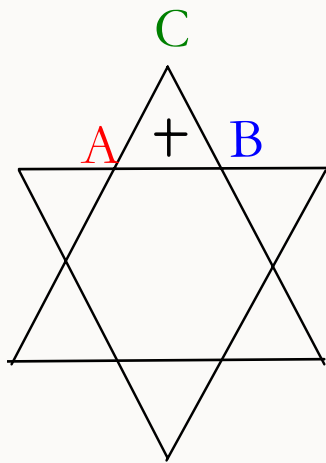


# FRUSTRATED MAGNETS

Heisenberg on Kagome

$$H = J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j$$

$$H = J \sum_{\text{triangles}} (\mathbf{S}_A + \mathbf{S}_B + \mathbf{S}_C)^2 - \frac{J}{2} \sum_i \mathbf{S}_i^2$$



So at T=0

$$\mathbf{S}_A + \mathbf{S}_B + \mathbf{S}_C = 0$$

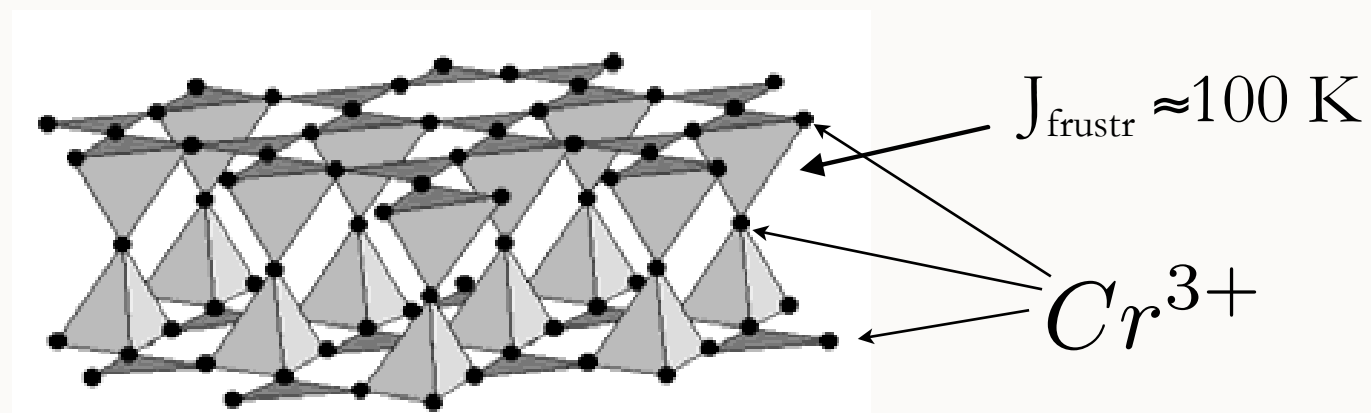
local conditions

Finite entropy!

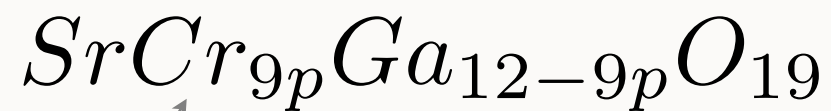
even after fixing SO(3)

# FRUSTRATED MAGNETS

This is a *spin liquid* to remarkably low  $T$



$$p = 1$$

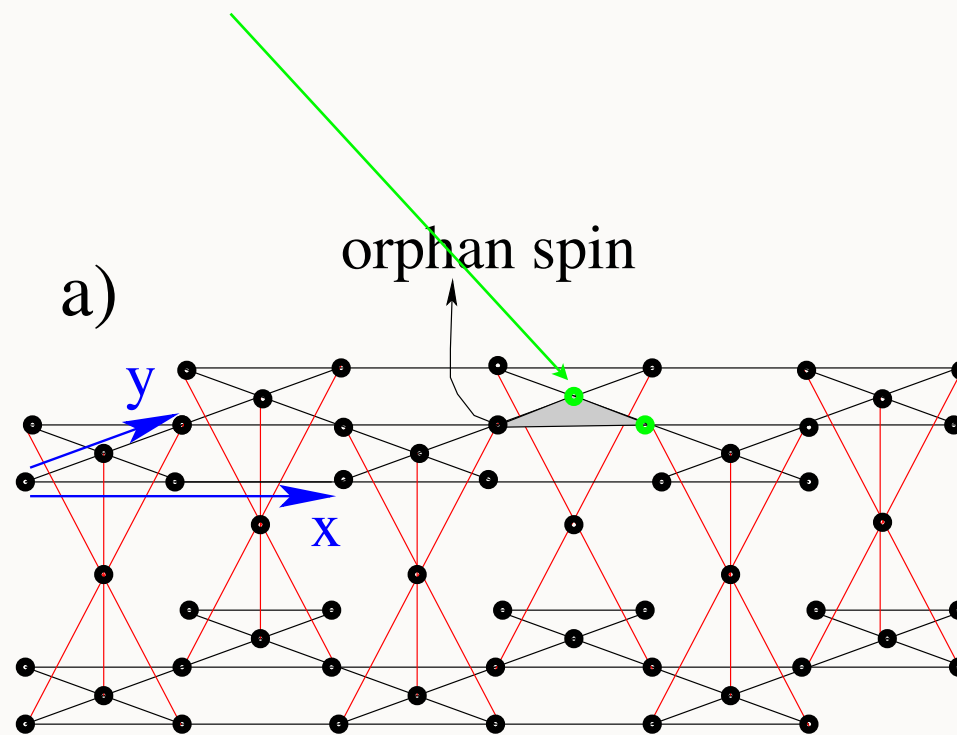


Magnetic

Non magnetic

# DOPING

Doping with *Ga* which is non-magnetic



The important situation is when two *Ga* fall in the same simplex

This leaves behind *orphan spin Cr*

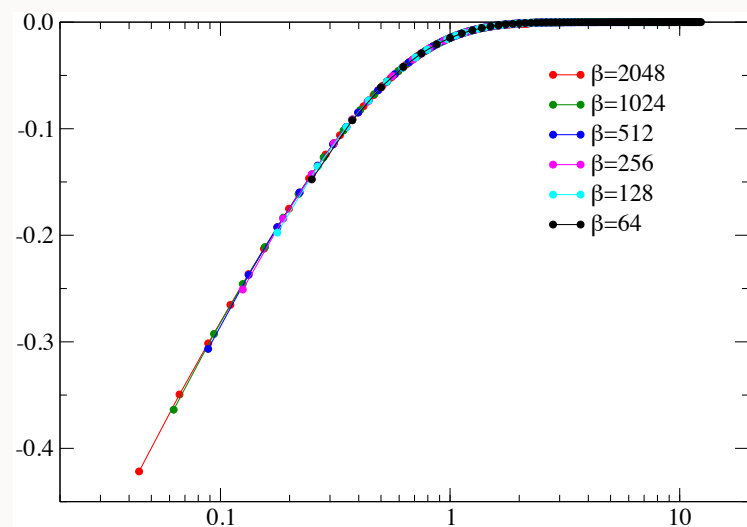


# DOPING

Montecarlo simulations show that effectively

$$H = \sum_{ij} J_{eff}(r_{ij}) \mathbf{S}_i \cdot \mathbf{S}_j$$

$$J_{eff}(r_{ij}) = -T \mathcal{J}(\sqrt{T} r_{ij})$$



$$\mathcal{J}(y) \simeq \log(1/y) \quad y \ll 1$$

$$\mathcal{J}(y) \simeq e^{-y} \quad y \gg 1$$



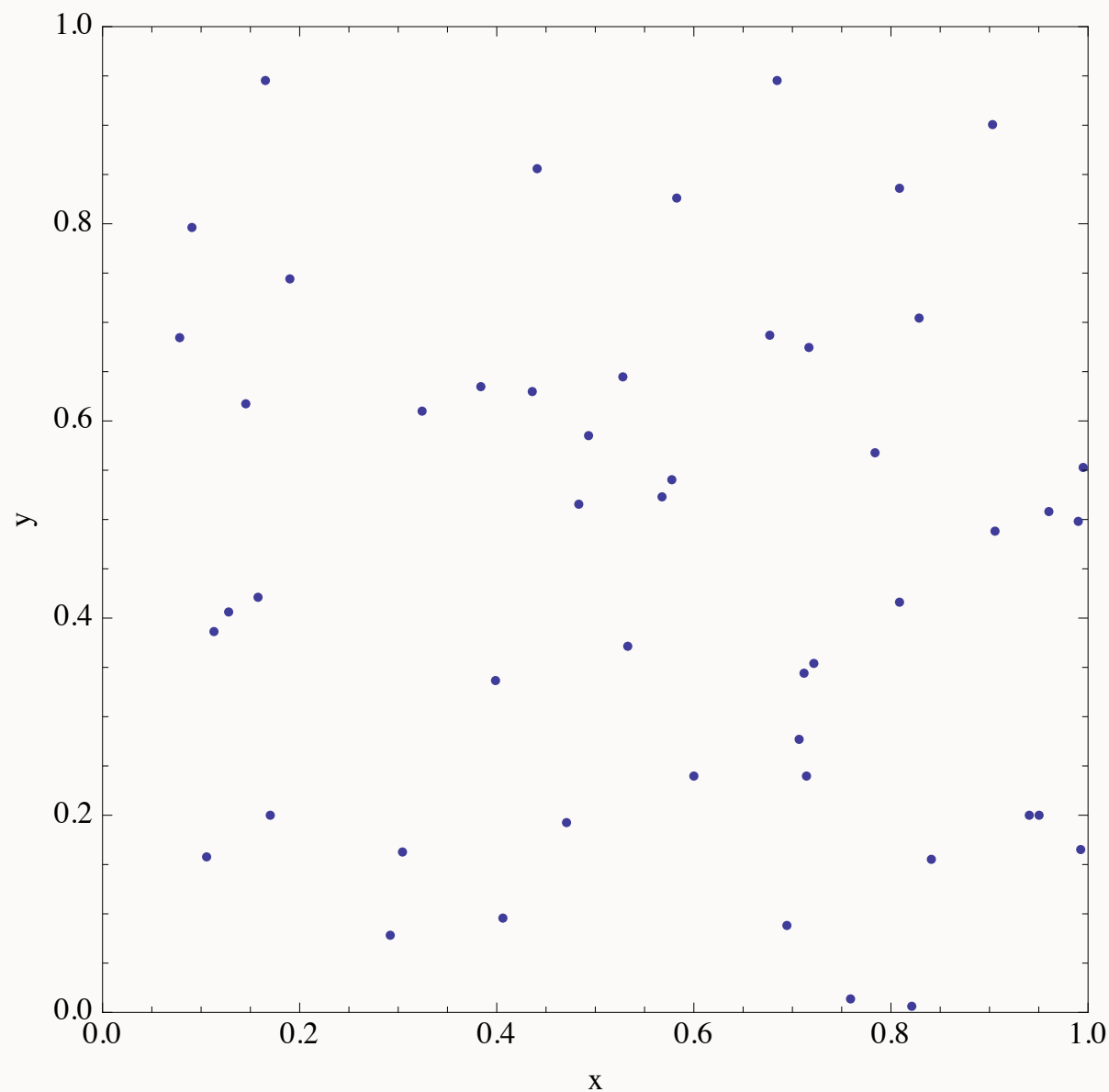
# DOPING

The long-range correlations of the spin liquid implies long-range interactions of the *orphan spins*

$$H = \sum_{ij} J_{eff}(r_{ij}) \mathbf{S}_i \cdot \mathbf{S}_j$$

the locations of the spins are random

# LONG RANGE SPIN GLASS



$$H = \sum_{ij} J_{eff}(r_{ij}) \mathbf{S}_i \cdot \mathbf{S}_j$$

Frustration+disorder

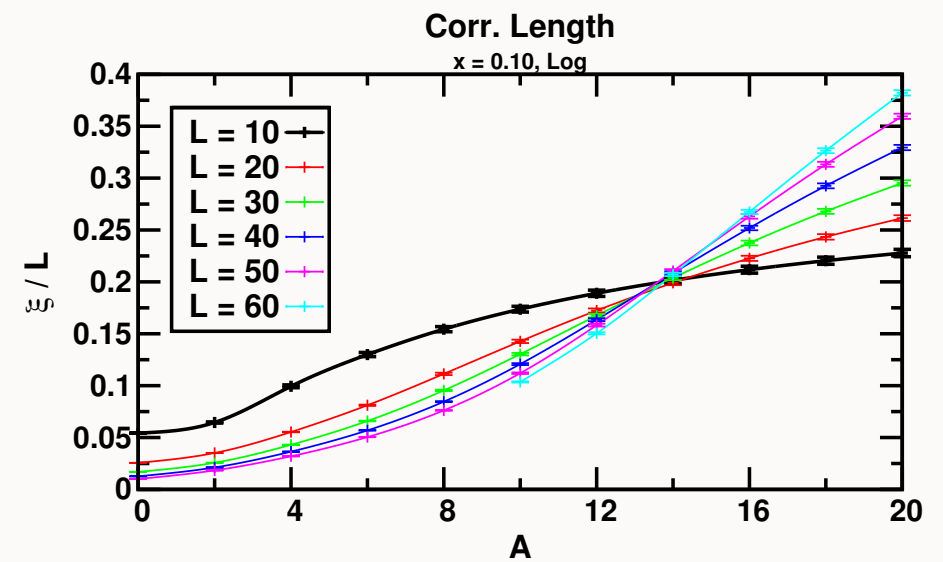
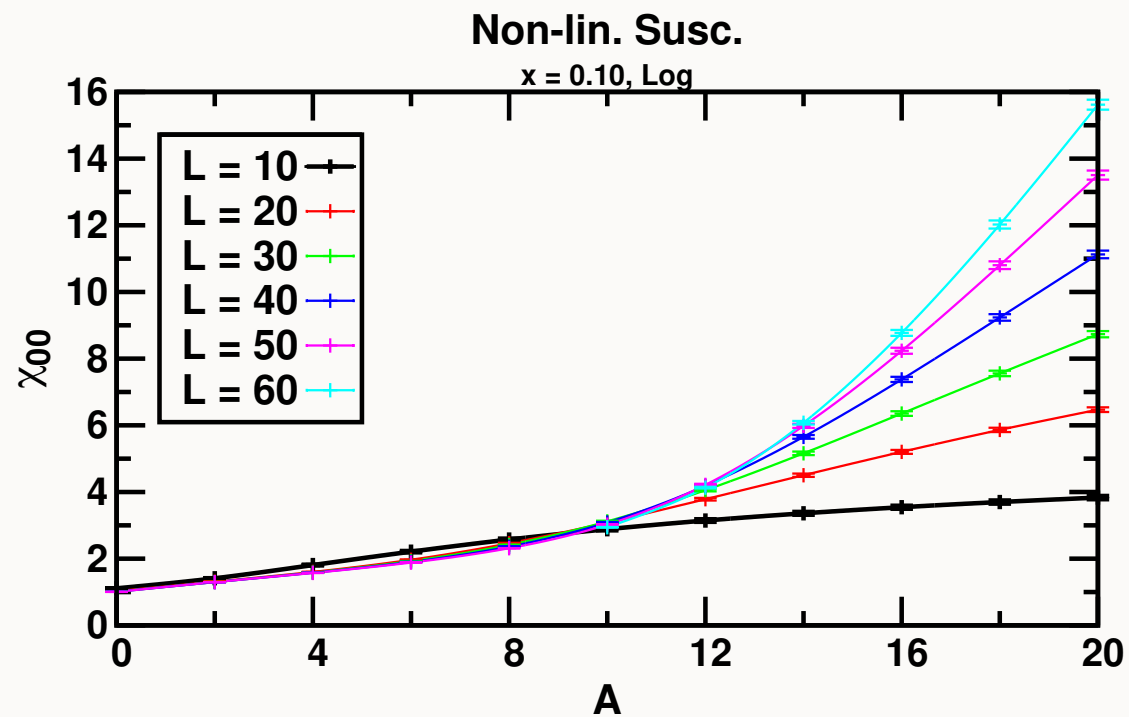
Does it have a  
spin glass phase?



# LONG RANGE SPIN GLASS

Apparently yes

Divergences in the large coupling limit



# LONG RANGE SPIN GLASS

Details:

$$\chi(\vec{k}) = N \sum_{\alpha, \beta} \langle |Q_{\vec{k}}^{\alpha, \beta}|^2 \rangle,$$

$$Q_{\vec{k}}^{\alpha, \beta}(t) = \frac{1}{N} \sum_i S_{i,1}^{\alpha}(t) S_{i,2}^{\beta}(t) e^{i\vec{k} \cdot \vec{r}_i}.$$

$$\xi_L = \frac{1}{2 \sin(k_{min}/2)} \left( \frac{\chi_{SG}(0)}{\chi_{SG}(\vec{k}_{min})} - 1 \right)^{1/2} ;$$



# LONG RANGE SPIN GLASS

Still in the working:

- a) Is it really a glassy phase?
- b) Does it look like a long-range (SK-like) or short range ( $d=2$ ) SG?
- c) What is the critical phase?
- d) What about many local minima in the SG phase?

# CONCLUSIONS



Thank you and Merry Christmas in the  
city of Santa Claus