



The Higgs boson and Top quark masses as test of Electroweak Vacuum Stability (+ impact of neutrinos)



Isabella Masina

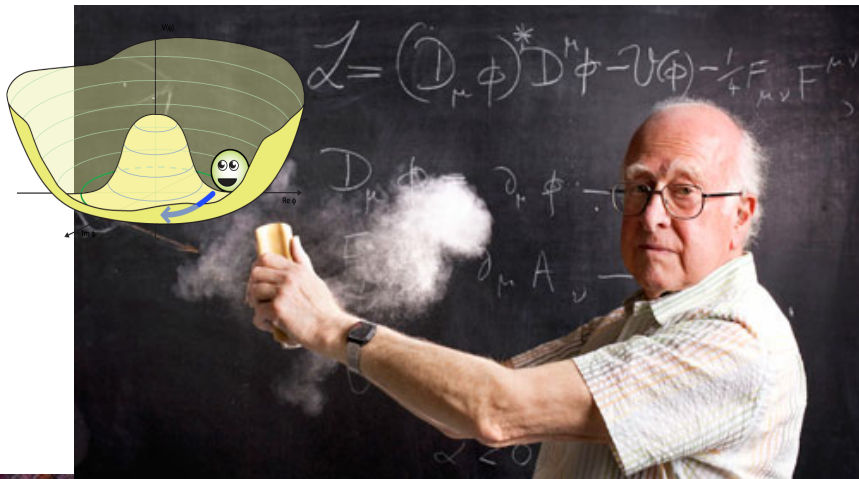
University of Ferrara and CP3-Origins Denmark

Neutrino Oscillation Workshop

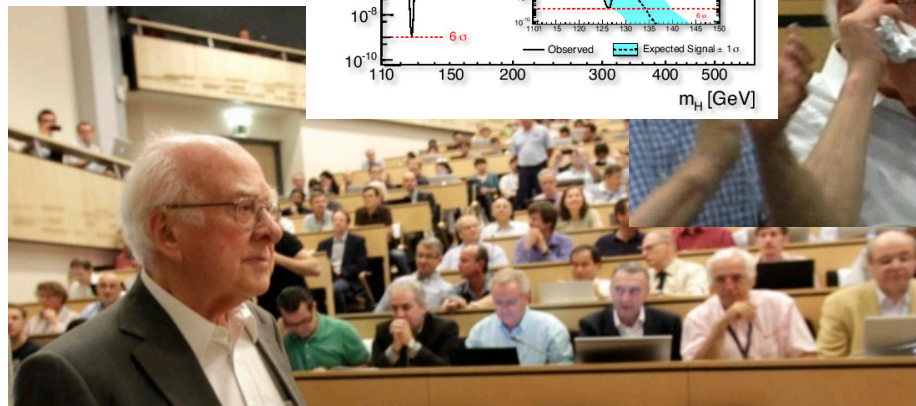
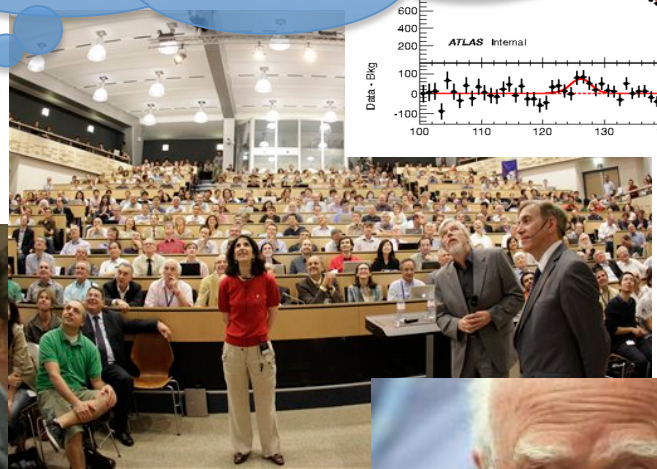
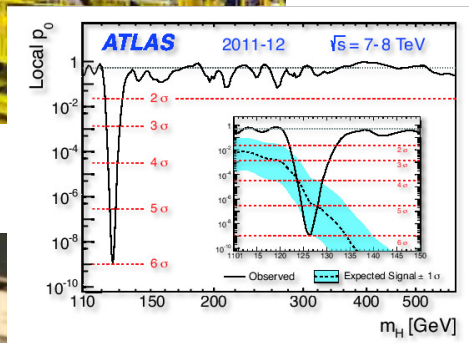
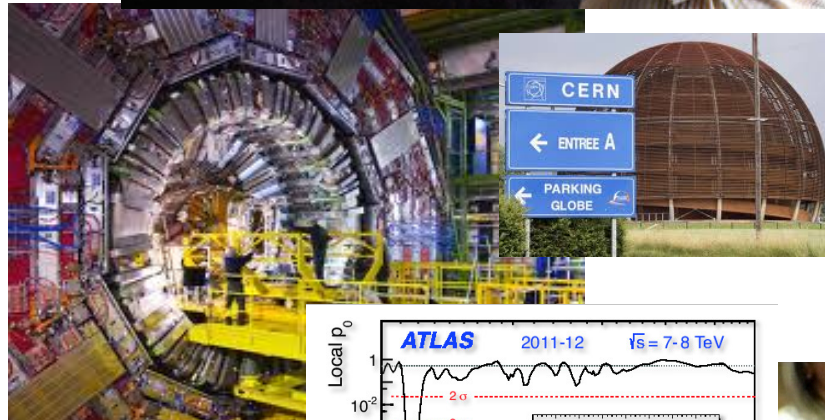
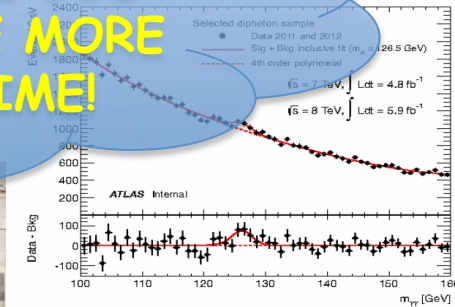
Conca Specchiulla, Otranto, Lecce, Italy

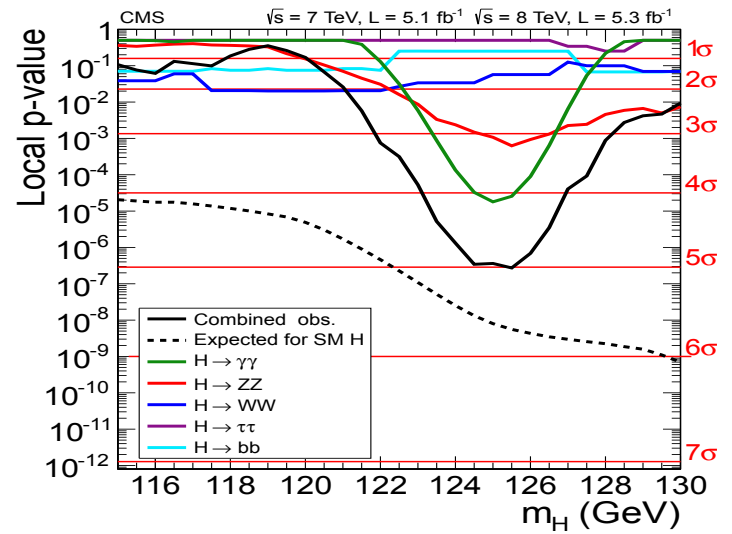
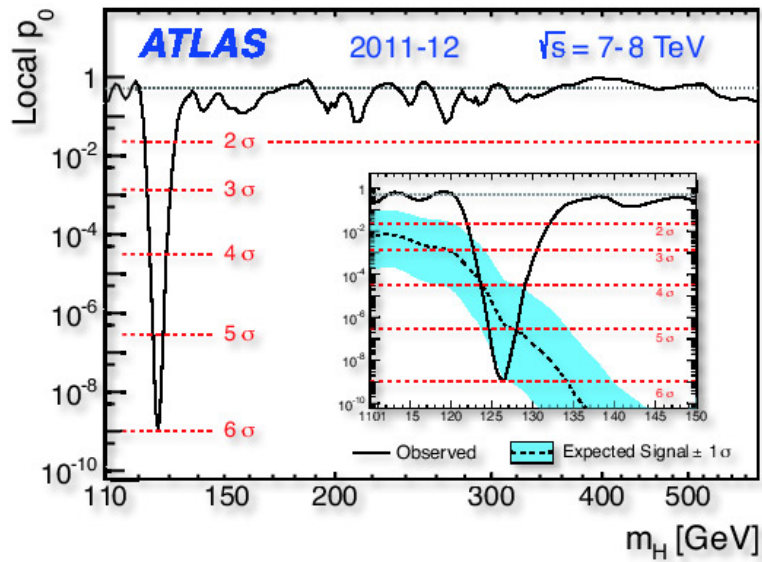
September 9-16, 2012





**DON'T CALL ME GOD
PARTICLE ONCE MORE
GODDAMN TIME!**





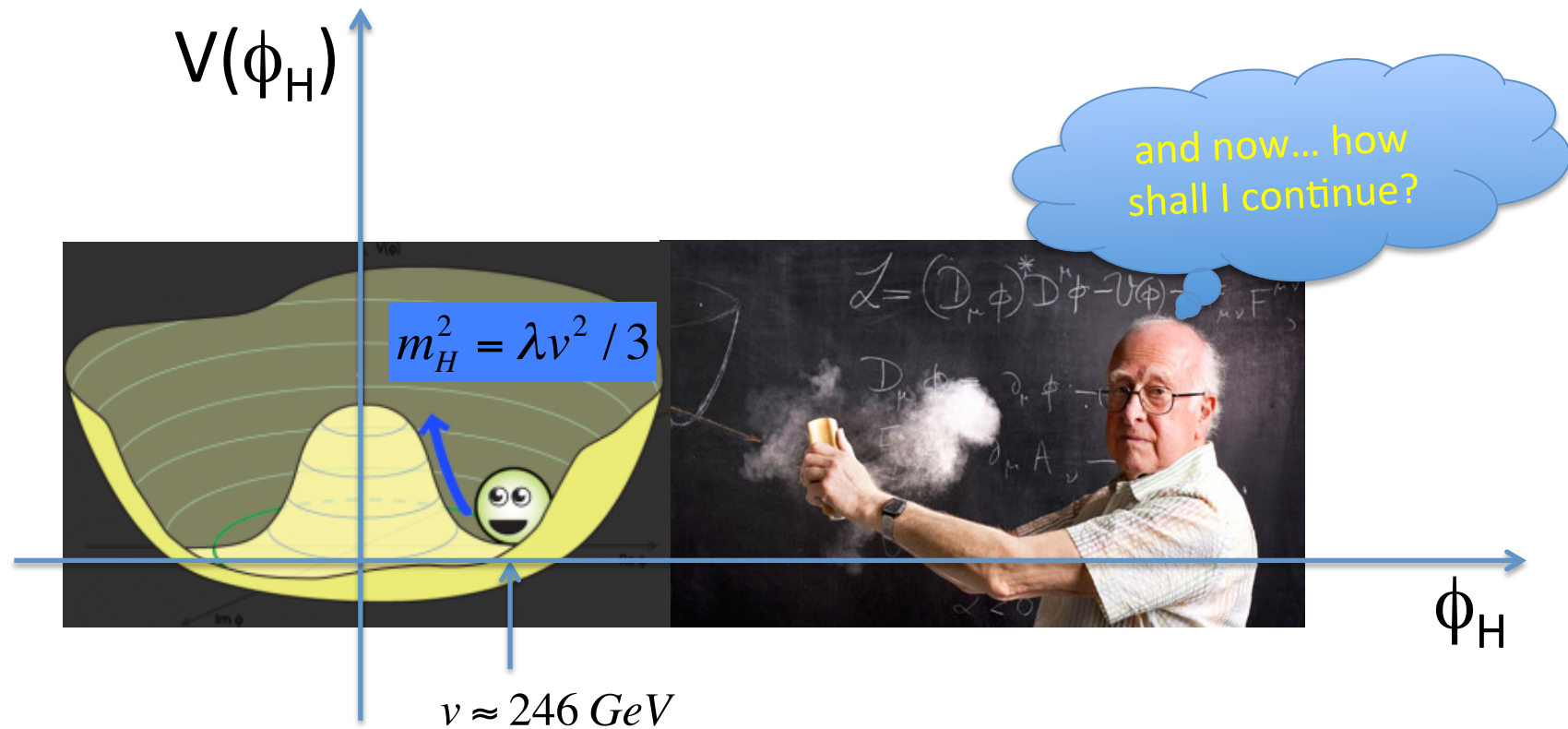
$$m_H = 124.8 - 126.5 \text{ GeV}$$

@2 σ

SO WHAT?

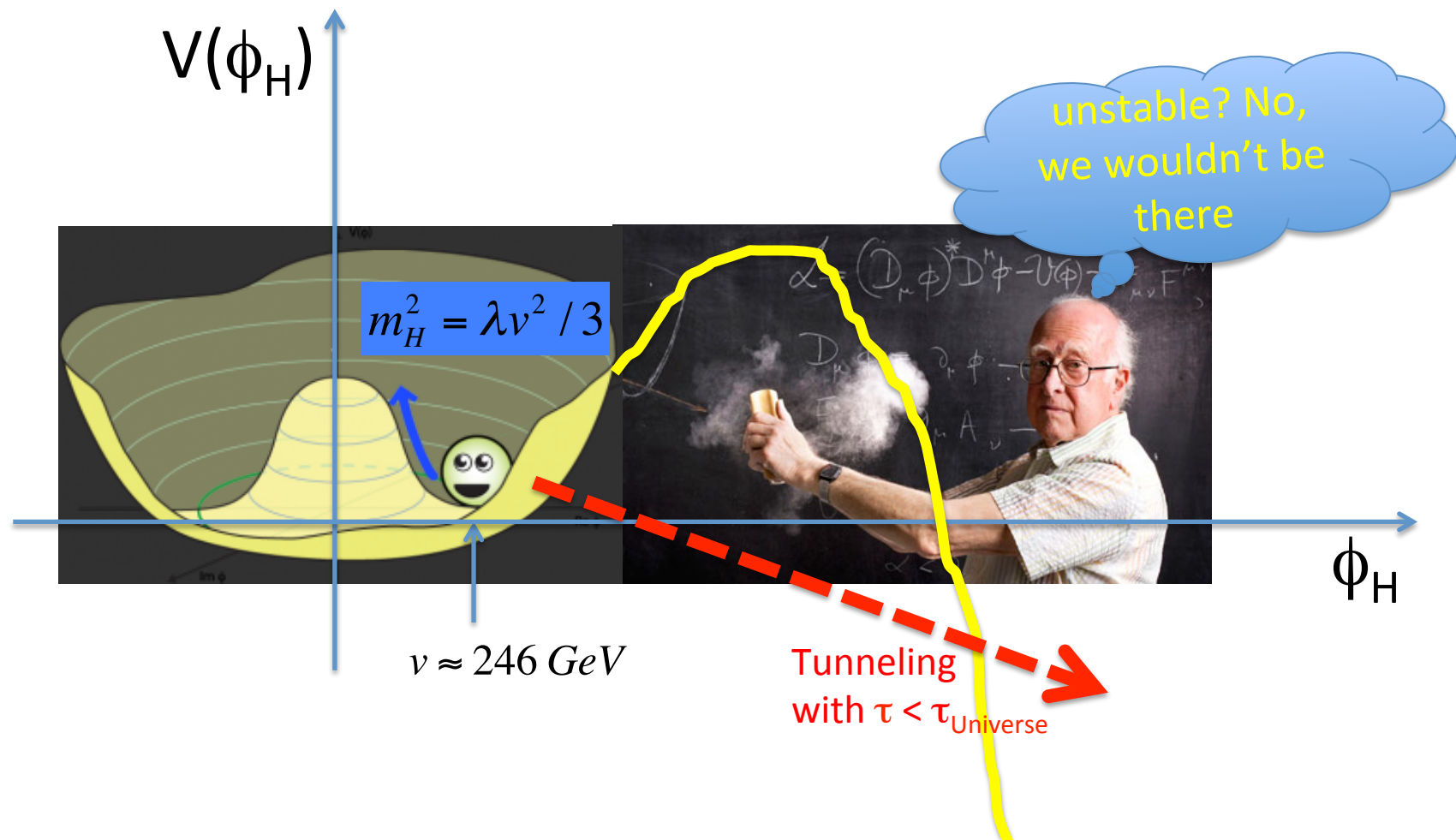
Consider the Higgs doublet $H = (0, (\phi_H + v)/\sqrt{2})$

and the SM Higgs potential: $V(\phi_H) = \frac{\lambda}{6} \left(|H|^2 - \frac{v^2}{2} \right)^2 \approx \frac{\lambda}{24} \phi_H^4$



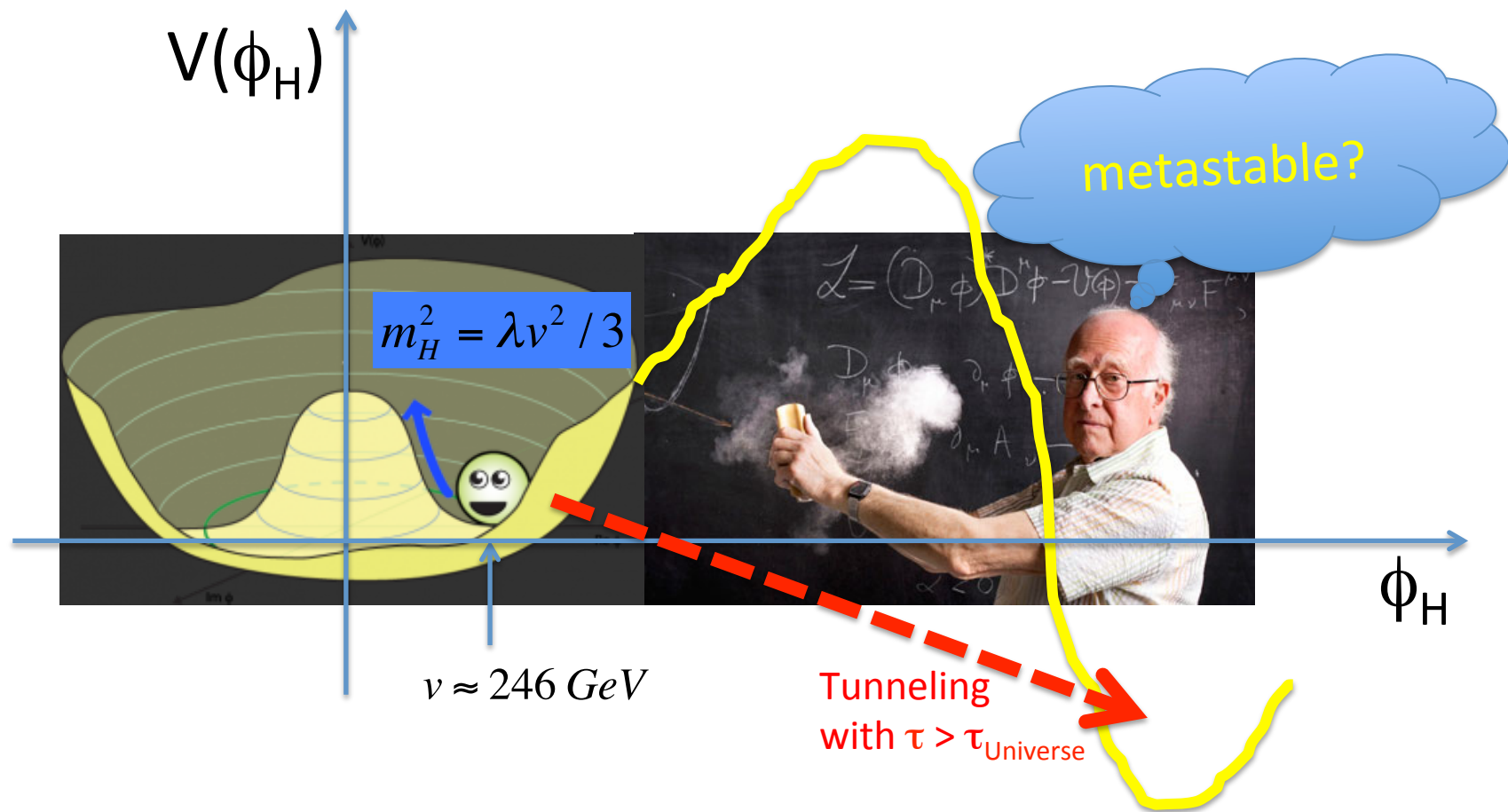
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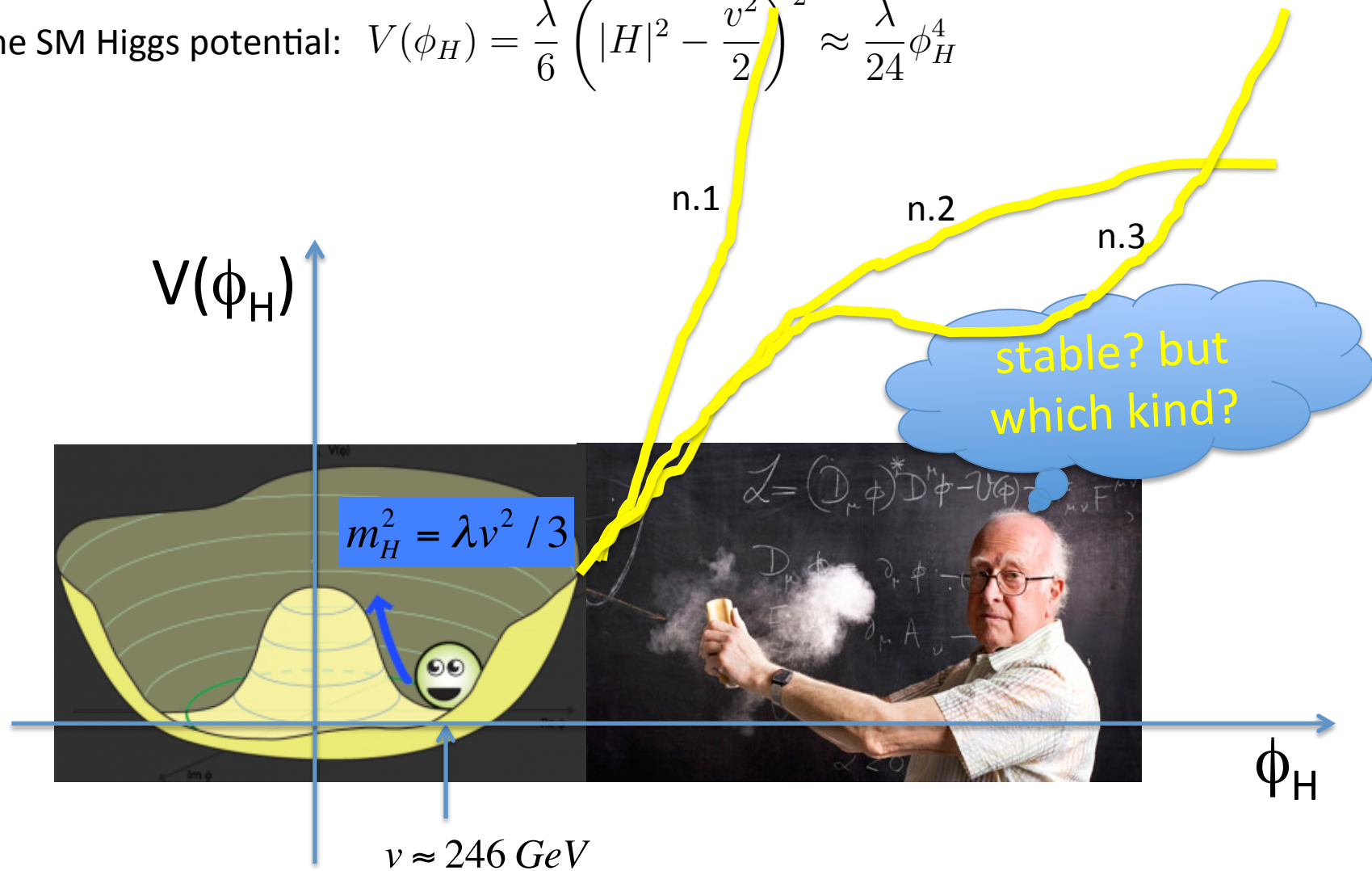
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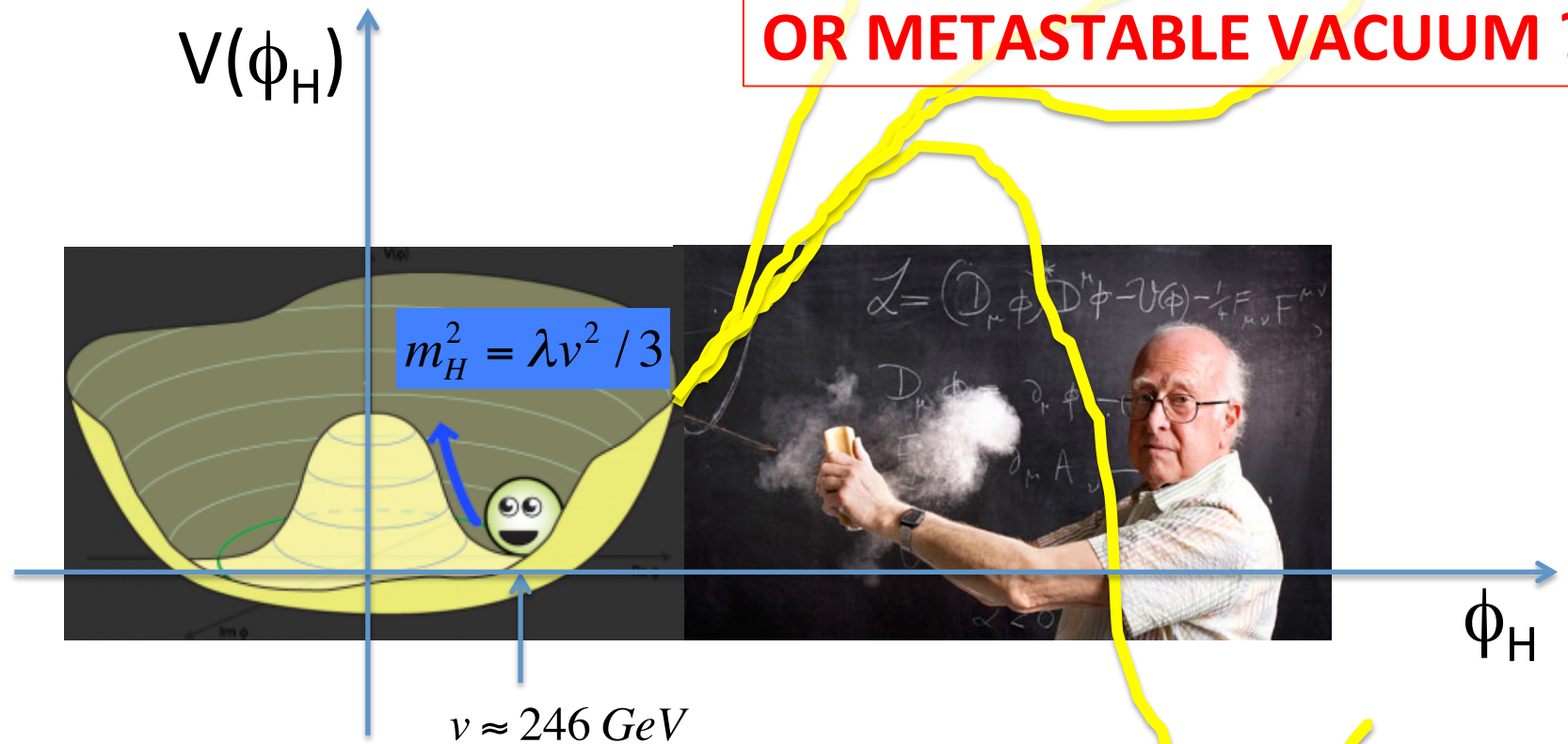
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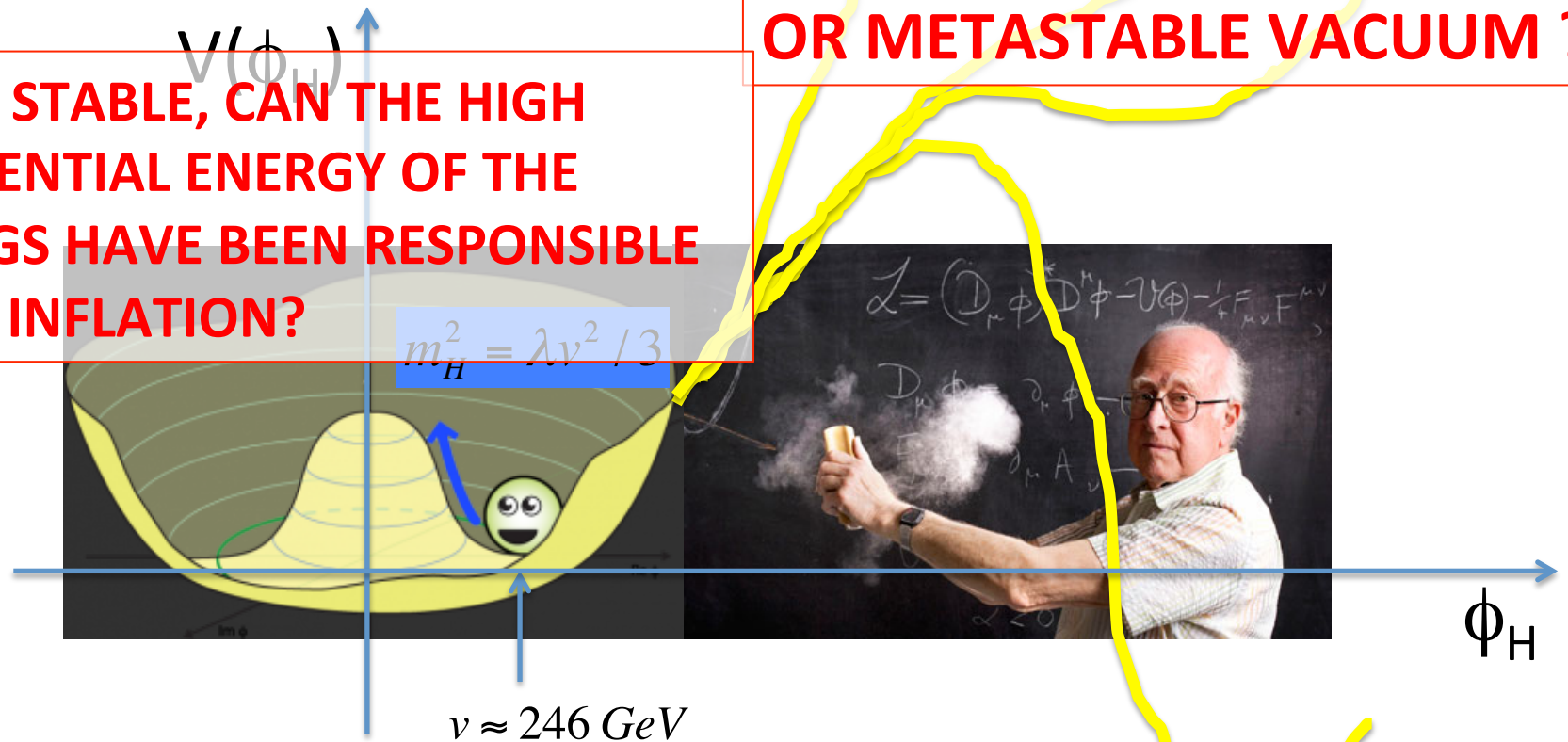


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1) DO WE LIVE IN A STABLE OR METASTABLE VACUUM ?



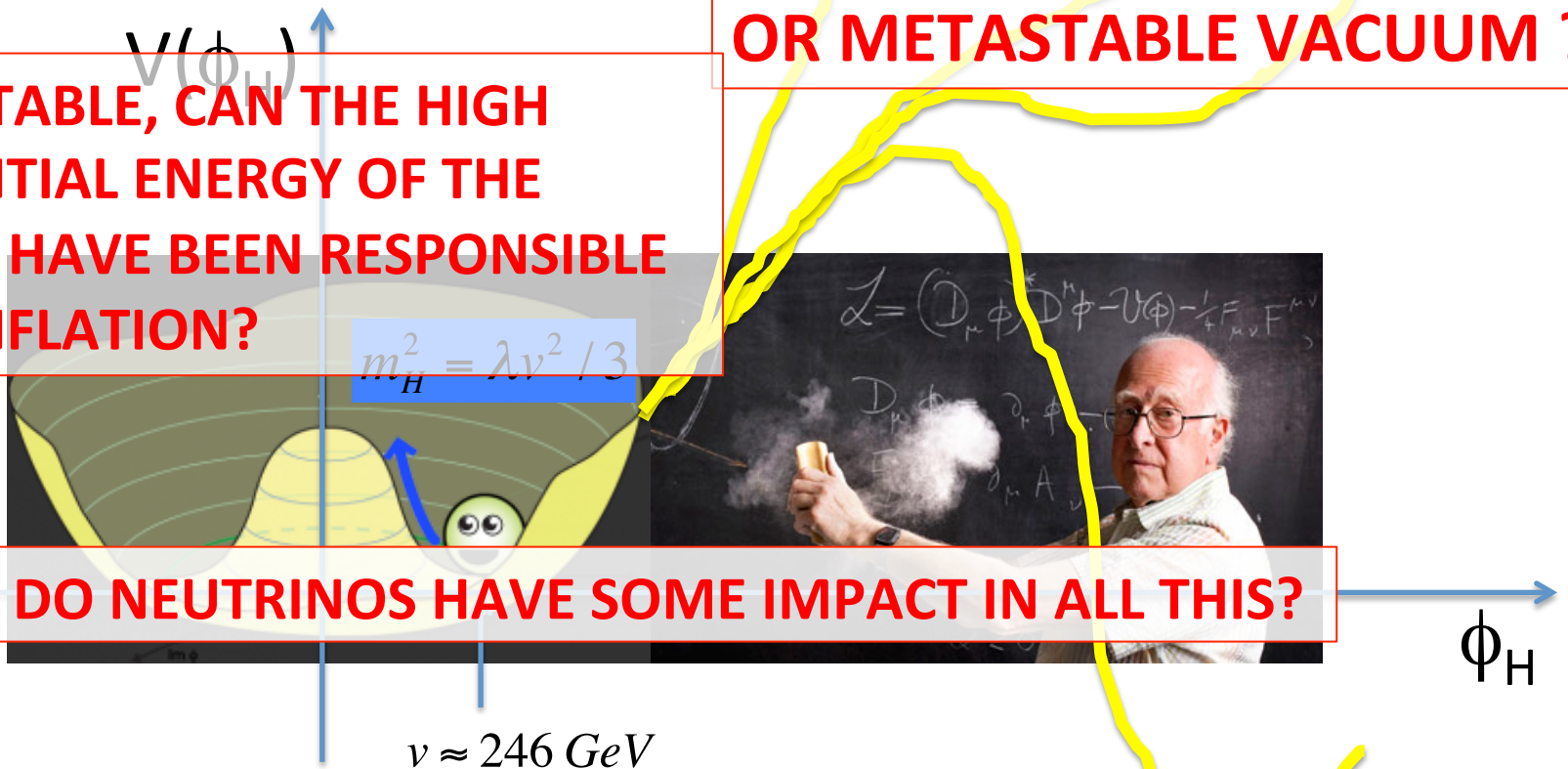
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3) DO NEUTRINOS HAVE SOME IMPACT IN ALL THIS?



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[Hung, Cabibbo et al '79, Lindner, Sher, Casas, Espinosa, Quiros, Giudice, Riotto, Isidori, Strumia, etc]

(Assuming desert) extrapolate the SM Higgs potential at renormalization scale μ via RGE.
This can now be done at NNLO!!

3-loop running for: $g(\mu)$, $g'(\mu)$, $g_3(\mu)$, $\lambda(\mu)$, $y_t(\mu)$

[Mihaila Salomon Steihauser, arXiv:1201.5868]

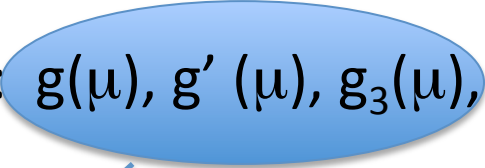
[Chetyrkin Zoller, arXiv:1205.2892]

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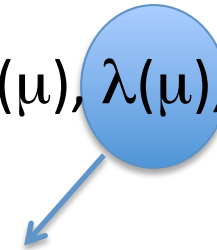
matched directly at m_Z
(larger exp error in α_3)

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matched at 2-loop via m_H (unavoidable theor error)

[Bezrukov Kalmykov Kniehl Shaposhnikov, arXiv:1205.2893]

[Degrassi Di Vita Elias-Miro Espinosa Giudice Isidori Strumia, arXiv:1205.6497]

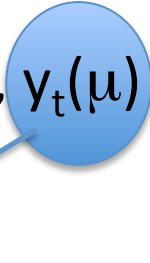
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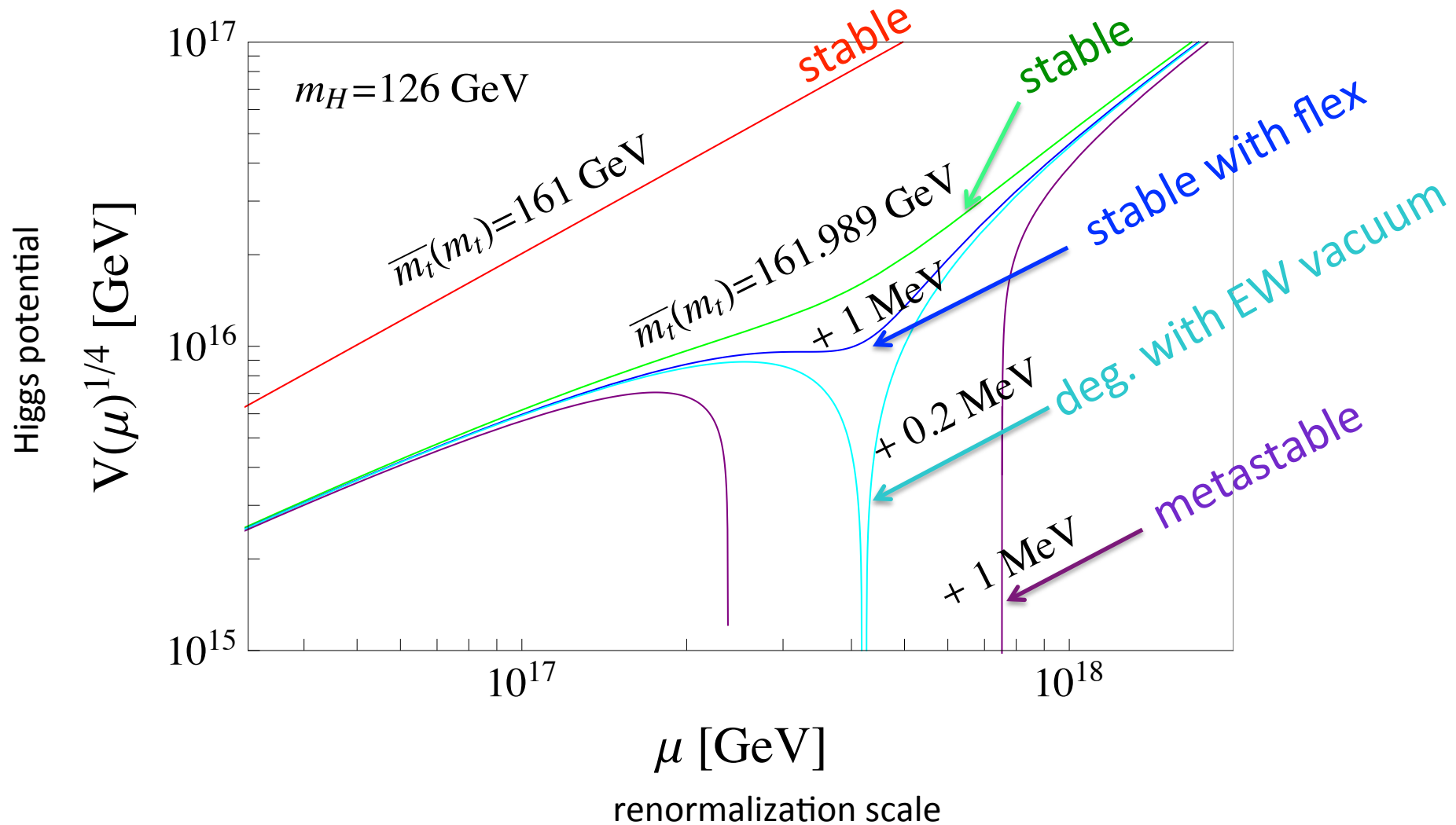
[Alekhin Djouadi Moch, arXiv:1207.0980]

It is inconsistent to use Tevatron measure
BETTER to match directly with $\overline{\text{MS}}$ running m_t

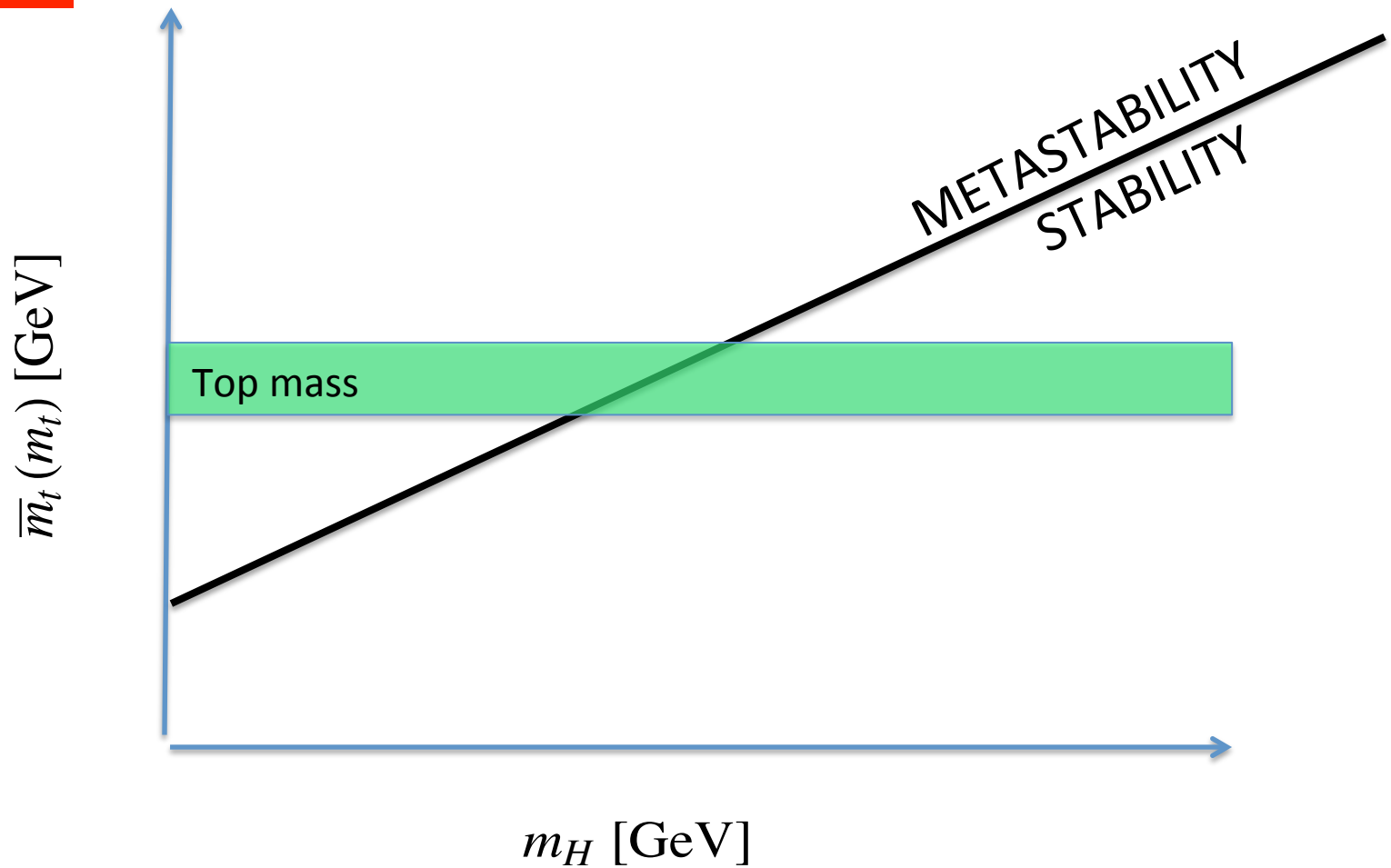
$$\overline{m}_t(m_t) = 163.3 \pm 2.7 \text{ GeV}$$

as done in [IM, arXiv:1209.0393]

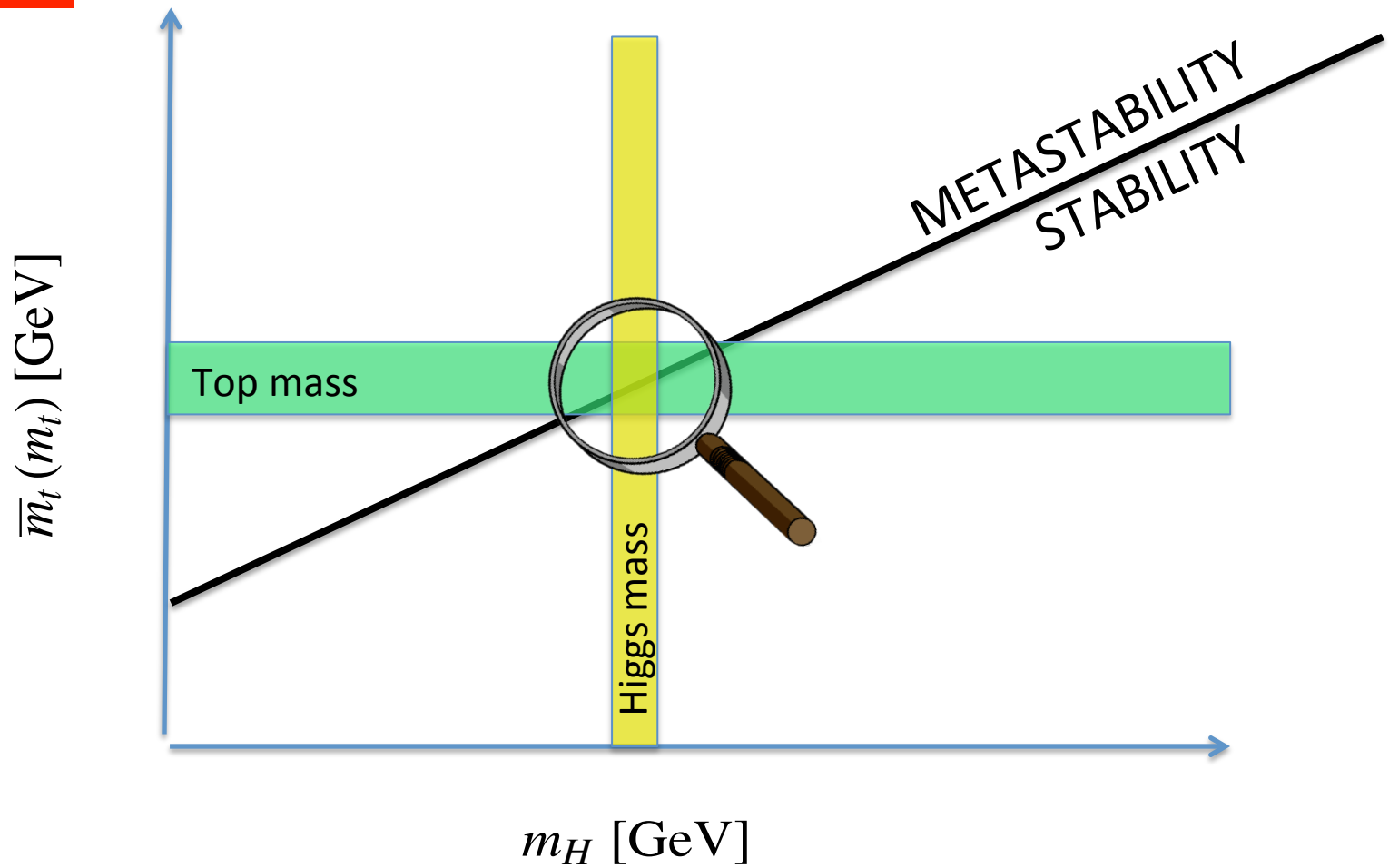
POSSIBLE SHAPES FOR THE HIGGS POTENTIAL CLOSE TO THE PLANCK SCALE

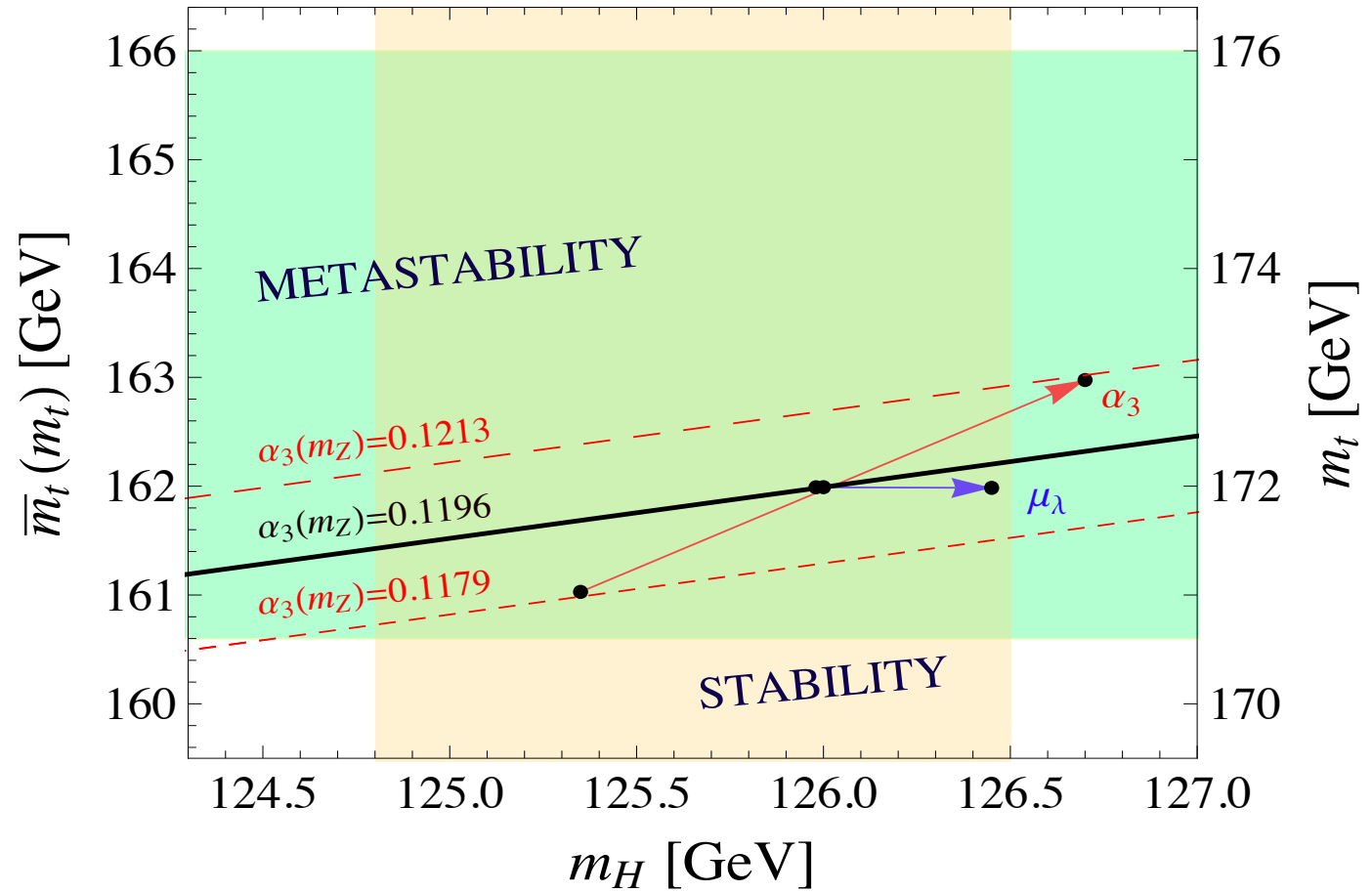


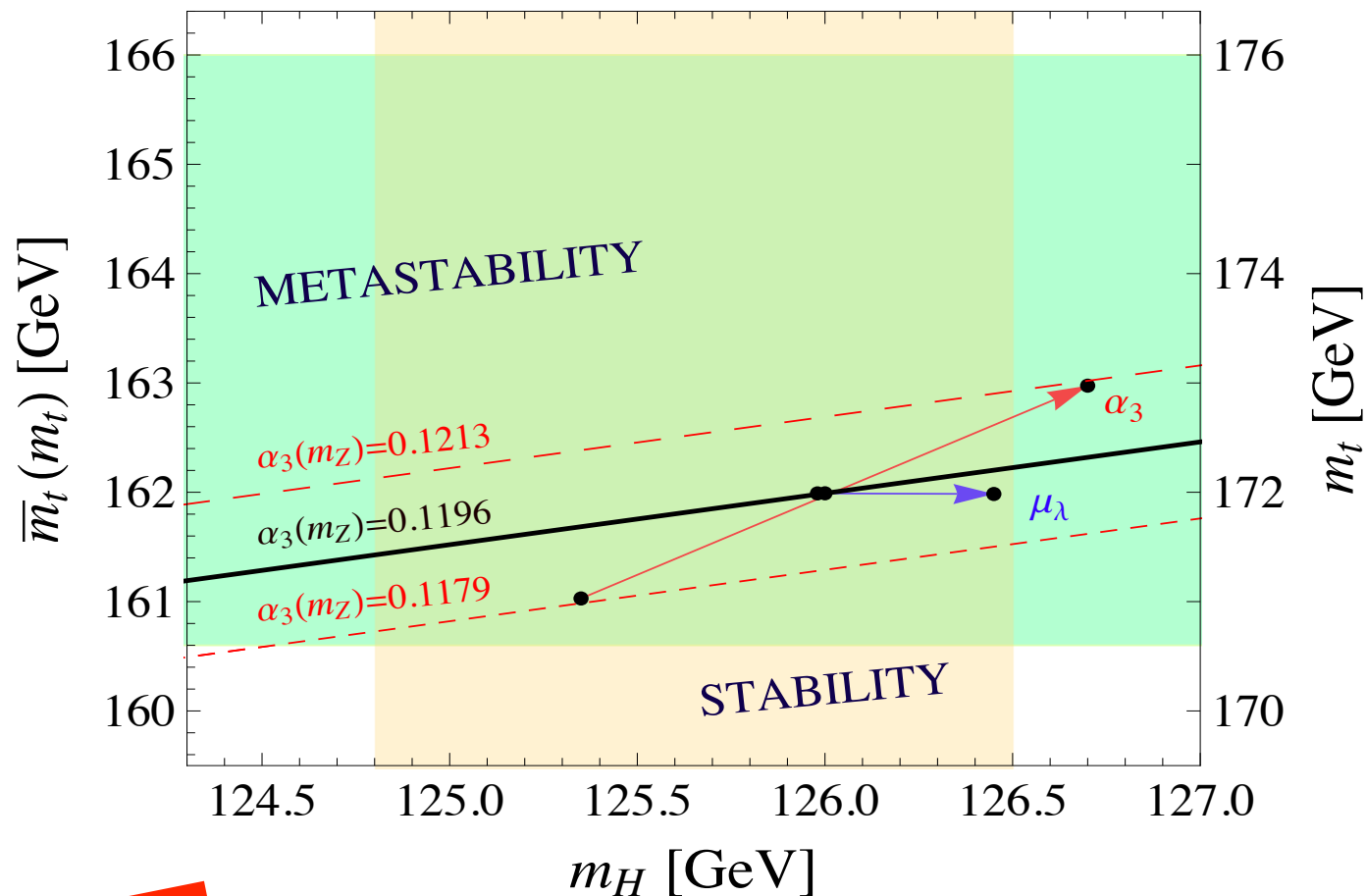
RESULTS



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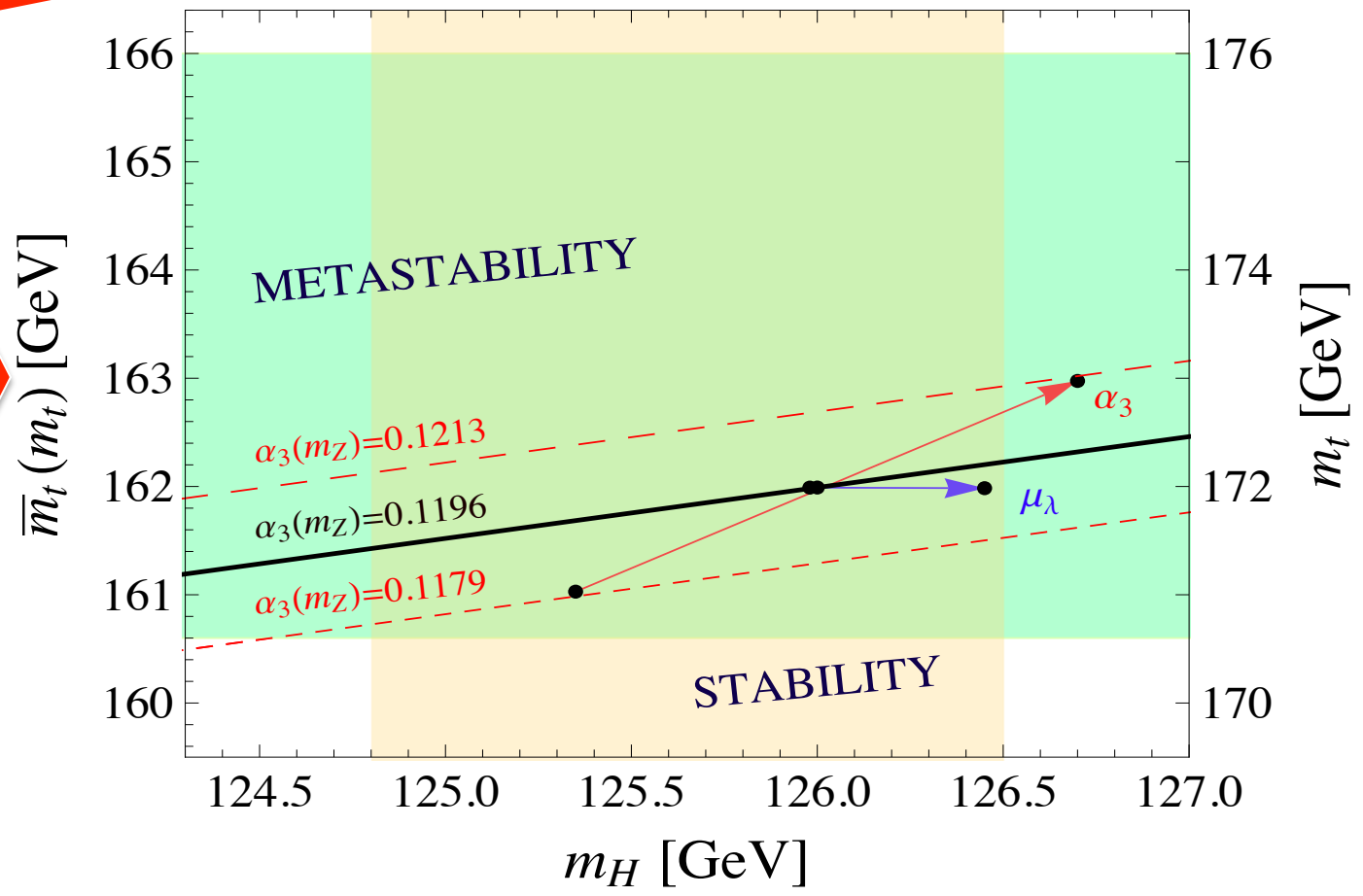


STABILITY BOUND

$$\overline{m}_t(m_t)[\text{GeV}] \leq 162.0 + 0.47 (m_H[\text{GeV}] - 126) \pm 0.7_{\alpha_3} - 0.2_{\mu_\lambda}$$

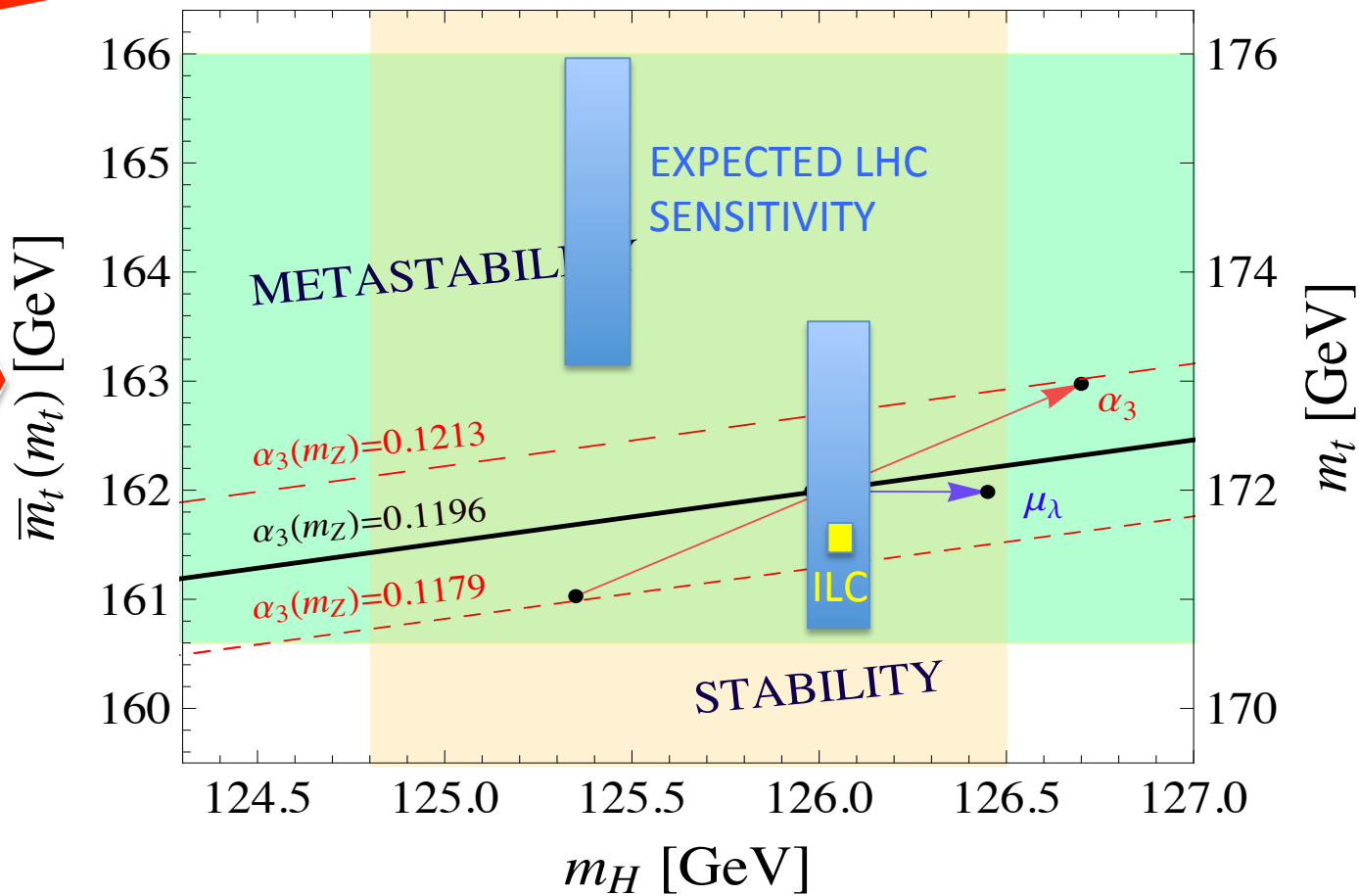
PROSPECTS

NEED MORE
PRECISE
MEASURE



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YES! If, for some reason, there has been a period in which the Hubble rate was dominated by a nearly constant V

$$\left(\frac{\dot{a}(t)}{a(t)}\right)^2 \equiv H(t)^2 \cong \frac{V(\mu_0)}{3M_{Pl}^2}$$

V acts as cosmological constant term

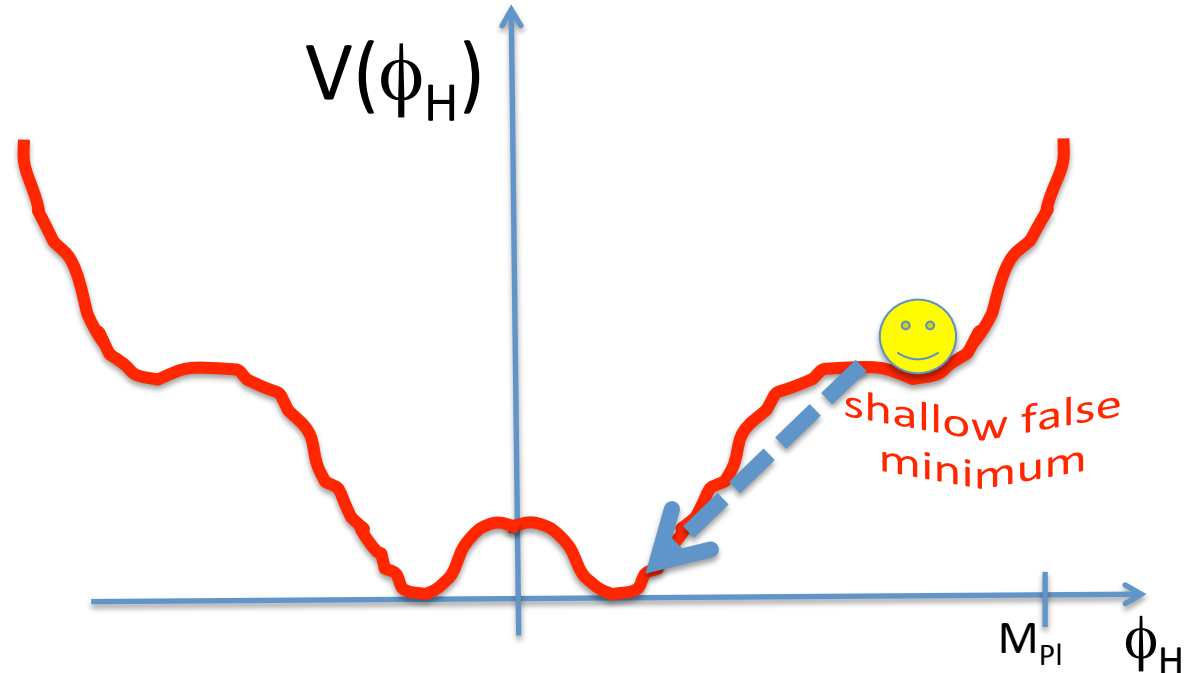


$$a(t) \propto e^{Ht}$$

EXPONENTIAL EXPANSION

EXAMPLE 1

A stable configuration like a shallow false minimum with the Higgs trapped in it during inflation, which ends because of some other mechanism



A model in scalar-tensor gravity & a model with hybrid inflation

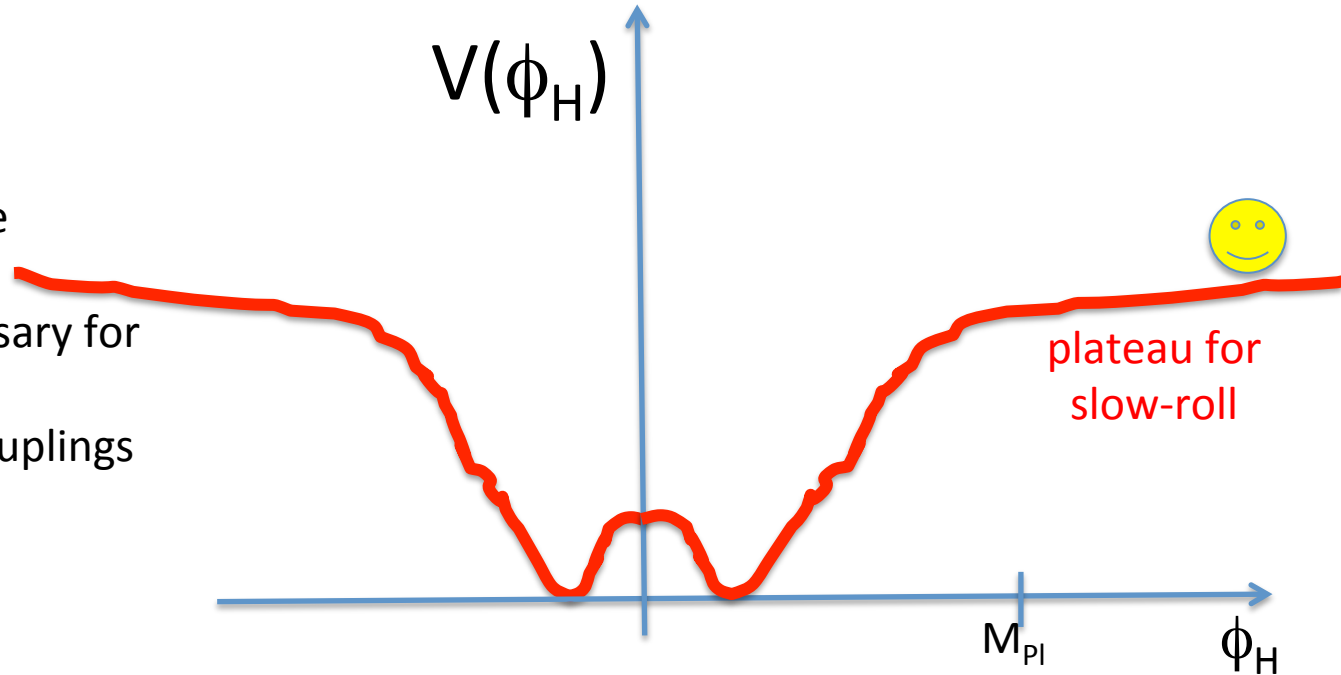
IM Notari, arXiv:1112.2659, 1204.4155

n_s is quite model dependent but tensor-to-scalar-ratio r is not

→ these models can be tested IM Notari, arXiv:1112.5430

EXAMPLE 2

A configuration more
(or as stable as)
an inflection point is necessary for
Higgs inflation via
non-minimal gravitation couplings



Model discussed in

Bezrukov Shaposhnikov, arXiv:0710.3755, ..., 1205.2893

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[Casas Ibarra Quiros, Okada Shafi, Giudice Strumia Riotto, Rodejohann Zhang, etc]

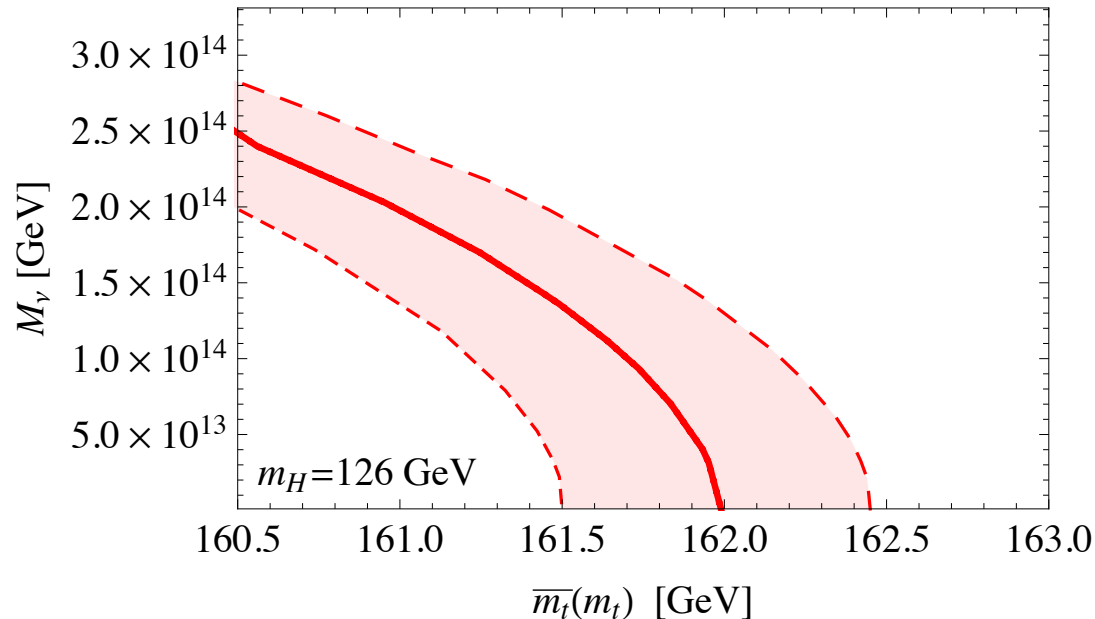
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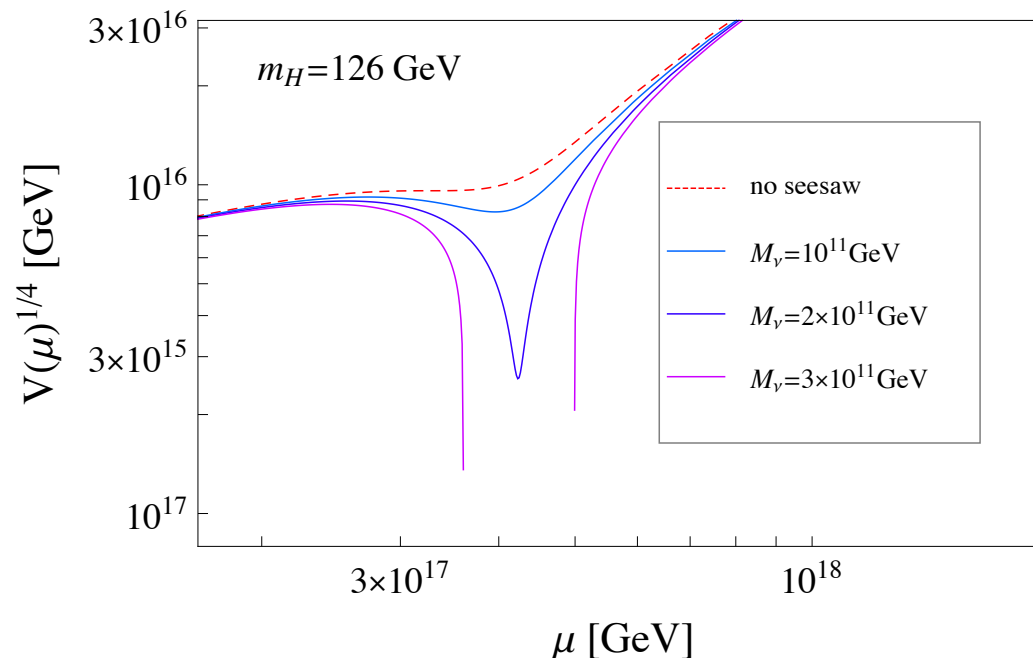
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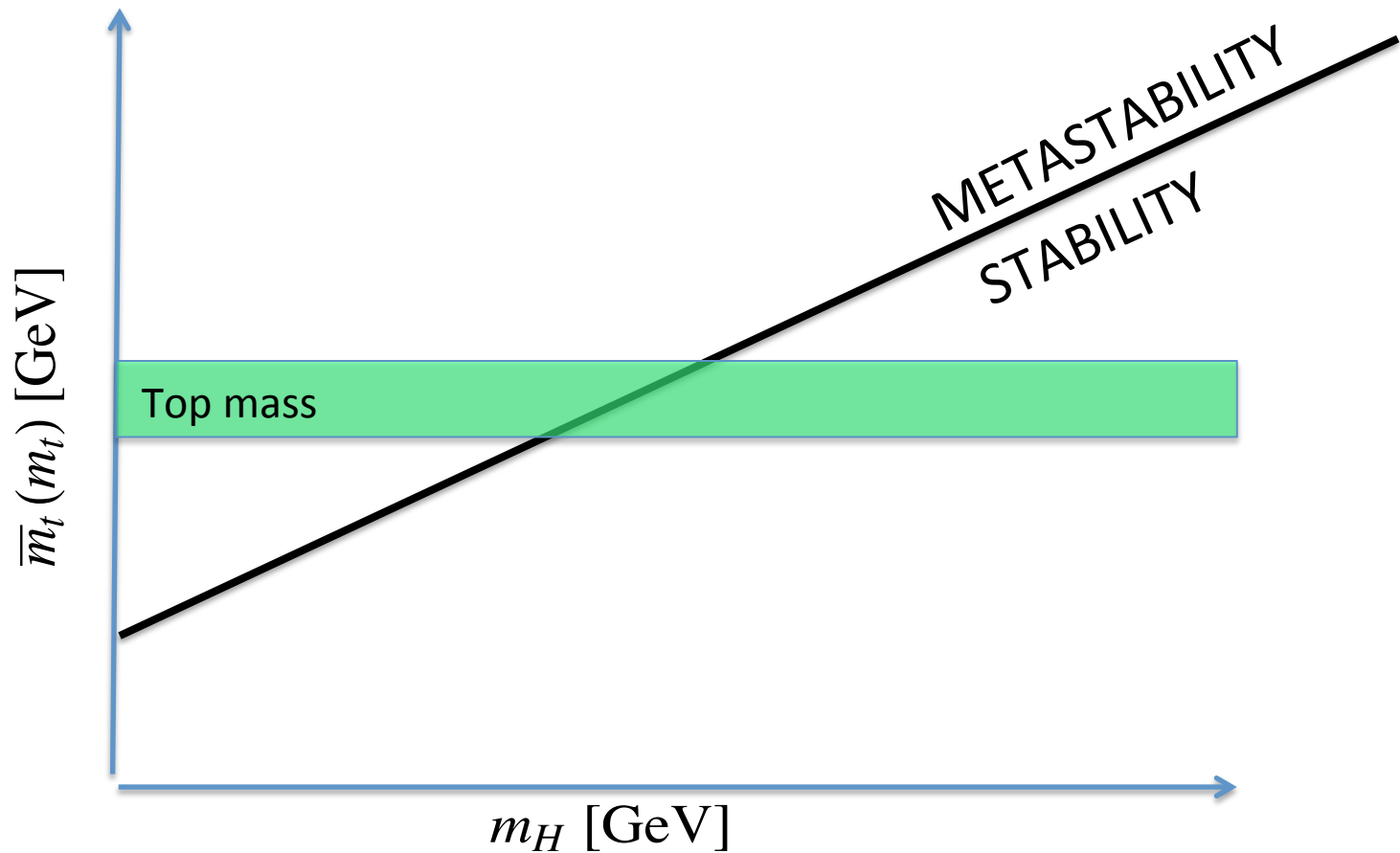
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More stringent if one starts from an inflection point configuration



CONCLUSIONS



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- 1) Intriguing that m_H was found right at the transition between stability and metastability
- 2) Some stable SM configurations very close to transition line (like e.g. shallow false minimum) might have been relevant for primordial inflation

