

*Neutrino mass from cosmological observations:
galaxy-clustering*

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Neutrino Oscillation Workshop
Conca Specchiulla (Otranto, Lecce, Italy) September 9-16, 2012

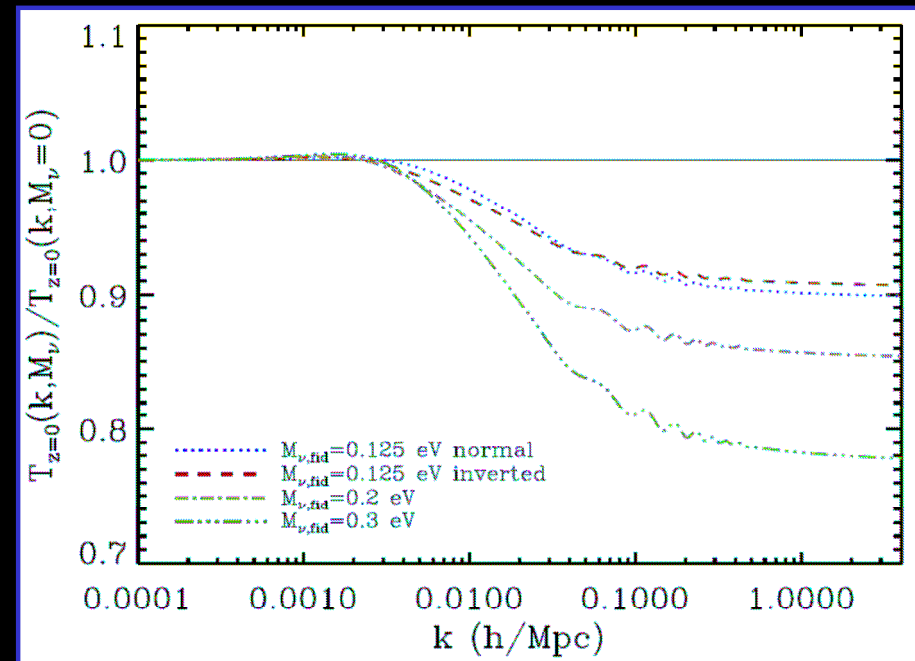
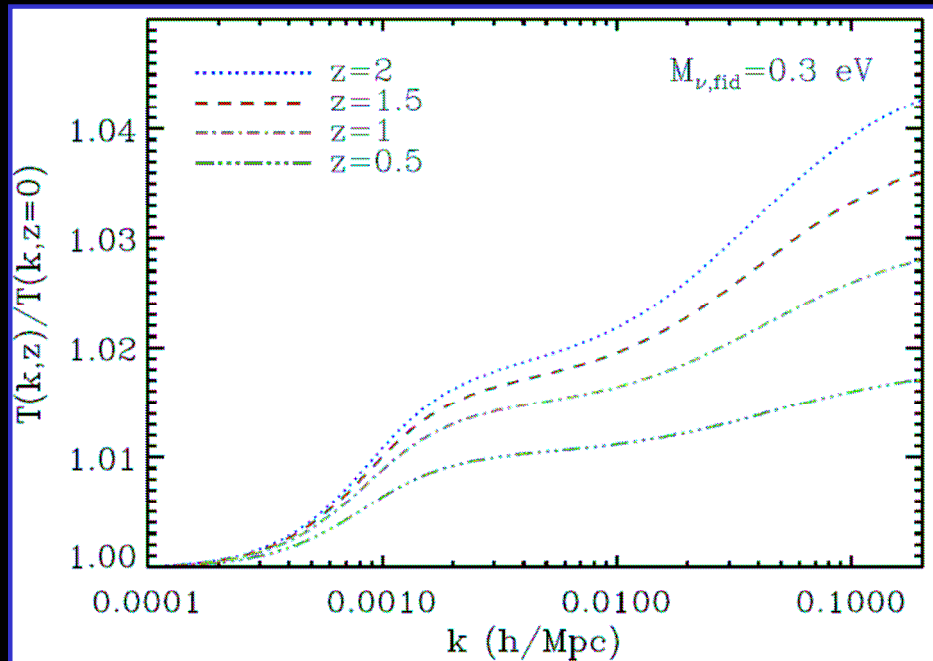
Λ CDM+v: WMAP7+BAO+H₀ $\rightarrow$ M _{ν} <0.58 (1.3 if w $\neq$ -1) eV at 95% C.L.

Probe	Current $\sum m_\nu$ (eV)	Forecast $\sum m_\nu$ (eV)	Key Systematics	Current Surveys	Future Surveys
CMB Primordial	1.3	0.6	Recombination	WMAP, Planck	None
CMB Primordial + Distance	0.58	0.35	Distance measurements	WMAP, Planck	None
Lensing of CMB	∞	0.2 – 0.05	NG of Secondary anisotropies	Planck, ACT [39], SPT [96]	EBEX [57], ACTPol, SPTPol, POLAR-BEAR [5], CMBPol [6]
Galaxy Distribution	0.6	0.1	Nonlinearities, Bias	SDSS [58, 59], BOSS [82]	DES [84], BigBOSS [81], DESpec [85], LSST [92], Subaru PFS [97], HETDEX [35] Euclid
Lensing of Galaxies	0.6	0.07	Baryons, NL, Photometric redshifts	CFHT-LS [23], COSMOS [50]	DES [84], Hyper SuprimeCam, LSST [92], Euclid [88], WFIRST[100]
Lyman α	0.9	0.1	Bias, Metals, QSO continuum	SDSS, BOSS, Keck	BigBOSS[81], TMT[99], GMT[89]
21 cm	∞	0.1 – 0.006	Foregrounds, Astrophysical modeling	GBT [11], LOFAR [91], PAPER [53], GMRT [86]	MWA [93], SKA [95], FFTT [49]
Galaxy Clusters	0.3	0.1	Mass Function, Mass Calibration	SDSS, SPT, ACT, XMM [101] Chandra [83]	DES, eRosita [87], LSST Euclid

Abazajian et al. 2011

Each of these probes faces technological, observational, and theoretical challenges

Massive neutrino effects on the matter transfer function (Only 3 active neutrinos)

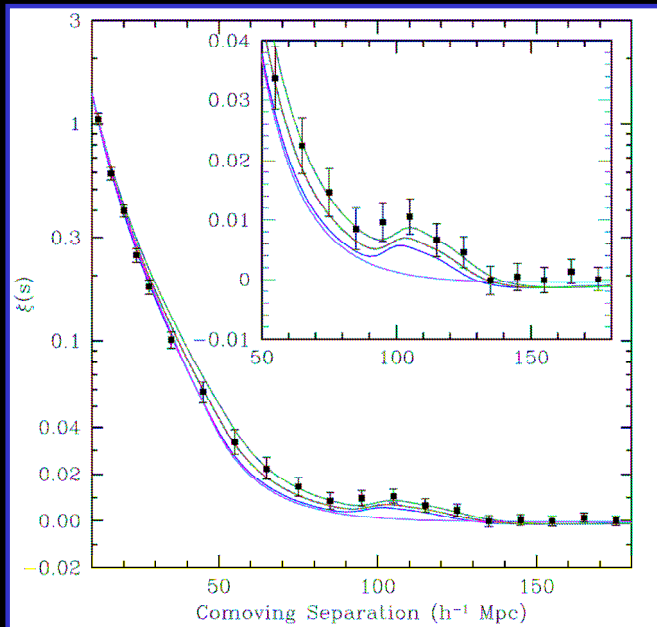


CC et al. 2011

$$\Phi(\vec{k}, a) = \Phi_p(\vec{k}) \times \left\{ \text{Transfer Function}(k) \right\} \times \left\{ \text{Growth Function}(a) \right\}$$

$$P_{\text{matter}}(k, z) = \frac{8\pi^2 c^4 k_0 \Delta_{\mathcal{R}}^2(k_0)}{25 H_0^4 \Omega_m^2} T^2(k, z) \left[\frac{G(z)}{G(z=0)} \right]^2 \left(\frac{k}{k_0} \right)^{n_s} e^{-k^2 \mu^2 \sigma_r^2}$$

Baryon Acoustic Oscillations (BAO)

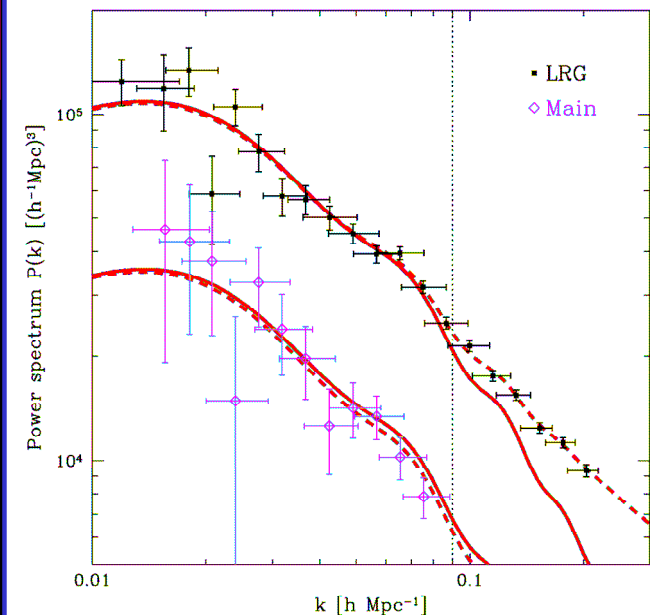


The large-scale redshift-space correlation function of the SDSS-LRG sample. The models are $\Omega_m h^2 = 0.12$ (top, green), 0.13 (red), and 0.14 (bottom with peak, blue), all with $\Omega_b h^2 = 0.024$ and $n_s = 0.98$. The magenta line shows a pure CDM model ($\Omega_m h^2 = 0.105$), which lacks the acoustic peak.

$$r_{\parallel} = \frac{c \Delta z}{H(z)}$$

$$r_{\perp} = (1 + z) D_A(z) \Delta \theta$$

Measured power spectra for the full SDSS-LRG and SDSS main galaxy samples. The solid curves correspond to the linear theory Λ CDM fits to WMAP3 alone, normalized to galaxy bias $b=1.9$ (top) and $b=1.1$ (bottom) relative to the $z=0$ matter power. The dashed curves include nonlinear corrections with $k > 0.09$



Forecast errors for Euclid: Fisher matrix for BAO+P(k)-shape

$$P_{\text{obs}}(k_{\text{ref}\perp}, k_{\text{ref}\parallel}, z) = \frac{D_A(z)_{\text{ref}}^2 H(z)}{D_A(z)^2 H(z)_{\text{ref}}} P_g(k_{\text{ref}\perp}, k_{\text{ref}\parallel}, z) + P_{\text{shot}}$$

$$P_g(k_{\text{ref}\perp}, k_{\text{ref}\parallel}, z) = b(z)^2 \left[1 + \beta(z, k) \frac{k_{\text{ref}\parallel}^2}{k_{\text{ref}\perp}^2 + k_{\text{ref}\parallel}^2} \right]^2 \times P_{\text{matter}}(k, z)$$

$$\begin{aligned} F_{ij}^{\text{LSS}} &= \int_{\vec{k}_{\min}}^{\vec{k}_{\max}} \frac{\partial \ln P_{\text{obs}}(\vec{k})}{\partial p_i} \frac{\partial \ln P_{\text{obs}}(\vec{k})}{\partial p_j} V_{\text{eff}}(\vec{k}) \frac{d\vec{k}}{2(2\pi)^3} \\ &= \int_{-1}^1 \int_{k_{\min}}^{k_{\max}} \frac{\partial \ln P_{\text{obs}}(k, \mu)}{\partial p_i} \frac{\partial \ln P_{\text{obs}}(k, \mu)}{\partial p_j} V_{\text{eff}}(k, \mu) \frac{2\pi k^2 dk d\mu}{2(2\pi)^3} \end{aligned}$$

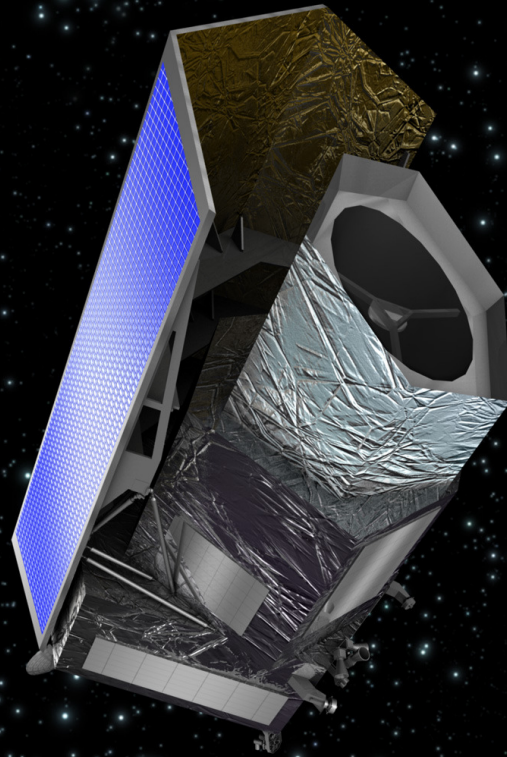
$$\left[\frac{\Delta P_g}{P_g} \right]^2 = \frac{2(2\pi)^2}{V_{\text{survey}} k^2 \Delta k \Delta \mu} \left[1 + \frac{1}{n_g P_g} \right]^2$$

$$V_{\text{eff}}(k, \mu) = \left[\frac{n_g P_g(k, \mu)}{n_g P_g(k, \mu) + 1} \right]^2 V_{\text{survey}}$$

$$F_{ij} = \frac{1}{2} \text{Tr} \left[\mathbf{C}^{-1} \frac{\partial \mathbf{C}}{\partial \theta_i} \mathbf{C}^{-1} \frac{\partial \mathbf{C}}{\partial \theta_j} \right] + \frac{\partial \mu^t}{\partial \theta_i} \mathbf{C}^{-1} \frac{\partial \mu}{\partial \theta_j}$$

$$\mathbf{M}_v + \{ \Omega_m, \Omega_{de}, h, \Delta_{\mathcal{R}}^2(k_0), \Omega_b, w_0, w_a, n_s \}$$

Euclid: Mapping the geometry of the dark Universe



Euclid is an ESA M-class mission selected for launch in 2019 in the Cosmic Vision 2015-2025 programme. The main goal of Euclid is to understand the origin of the accelerating expansion of the Universe. To achieve this goal, it is proposed to build a satellite equipped with a 1.2 m telescope and three imaging and spectroscopic instruments working in the visible and near-infrared wavelength domains. These instruments will explore the expansion history of the Universe and the evolution of cosmic structures by measuring shapes and red-shifts of galaxies as well as the distribution of galaxy-clusters as function of redshift $0.5 < z < 2$, over 15000 deg^2 of the sky. The satellite will be launched by a Soyuz ST-2.1B rocket and transferred to the L2 Lagrange point for a 6 years mission.

Neutrino constraints from the Euclid galaxy survey at 1- σ

Table 1: Parameter 1- σ errors for slitless spectroscopy

slitless+BOSS						
fiducial $\rightarrow$	$M_\nu=0.3$ eV ^a	$M_\nu=0.2$ eV ^a	$M_\nu=0.125$ eV ^b	$M_\nu=0.125$ eV ^c	$M_\nu=0.05$ eV ^b	$N_{\text{eff}}=3.04^d$
Ω_m	0.0140	0.0137	0.0139	0.0138	0.0137	0.0124
Ω_{de}	0.0260	0.0265	0.0258	0.0257	0.0253	0.0256
Ω_b	0.0032	0.0031	0.0032	0.0032	0.0032	0.0034
h	0.0116	0.0112	0.0113	0.0114	0.0113	0.0137
M_ν	0.1459	0.1461	0.1795	0.1435	0.1428	--
N_{eff}	--	--	--	--	--	0.5435
ns	0.0233	0.0225	0.0314	0.0228	0.0220	0.0326
w_0	0.0815	0.0837	0.0812	0.0808	0.0801	0.0807
w_a	0.3461	0.3573	0.3450	0.3440	0.3386	0.3324
FoM	51.75	48.44	52.44	52.68	54.25	55.23
slitless+BOSS+Planck						
Ω_m	0.0034	0.0035	0.0033	0.0035	0.0035	0.0031
Ω_{de}	0.0064	0.0064	0.0062	0.0064	0.0065	0.0064
Ω_b	0.0006	0.0056	0.0006	0.0005	0.0005	0.0005
h	0.0043	0.0043	0.0043	0.0043	0.0042	0.0046
M_ν	0.0347	0.0433	0.0311	0.0441	0.0526	--
N_{eff}	--	--	--	--	--	0.0865
ns	0.0022	0.0022	0.0022	0.0022	0.0022	0.0041
w_0	0.0732	0.0721	0.0716	0.0715	0.0709	0.0705
w_a	0.1760	0.1742	0.1713	0.1725	0.1722	0.1664
$\Delta_{\mathcal{R}}^2(k_0)$	0.0250	0.0226	0.0226	0.0227	0.0244	0.0227
FoM	245.07	242.80	259.32	247.96	240.31	294.15

^afor degenerate spectrum: $m_1 \approx m_2 \approx m_3$; ^bfor normal hierarchy: $m_3 \neq 0$, $m_1 \approx m_2 \approx 0$

^cfor inverted hierarchy: $m_1 \approx m_2$, $m_3 \approx 0$; ^dfiducial cosmology with massless neutrinos

Only 3 active
neutrinos for
 M_ν errors

CC et al. 2011

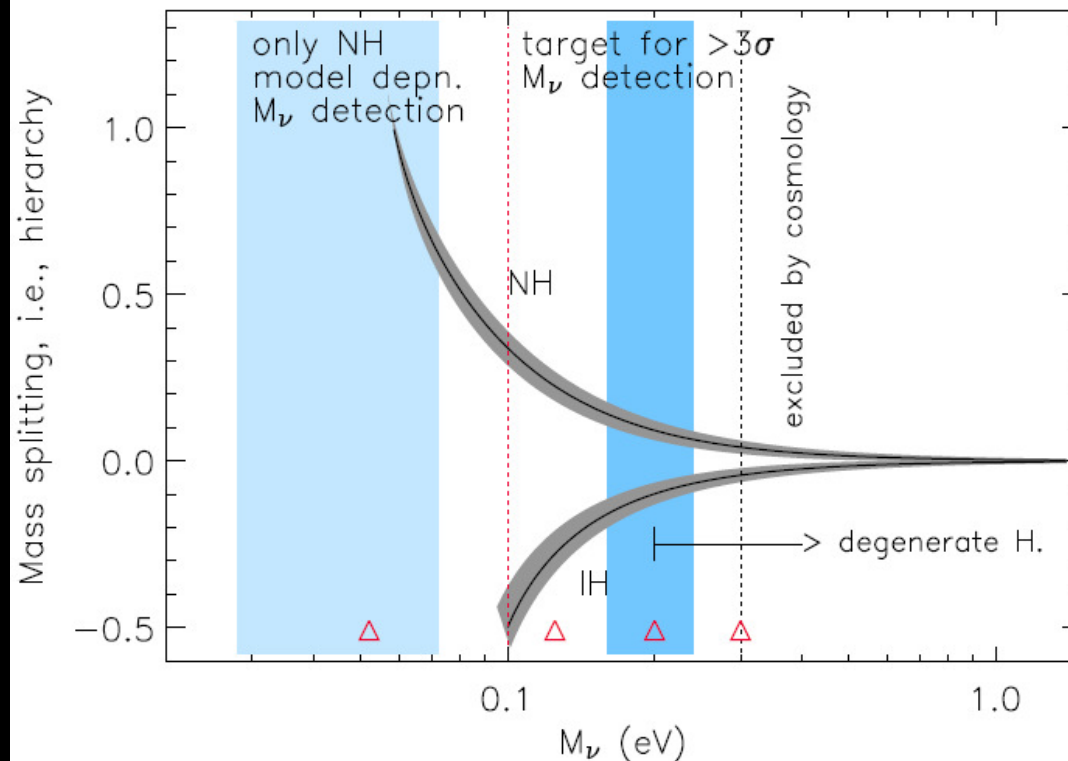


Table 5: $\sigma(M_\nu)$ and $\sigma(N_{\text{eff}})$ marginalised errors from LSS+CMB

General cosmology						
fiducial→	$M_\nu=0.3 \text{ eV}^a$	$M_\nu=0.2 \text{ eV}^a$	$M_\nu=0.125 \text{ eV}^b$	$M_\nu=0.125 \text{ eV}^b$	$M_\nu=0.05 \text{ eV}^b$	$N_{\text{eff}}=3.04^d$
slitless+BOSS+Planck	0.035	0.043	0.031	0.044	0.053	0.086
Λ CDM cosmology						
slitless+BOSS+Planck	0.017	0.019	0.017	0.021	0.021	0.023

20%

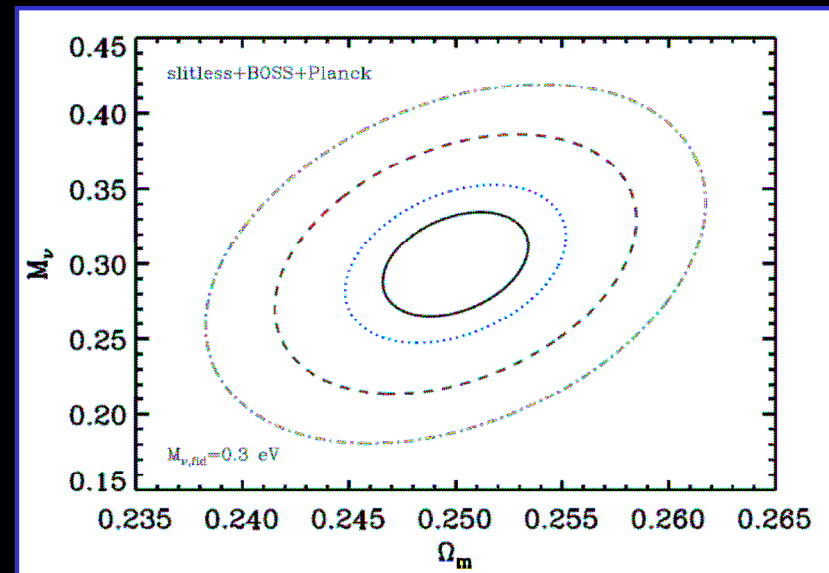
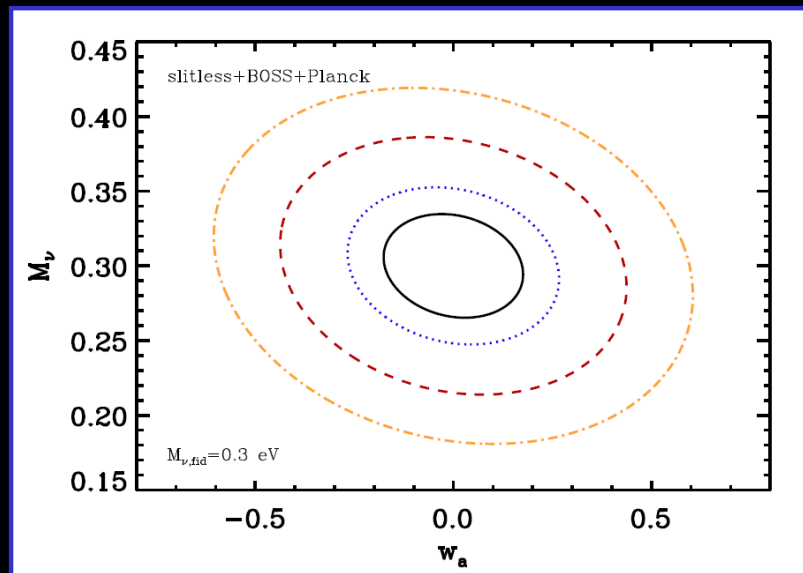
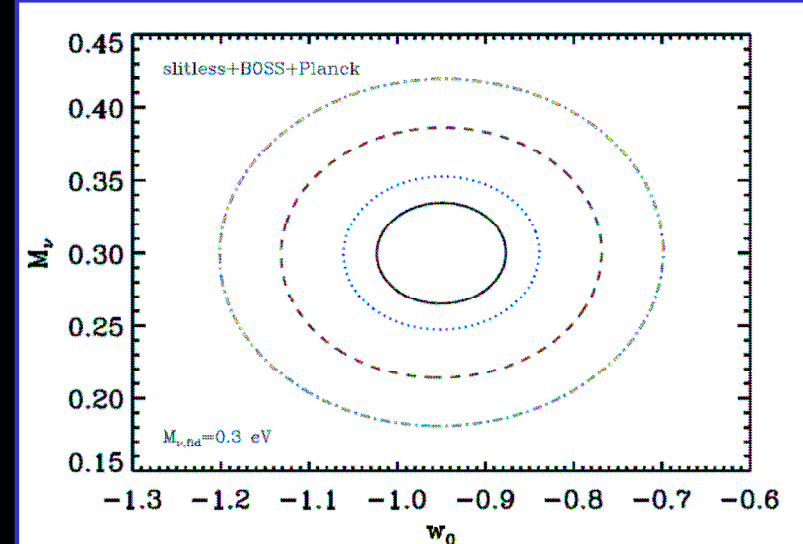
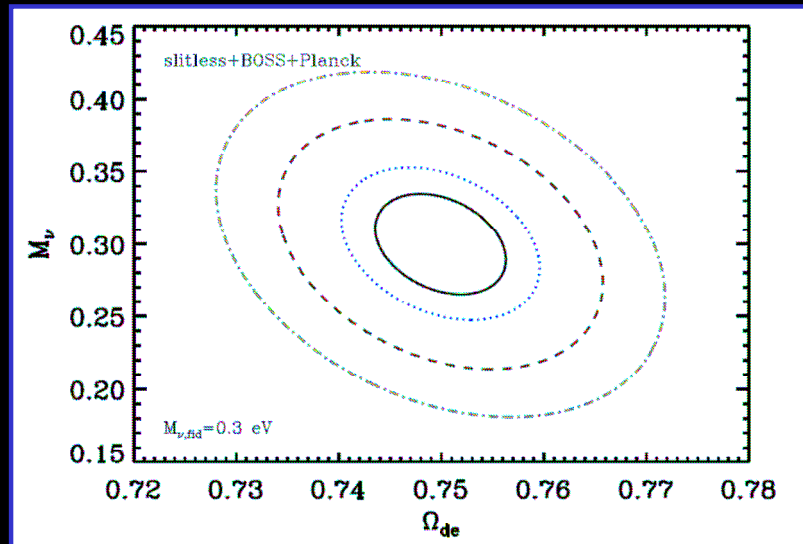
^afor degenerate spectrum: $m_1 \approx m_2 \approx m_3$; ^bfor normal hierarchy: $m_3 \neq 0$, $m_1 \approx m_2 \approx 0$

^cfor inverted hierarchy: $m_1 \approx m_2$, $m_3 \approx 0$; ^dfiducial cosmology with massless neutrinos

Only 3 active neutrinos for M_ν errors

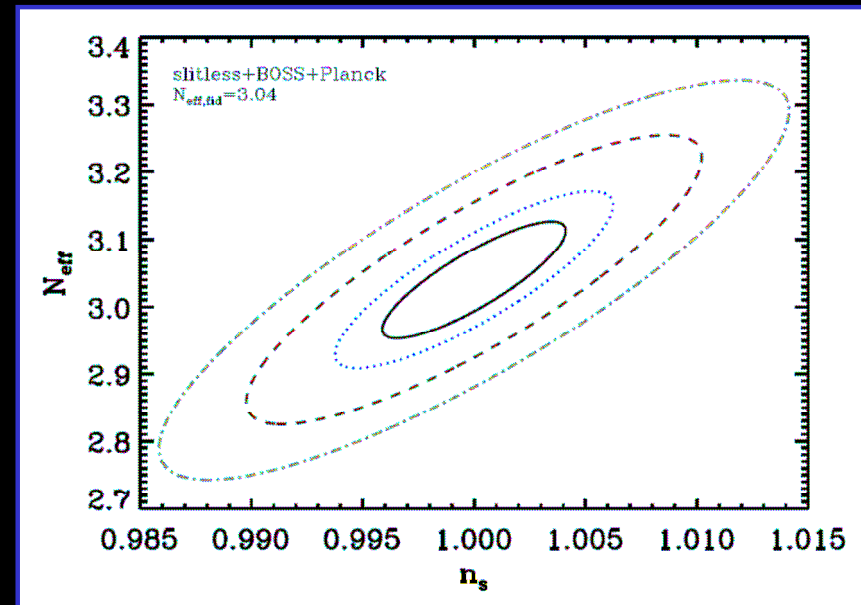
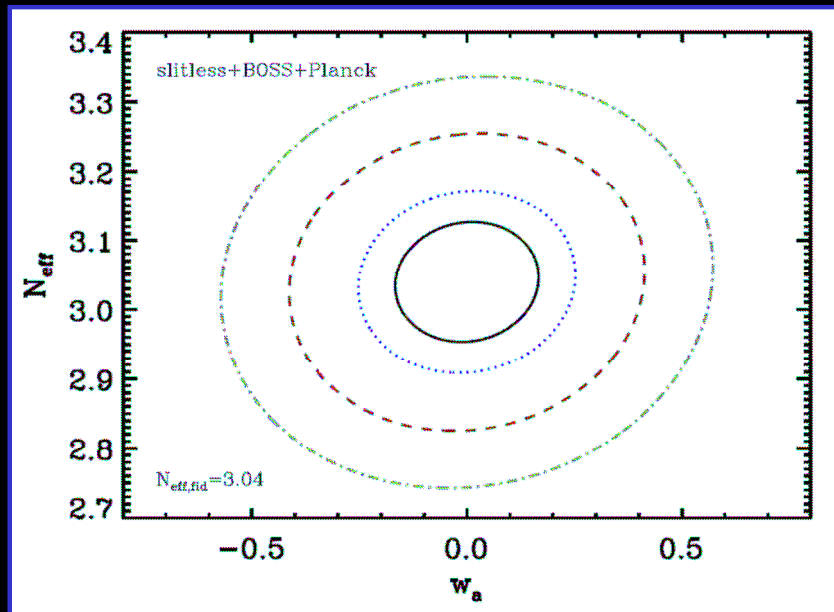
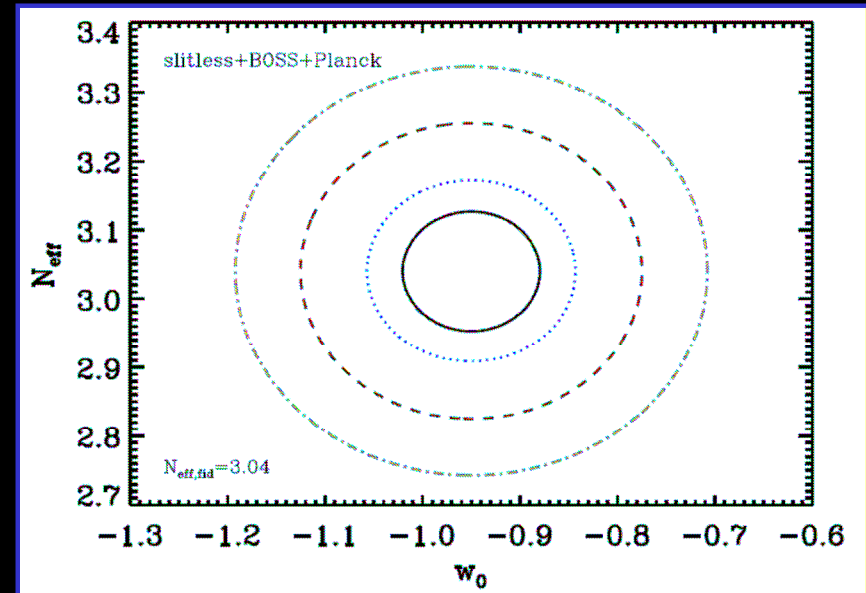
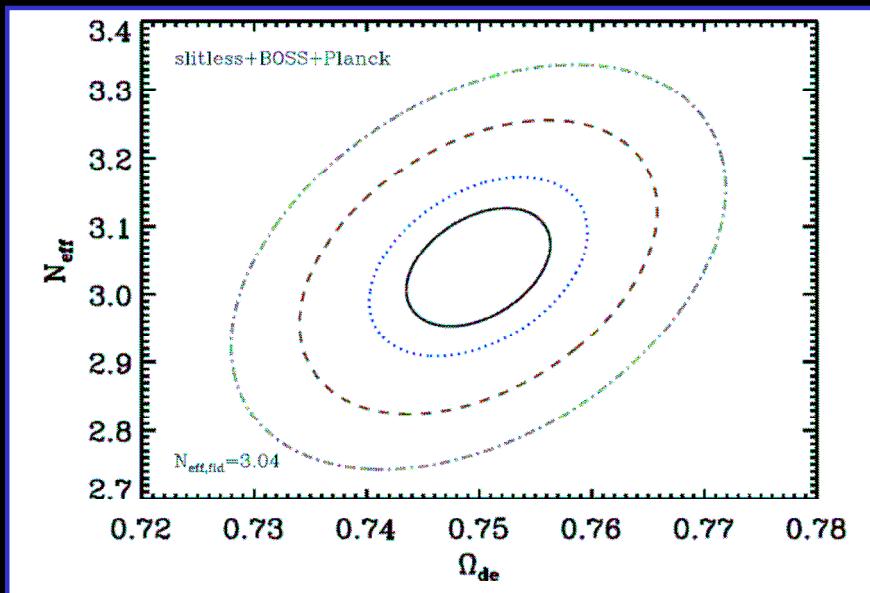
CC et al. 2011

Marginalised 1- σ errors for M_ν from Euclid+Planck (CC et al. 2011)

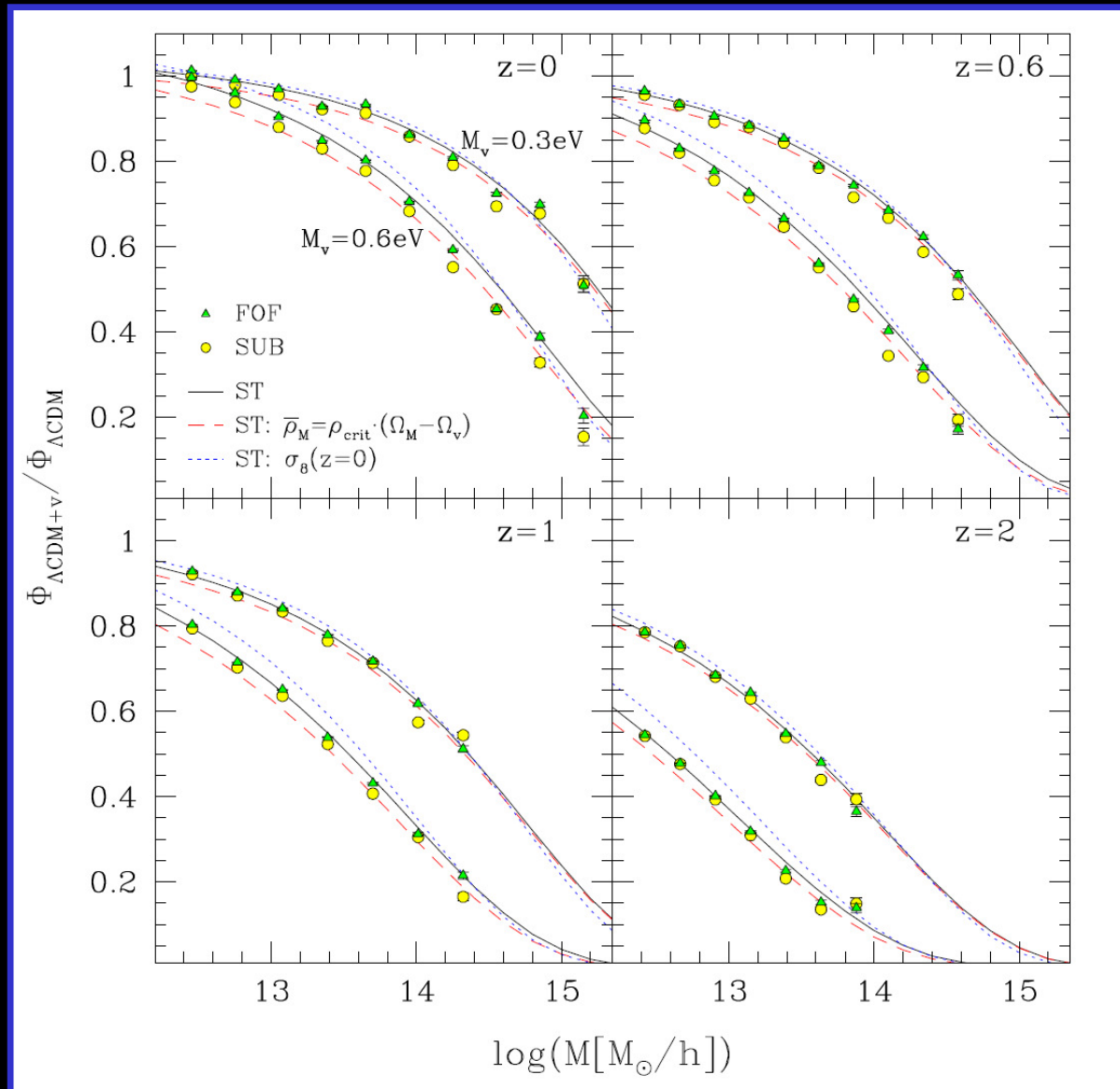


CC et al. 2011

Marginalised 1- σ errors for N_{eff} from Euclid+Planck (CC et al. 2011)



Effects of massive neutrinos on the the halo mass function



Only 3 active
neutrinos

Marulli, CC et al. 2011

General cosmology				
	BAO+COUNTS ^a +CMB		BAO+COUNTS ^b +CMB	
	σ	r	σ	r
Ω_m	0.0106	0.4046	0.0057	0.6860
Ω_K	0.0039	0.3854	0.0031	0.6551
Ω_b	0.0016	0.0125	0.0008	0.3456
h	0.0125	-0.0380	0.0061	-0.3841
M_ν	0.1853	1.0000	0.1064	1.0000
n_s	0.0024	-0.0297	0.0023	0.0722
w_0	0.2133	0.0020	0.1477	0.7178
w_a	0.7218	-0.2123	0.5119	-0.7616
$\log(10^{10} A_s)$	0.0222	0.8878	0.0175	0.8599

Λ CDM				
	BAO+COUNTS ^a +CMB		BAO+COUNTS ^b +CMB	
	σ	r	σ	r
Ω_m	0.0036	-0.8361	0.0008	0.1401
Ω_b	0.0009	-0.7042	0.0003	0.5604
h	0.0068	0.7796	0.0021	-0.3582
M_ν	0.0758	1.0000	0.0339	1.0000
n_s	0.0023	0.2220	0.0023	0.5414
$\log(10^{10} A_s)$	0.0138	0.7522	0.0103	0.9441

Nuisance parameters kept fixed to the fiducial values

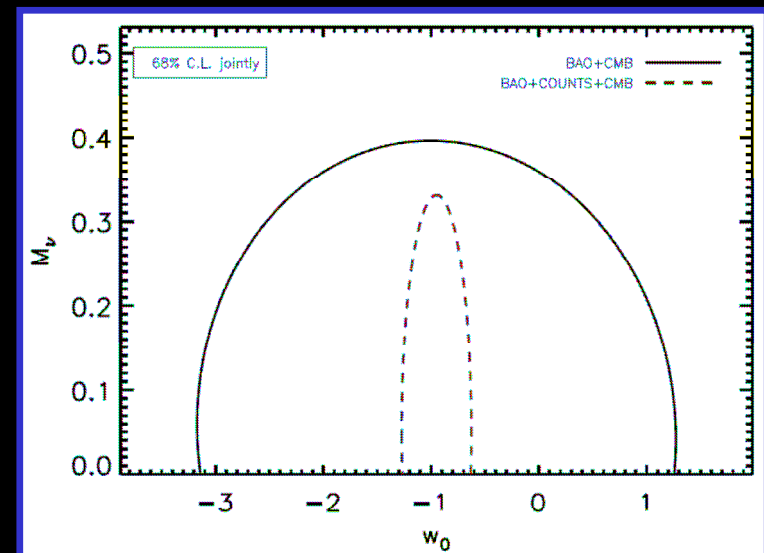
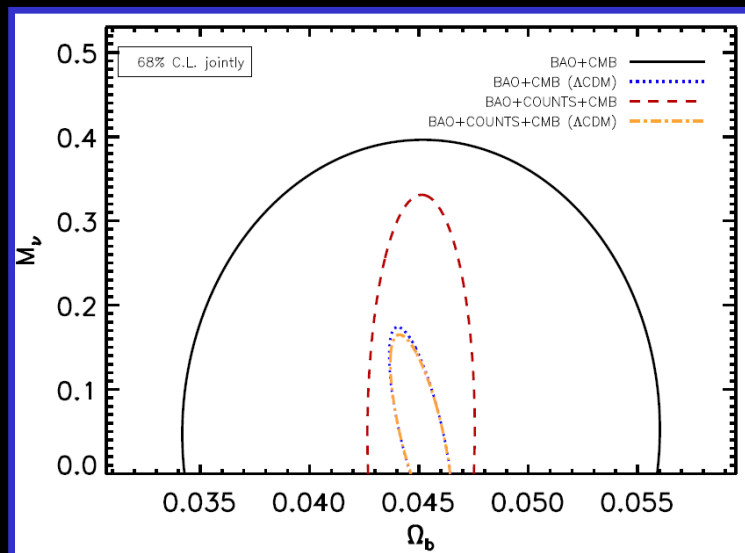
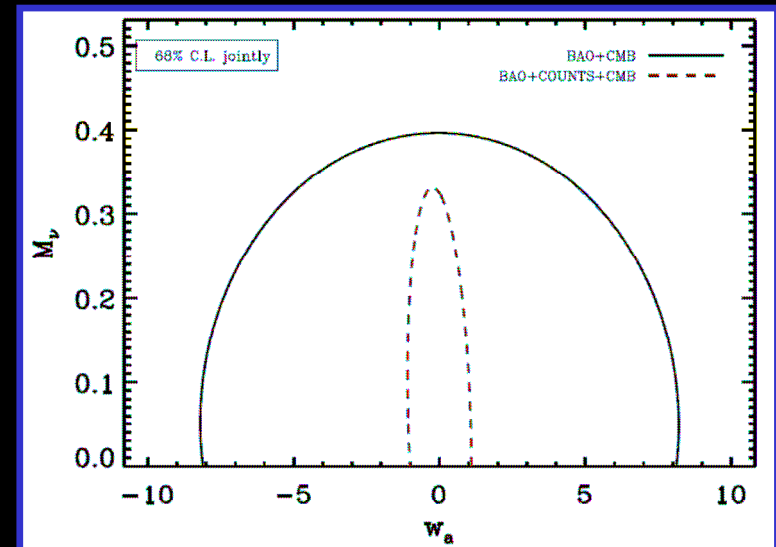
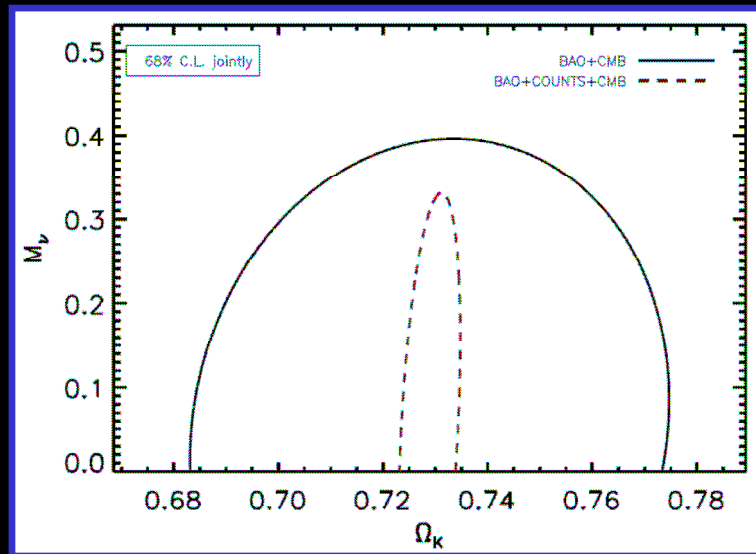
Only 3 active neutrinos for M_ν errors

$$r \equiv \frac{(F^{-1})_{\alpha\beta}}{\sqrt{(F^{-1})_{\alpha\alpha}(F^{-1})_{\beta\beta}}}$$

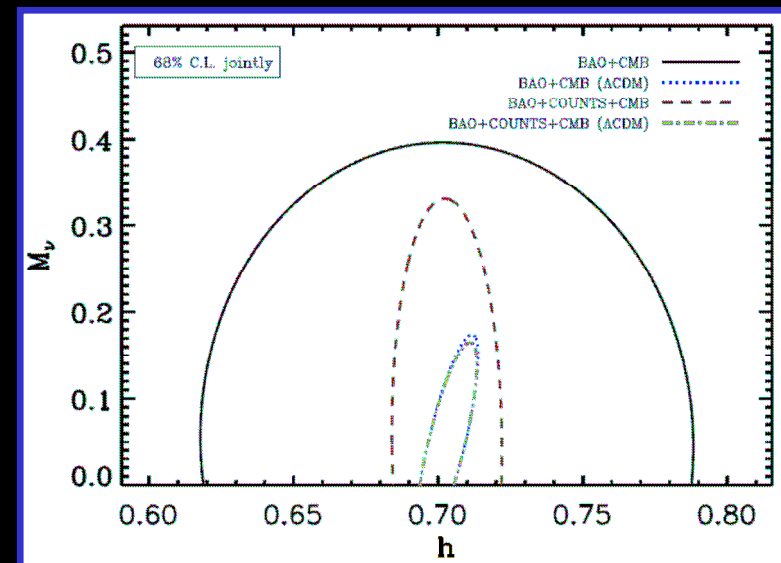
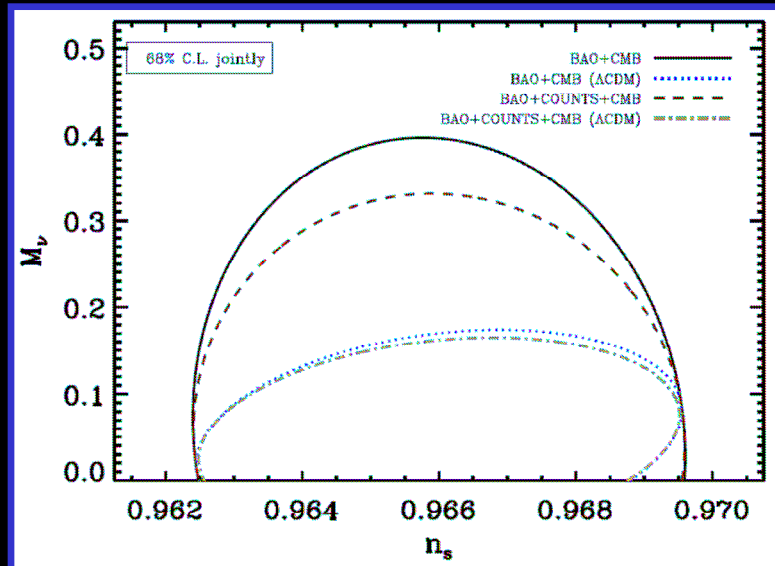
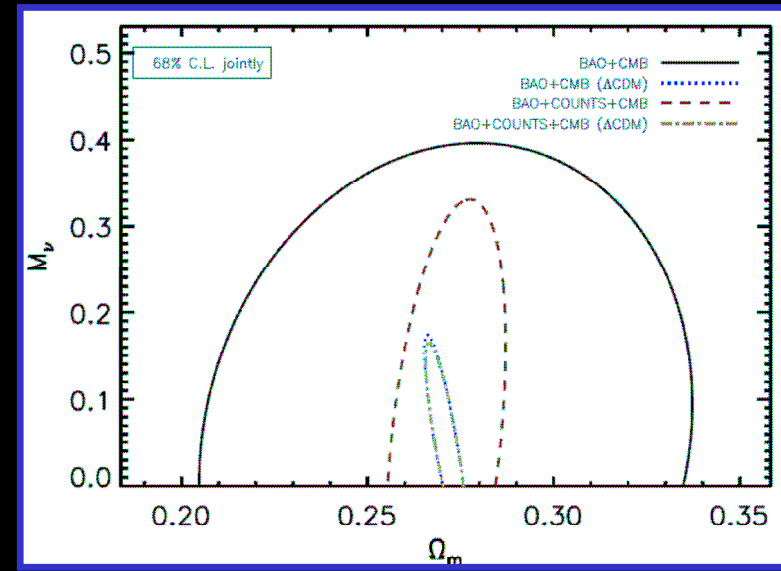
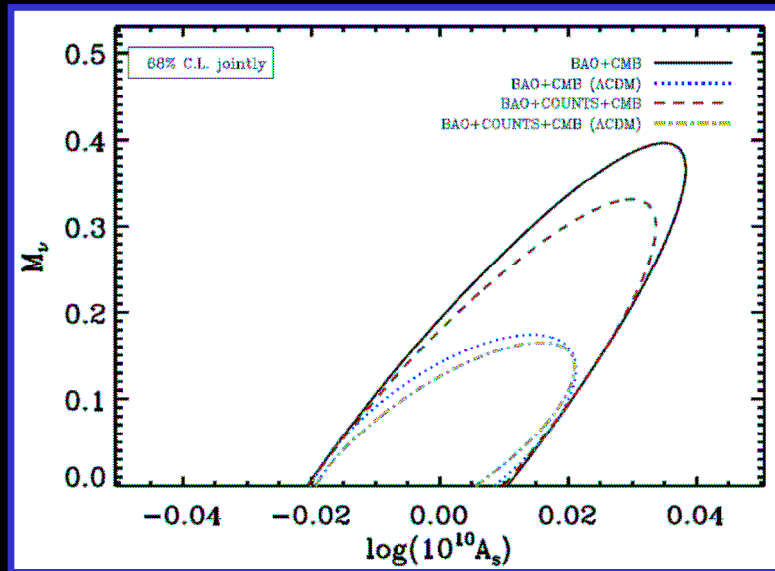
Correlation coefficients

CC et al. 2012

Confidence contours at 68% C.L. for galaxy-clusters (CC et al. 2012)

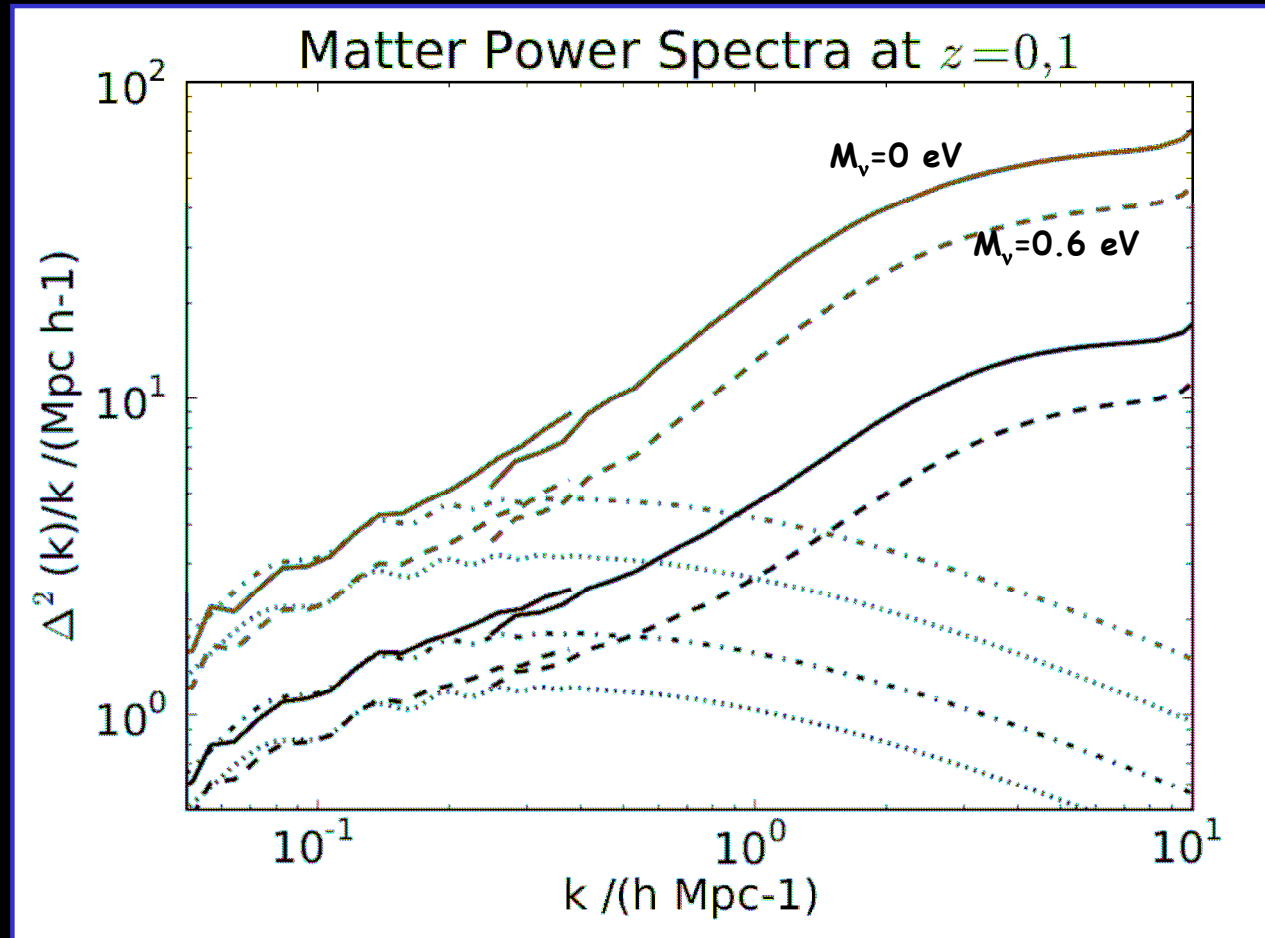


Confidence contours at 68% C.L. for galaxy-clusters (CC et al. 2012)



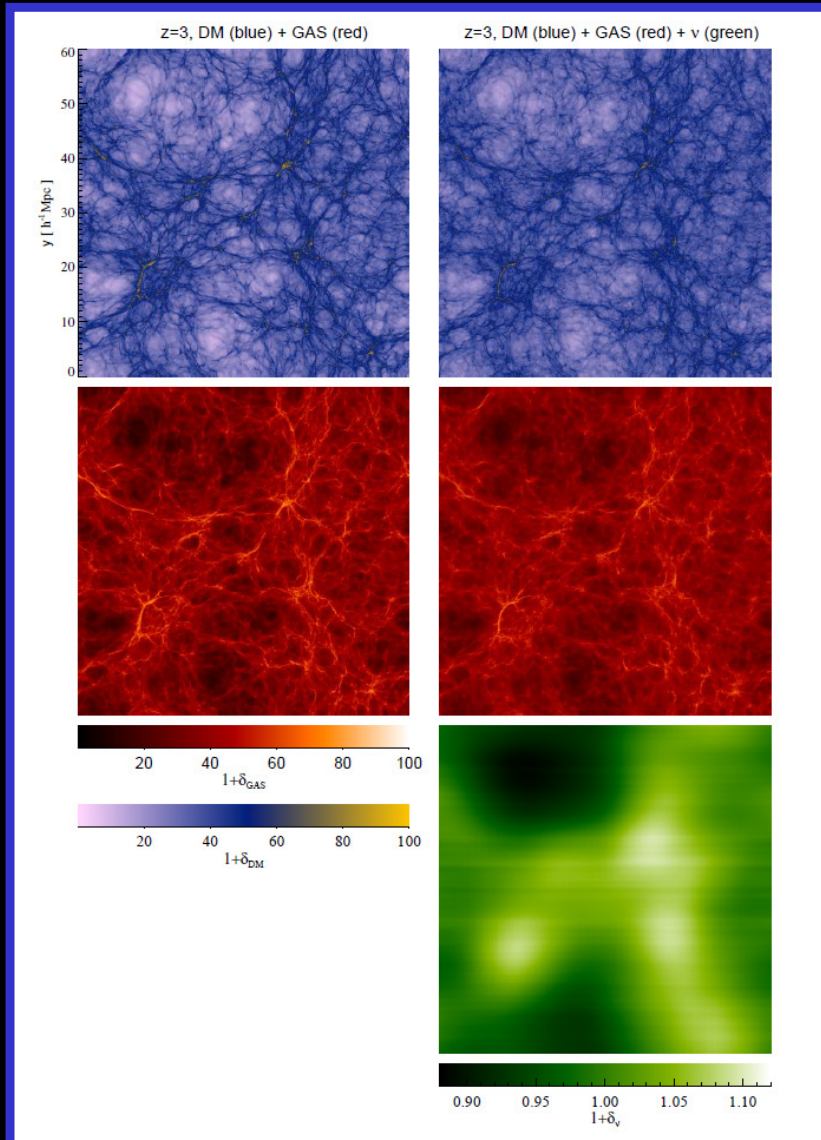
Non-linear effects on the matter power spectrum due to neutrinos

Only 3 active
neutrinos



Bird et al. 2011

Gadget-III modified to include massive neutrinos with a particle-based implementation.



Viel et al. 2010

Density slices of thickness $6 h^{-1}$ comoving Mpc at $z=3$ extracted from two $60 h^{-1}$ Mpc hydrodynamical simulations with gas and dark matter and no neutrinos. The right column shows a simulation that includes neutrinos with $M_\nu = 1.2$ eV. The presence of neutrinos (bottom panel, green) clearly affects both the gas (red) and the dark matter (blue) distribution.

DEMNUi simulations (PI: C. Carbone)

- **5x10⁶ cpu-hours on BGQ/FERMI at CINECA to build up 10 mixed dark matter cosmological simulations**
- **$\Omega_m=0.271$, $\Omega_\Lambda=0.729$, $\Omega_b=0.045$, $h=0.703$, $\sigma_8=0.809$, $n_s=0.966$, $0 < M_\nu < 0.3$ eV, $-1 < w < -0.9$**
- **box-side size: 2 Gpc/h (64 times larger than Millennium)**
- **particle number: 2 x 2048³ (CDM+v)**
- **CDM mass: 6.5 x 10¹⁰ M_⊙/h**
- **softening length: 20 kpc/h**
- **starting redshift: $z_{in}=99$ (depends on M_ν for particle-based v)**
- **# snapshots: 64**

GOALS

- mock galaxy catalogs via box-stacking and HOD
- mock shear maps via box-stacking and ray-tracing
- mock CMB weak-lensing and ISW/Rees-Sciama maps
- CMB/shear/galaxy-clustering statistics
- reference skies for future galaxy/shear/CMB-lensing probes, e.g. Euclid

The above includes a constant DE-background and M_v effects at non-linear level