

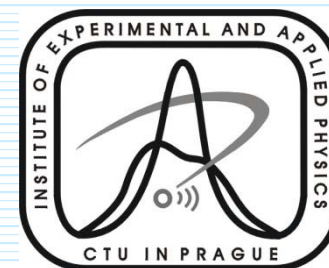
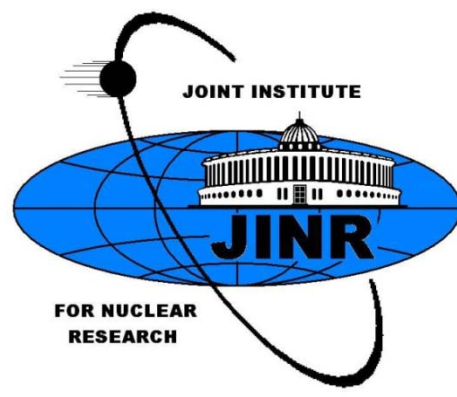


**NEUTRINO  
OSCILLATION  
WORKSHOP**

*Otranto (Lecce), Italy  
September 4-11, 2016*

**Neutrinoless DBD mechanisms and NMEs**

**Fedor Šimkovic**



## OUTLINE

- *Introduction*
- *Standard (conservative)  $0\nu\beta\beta$ -decay picture*  
*Majorana  $\nu$ -mass, NMEs, quenching*
- *Light and heavy  $\nu$ -exchange, V-A interaction*  
*heavy  $\nu$ - NMEs, limit on  $U_{eh}$  mixing*
- *$0\nu\beta\beta$ -decay within the LR-symmetric model*  
*importance of light and  $\nu$ -exchange addressed*
- *Effect of non-standard  $\nu$ -interactions on the  $0\nu\beta\beta$ -decay*  
*complementarity of the cosmology,  $\nu$ -mass,  $0\nu\beta\beta$ -decay*  
*observations*
- *Conclusions*

**Amand Faesler, V. Rodin** (U. Tuebingen), **P. Vogel** (Caltech), **J. Engel** (North Carolina U.), **S. Kovalenko** (Valparaiso U.), **M. Krivoruchenko** (ITEP Moscow), **J. Vergados** (U. Ioannina), **S. Petcov** (SISSA), **D. Štefánik, R. Dvornický** (Comenius U.), **E. Lisi, G. Fogli** (U. Bari) etc

*The answer to the question whether neutrinos are their own antiparticles is of central importance, not only to our understanding of neutrinos, but also to our understanding of the origin of mass.*

## What is the nature of neutrinos?

Actually, when NMEs will be needed to analyze data?



$\nu$



GUT's



Only the  $0\nu\beta\beta$ -decay can answer this fundamental question

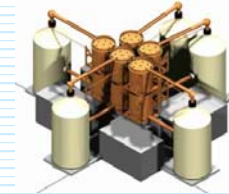
Analogy with  
kaons:  $K_0$  and  $\bar{K}_0$

Could we have both?  
(light Dirac and heavy Majorana)

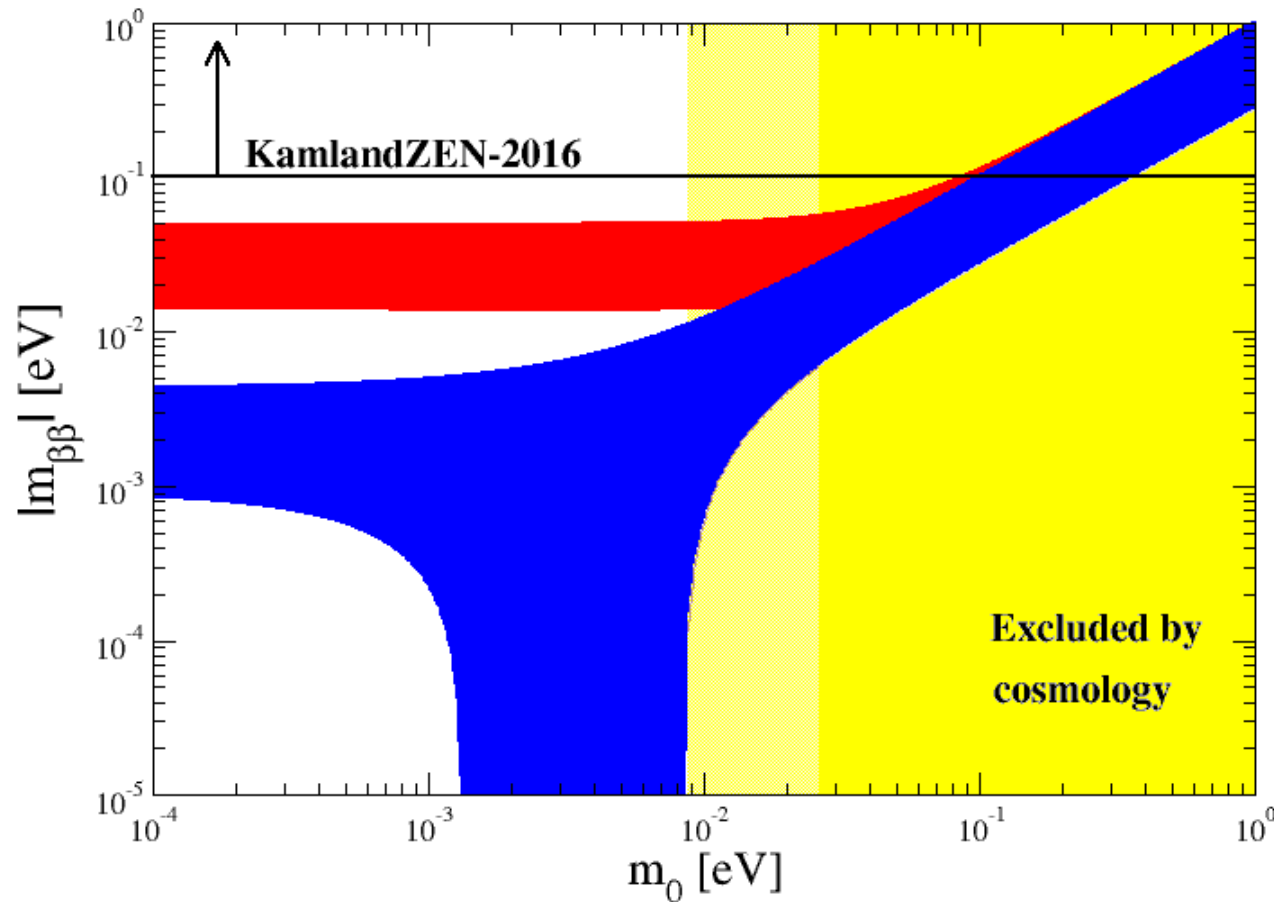
Analogy with  
 $\pi_0$

*Standard (conservative)  $0\nu\beta\beta$ -decay  
picture*

$$\left(T_{1/2}^{0\nu}\right)^{-1} = \left|\frac{m_{\beta\beta}}{m_e}\right|^2 g_A^4 |M_\nu^{0\nu}|^2 G^{0\nu}$$



**Issue: Lightest neutrino mass  $m_0$**



**Complementarity of  $0\nu\beta\beta$ -decay,  $\beta$ -decay and cosmology**

$\beta$ -decay (Mainz, Troitsk)

$$m_\beta^2 = \sum_i |U_{ei}^L|^2 m_i^2 \leq (2.2 \text{ eV})^2$$

**KATRIN:  $(0.2 \text{ eV})^2$**

**Cosmology (Planck)**

$$\Sigma < 110 \text{ meV}$$

$$m_0 > 26 \text{ meV (NS)}$$

$$87 \text{ meV (IS)}$$

**$m_{\beta\beta}=0$  does not imply that the  $0\nu\beta\beta$ -decay is not allowed!**

$$\left(T_{1/2}^{0\nu}\right)^{-1} = \left|\frac{m_{\beta\beta}}{m_e}\right|^2 g_A^4 |M_\nu^{0\nu}|^2 G^{0\nu}$$

Represents a simplified expression for the  $0\nu\beta\beta$ -decay rate

### Decomposition of $\nu$ -propagator

S. Pascoli and S.T Petcov,  
PRD 77, 113003 (2008)

$$\mathcal{P} = \sum_j U_{ej}^2 \frac{m_j}{q^2 - m_j^2} = P_1 + P_3 + P_5 + \dots$$

$$P_1 = \frac{1}{q^2} \sum_j U_{ej}^2 m_j = \frac{1}{q^2} \langle m \rangle \quad P_3 = \frac{1}{q^2} \sum_j U_{ej}^2 m_j \frac{m_j^2}{q^2}$$

$$m_{\beta\beta} \equiv \langle m \rangle \quad m_j^2 \ll |q^2| \quad |q^2| \sim (100 \text{ MeV})^2$$

There are also additional higher order contributions to the  $0\nu\beta\beta$ -decay amplitude



***The  $0\nu\beta\beta$ -decay Nuclear Matrix Elements  
must be evaluated using tools of nuclear theory***

**The double beta decay process can be observed due to nuclear pairing interaction that favors energetically the even-even nuclei over the odd-odd nuclei**

***In double beta decay two neutrons bound in the ground state of an initial even-even nucleus are simultaneously transformed into two protons that are bound in the ground state or excited ( $0^+$ ,  $2^+$ ) states of the final nucleus***

***It is necessary to evaluate, with a sufficient accuracy, wave functions of both nuclei, and evaluate the matrix element of the  $0\nu\beta\beta$ -decay operator connecting them***

***This can not be done exactly, some approximation and/or truncation is always needed. Moreover, there is no other analogues observable that can be used to judge directly the quality of the result.***

Method	$g_A$	src	$M_\nu^{0\nu}$					
			$^{48}\text{Ca}$	$^{76}\text{Ge}$	$^{82}\text{Se}$	$^{96}\text{Zr}$	$^{100}\text{Mo}$	$^{110}\text{Pd}$
ISM-StMa	1.25	UCOM	0.85	2.81	2.64			
ISM-CMU	1.27	Argonne	0.80	3.37	3.19			
		CD-Bonn	0.88	3.57	3.39			
IBM	1.27	Argonne	1.75	4.68	3.73	2.83	4.22	4.05
QRPA-TBC	1.27	Argonne	0.54	5.16	4.64	2.72	5.40	5.76
		CD-Bonn	0.59	5.57	5.02	2.96	5.85	6.26
QRPA-Jy	1.26	CD-Bonn		5.26	3.73	3.14	3.90	6.52
dQRPA-NC	1.25	without		5.09				
PHFB	1.25	Argonne				2.84	5.82	7.12
		CD-Bonn				2.98	6.07	7.42
NREDF	1.25	UCOM	2.37	4.60	4.22	5.65	5.08	
REDF	1.25	without	2.94	6.13	5.40	6.47	6.58	
Mean value			1.34	4.55	4.02	3.78	5.57	6.12
variance			0.81	1.20	0.91	2.49	0.58	1.78

Method	$g_A$	src	$M_\nu^{0\nu}$					
			$^{116}\text{Cd}$	$^{124}\text{Sn}$	$^{128}\text{Te}$	$^{130}\text{Te}$	$^{136}\text{Xe}$	$^{150}\text{Nd}$
ISM-StMa	1.25	UCOM		2.62		2.65	2.19	
ISM-CMU	1.27	Argonne		2.00		1.79	1.63	
		CD-Bonn		2.15		1.93	1.76	
IBM	1.27	Argonne	3.10	3.19	4.10	3.70	3.05	2.67
QRPA-TBC	1.27	Argonne	4.04	2.56	4.56	3.89	2.18	
		CD-Bonn	4.34	2.91	5.08	4.37	2.46	3.37
QRPA-Jy	1.26	CD-Bonn	4.26	5.30	4.92	4.00	2.91	
dQRPA-NC	1.25	without				1.37	1.55	2.71
PHFB	1.27	Argonne			3.90	3.81		2.58
		CD-Bonn			4.08	3.98		2.68
NREDF	1.25	UCOM	4.72	4.81	4.11	5.13	4.20	1.71
REDF	1.25	without	5.52	4.33		4.98	4.32	5.60
Mean value			4.34	3.07	4.34	3.42	2.59	3.01
variance			0.79	1.01	0.23	1.67	1.10	1.34

**NMEs for  
unquenched value  
of  $g_A$**

**Mean field approaches  
(PHFB, NREDF, REDF)  
⇒ Large NMEs**

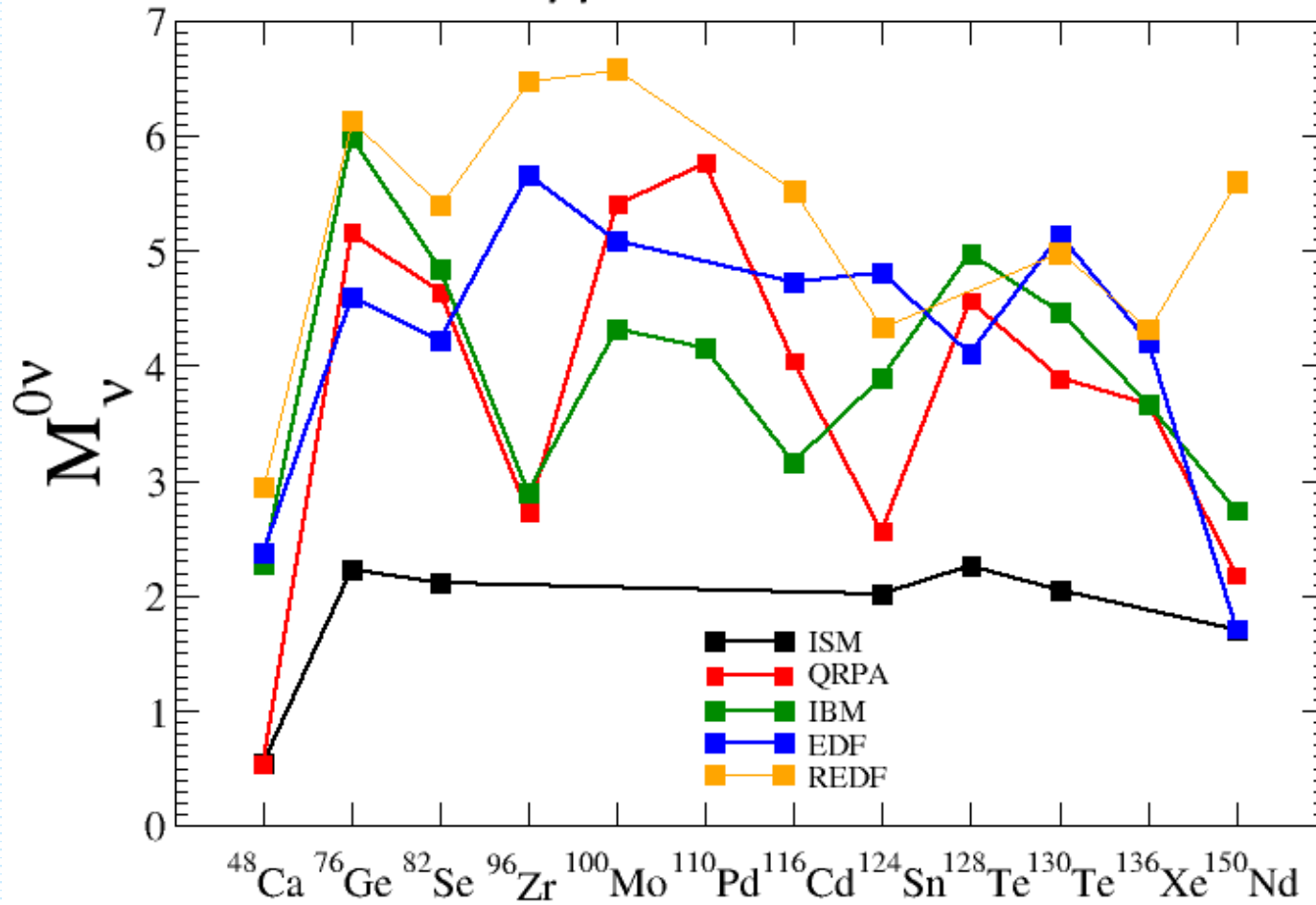
**Interacting Shell Model  
(ISM-StMa, ISM-CMU)  
⇒ small NMEs**

**Quasiparticle Random  
Phase Approximation  
(QRPA-TBC, QRPA-Jy,  
dQRPA-NC)  
⇒ Intermediate NMEs**

**Interacting Boson Model  
(IBM)  
⇒ Close to QRPA results**

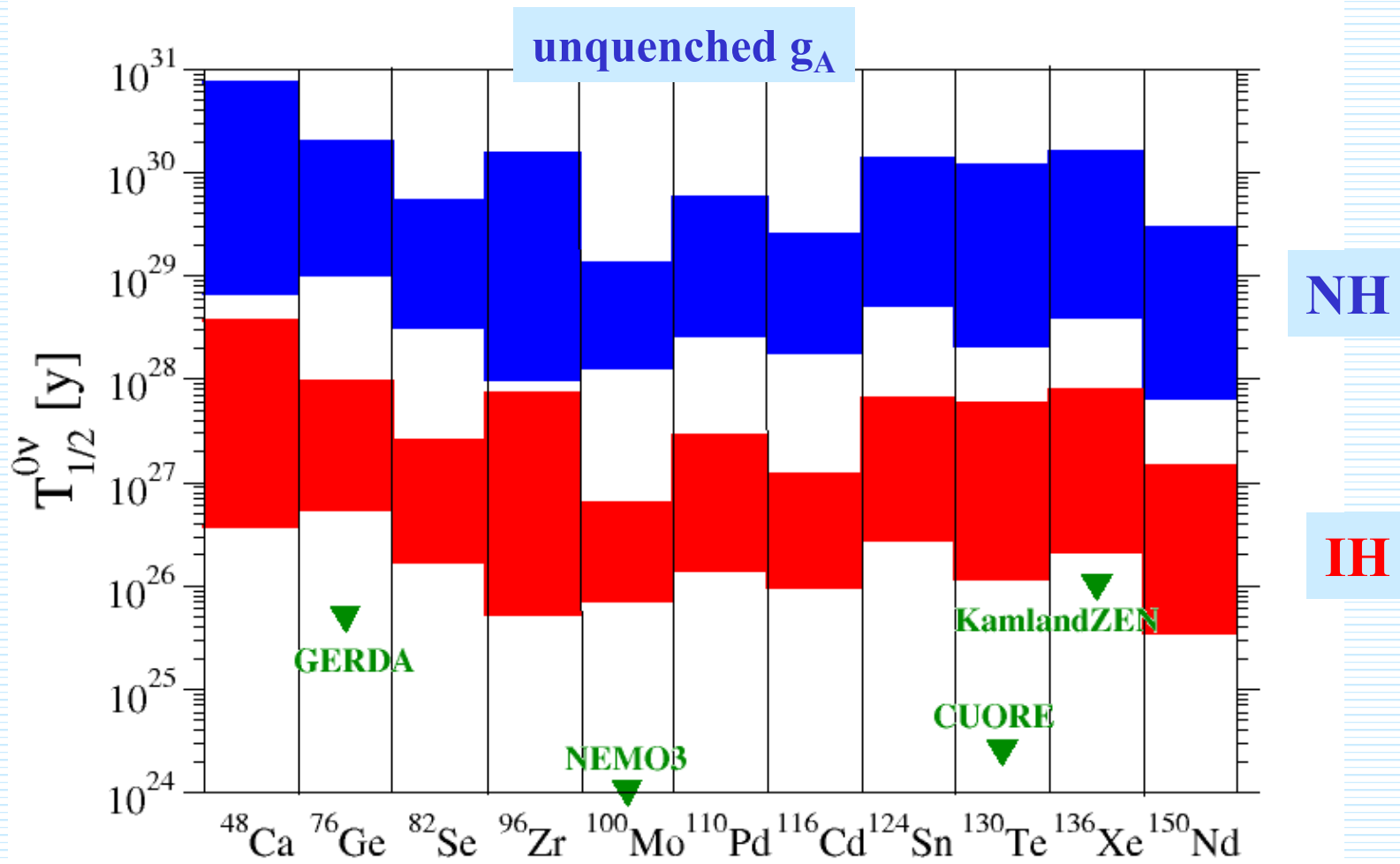


## $0\nu\beta\beta$ NMEs -status 2016



	mean field meth.	ISM	IBM	QRPA
Large model space	yes	no	yes	yes
Constr. Interm. States	no	yes	no	yes
Nucl. Correlations	limited	all	restricted	restricted

# $0\nu\beta\beta$ –half lives for NH and IH with included uncertainties in NMEs



**NH:**  $m_1 \ll m_2 \ll m_3$   $m_3 \simeq \sqrt{\Delta m^2}$

**IH:**  $m_3 \ll m_1 < m_2$   $m_1 \simeq m_2 \simeq \sqrt{\Delta m^2}$

$m_1 \ll \sqrt{\delta m^2}$ ,  $m_2 \simeq \sqrt{\delta m^2}$

$m_3 \ll \sqrt{\Delta m^2}$

$1.4 \text{ meV} \leq m_{\beta\beta} \leq 3.6 \text{ meV}$

Lightest  $\nu$ -mass equal to zero

$20 \text{ meV} \leq m_{\beta\beta} \leq 49 \text{ meV}$

# Could multiple $0\nu\beta\beta$ measurements be helpful to extract $m_{\beta\beta}$ ?

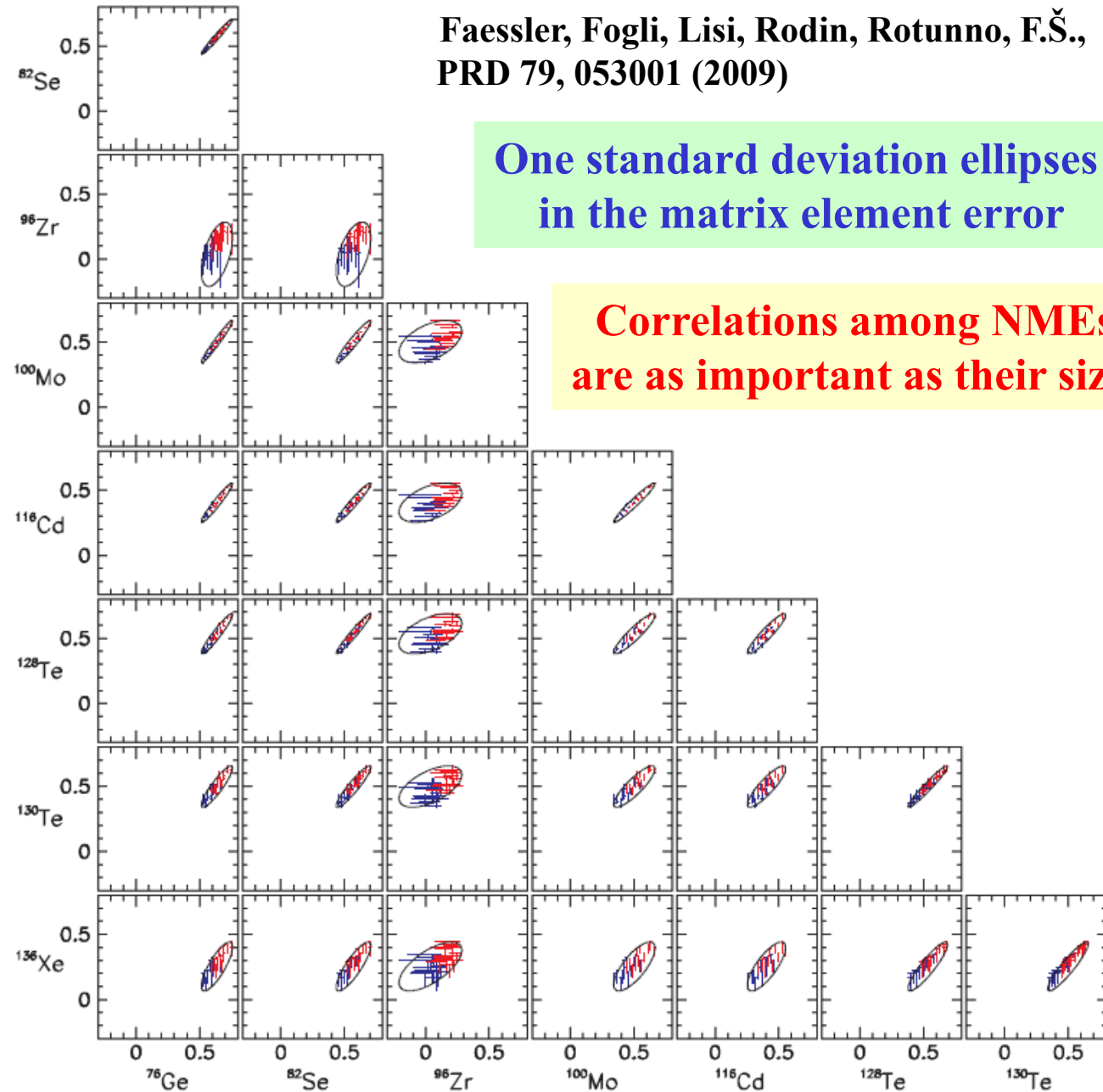
**Problem:**  
Uncertainties  
in NME from  
different  
nuclei are highly  
correlated.

**Calculations:**  
varying method  
(QRPA, RQRPA),  
the value  $g_A^{\text{eff}}$   
(1.0 and 1.25),  
the treatment of  $\text{src}$   
(Jastr. and UCOM),  
the size of model  
space (3 choices)

Faessler, Fogli, Lisi, Rodin, Rotunno, F.Š.,  
PRD 79, 053001 (2009)

One standard deviation ellipses  
in the matrix element error

Correlations among NMEs  
are as important as their size.



*Is this expression accurate enough?*

$$\left(T_{1/2}^{0\nu}\right)^{-1} = \left|\frac{m_{\beta\beta}}{m_e}\right|^2 g_A^4 |M_\nu^{0\nu}|^2 G^{0\nu}$$

## *The $0\nu\beta\beta$ -decay with emission of electrons in $p_{1/2}$ wave state*

D. Štefánik, R. Dvornický, F.Š., Nuclear Theory 33 (2014) 115

$$\psi(\mathbf{r}, p, s) \simeq \psi_{s_{1/2}}(\mathbf{r}, p, s) + \psi_{p_{1/2}}(\mathbf{r}, p, s) =$$

$$\begin{pmatrix} g_{-1}(\varepsilon, r) \chi_s \\ f_{+1}(\varepsilon, r) (\vec{\sigma} \cdot \hat{\mathbf{p}}) \chi_s \end{pmatrix} + \begin{pmatrix} ig_{+1}(\varepsilon, r) (\vec{\sigma} \cdot \hat{\mathbf{r}}) (\vec{\sigma} \cdot \hat{\mathbf{p}}) \chi_s \\ -if_{-1}(\varepsilon, r) (\vec{\sigma} \cdot \hat{\mathbf{r}}) \chi_s \end{pmatrix}$$

Exact relativ. electron w.f.

$$J^\rho(\mathbf{x}) = \sum_n \tau_n^+ \delta(\mathbf{x} - \mathbf{r}_n) \left[ (g_V - g_A C_n) g^{\rho 0} + g^{\rho k} \right.$$

$$\left. \times \left( g_A \sigma_n^k - g_V D_n^k - g_P (p_n^k - p_n'^k) \frac{\vec{\sigma}_n \cdot (\mathbf{p}_n - \mathbf{p}_n')}{2m_N} \right) \right]$$

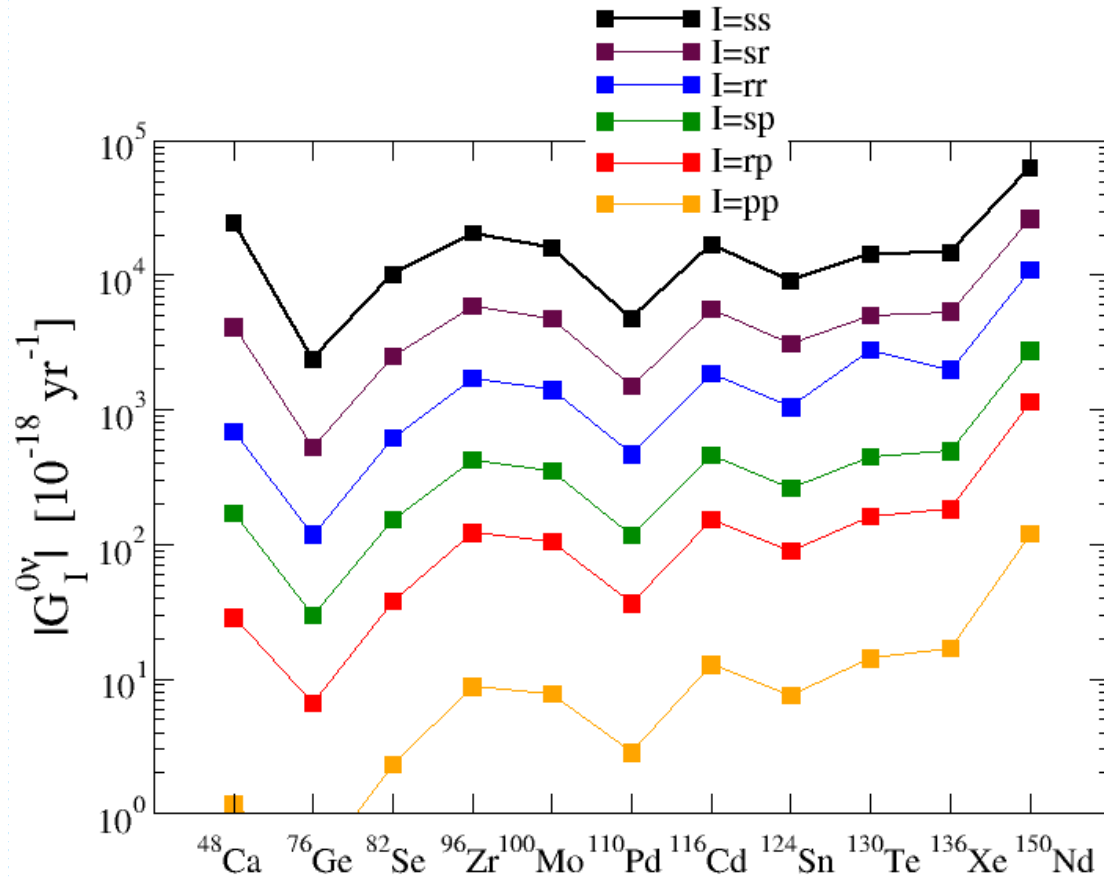
Higher order terms of nucleon current with nucleon recoil (odd parity operators)

$$C_n = \frac{\vec{\sigma}_n \cdot (\mathbf{p}_n + \mathbf{p}_n')}{2m_N} - \frac{g_P}{g_A} (E_n - E_n') \frac{\vec{\sigma}_n \cdot (\mathbf{p}_n - \mathbf{p}_n')}{2m_N}$$

$$D_n = \frac{(\mathbf{p}_n + \mathbf{p}_n')}{2m_N} - i \left( 1 + \frac{g_M}{g_V} \right) \frac{\vec{\sigma}_n \times (\mathbf{p}_n - \mathbf{p}_n')}{2m_N}$$

**$0\nu\beta\beta$ -decay rate  
with  $p_{1/2}$  electrons  
(2 additional NMEs  
and 5 phase-space  
factors)**

$$\left[ T_{1/2}^{0\nu\beta\beta} \right]^{-1} = \frac{|m_{\beta\beta}|^2}{m_e^2} g_A^4 \left( 2\text{Re} \{ M_s M_r^* \} G_{sr} \right. \\ \left. + 2\text{Re} \{ M_s M_p^* \} G_{sp} + 2\text{Re} \{ M_r M_p^* \} G_{rp} \right. \\ \left. + G_{ss} |M_s|^2 + G_{rr} |M_r|^2 + G_{pp} |M_p|^2 \right),$$



**Calculated phase-space  
factor for  $0\nu\beta\beta$ -decay  
with emission of  $s_{1/2}$  and  $p_{1/2}$   
electrons  
( $m_{\beta\beta}$  mechanism)**

**Effect of  $p_{1/2}$  wave is below 10%**

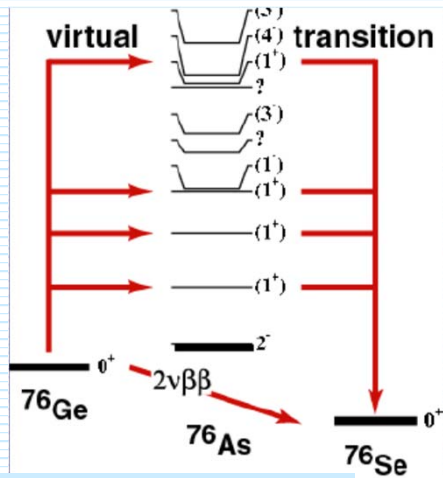
**Some kinematical factor  
large but corresponding  
NMEs are small.**

$g_A^4 = (1.269)^4 = 2.6$  **Quenching of  $g_A$**  (from exp.:  $T_{1/2}^{0\nu}$  up 2.5 x larger)

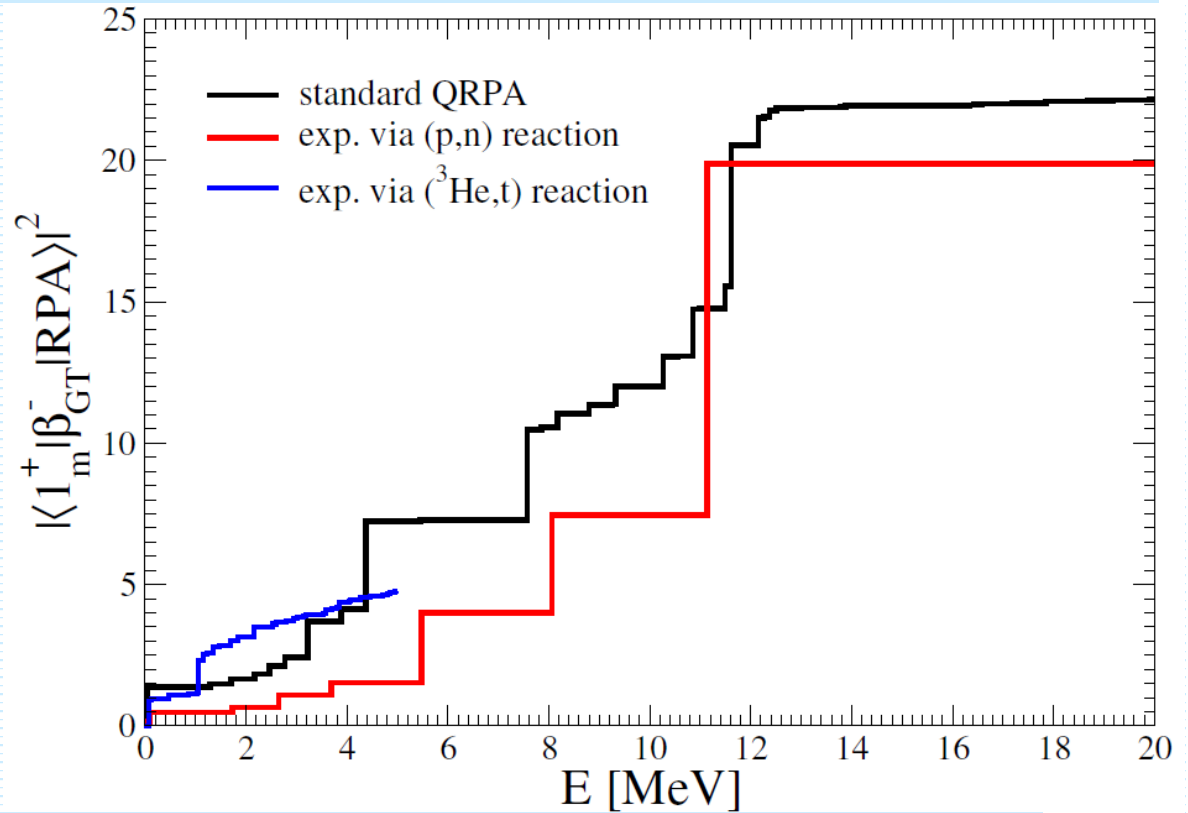
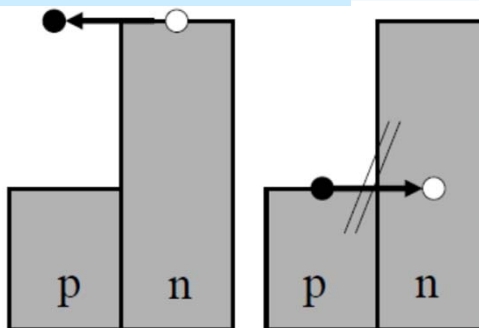
$(g_A^{\text{eff}})^4 = 1.0$

Strength of GT trans. (approx. given by Ikeda sum rule =  $3(N-Z)$ ) has to be quenched to reproduce experiment

${}^{76}_{32}\text{Ge}_{44} \Rightarrow$   
 $S_{\beta^-} - S_{\beta^+} = 3(N-Z) = 36$



**Pauli blocking**



**Cross-section for charge exchange reaction:**

$$\left[ \frac{d\sigma}{d\Omega} \right] = \left[ \frac{\mu}{\pi\hbar} \right]^2 \frac{k_f}{k_i} N_d |v_{\sigma\tau}|^2 |\langle f | \sigma\tau | i \rangle|^2$$

$q = 0!!$

largest at 100 - 200 MeV/A



## Quenching of $g_A$ (from theory: $T_{1/2}^{0\nu}$ up 50 x larger)

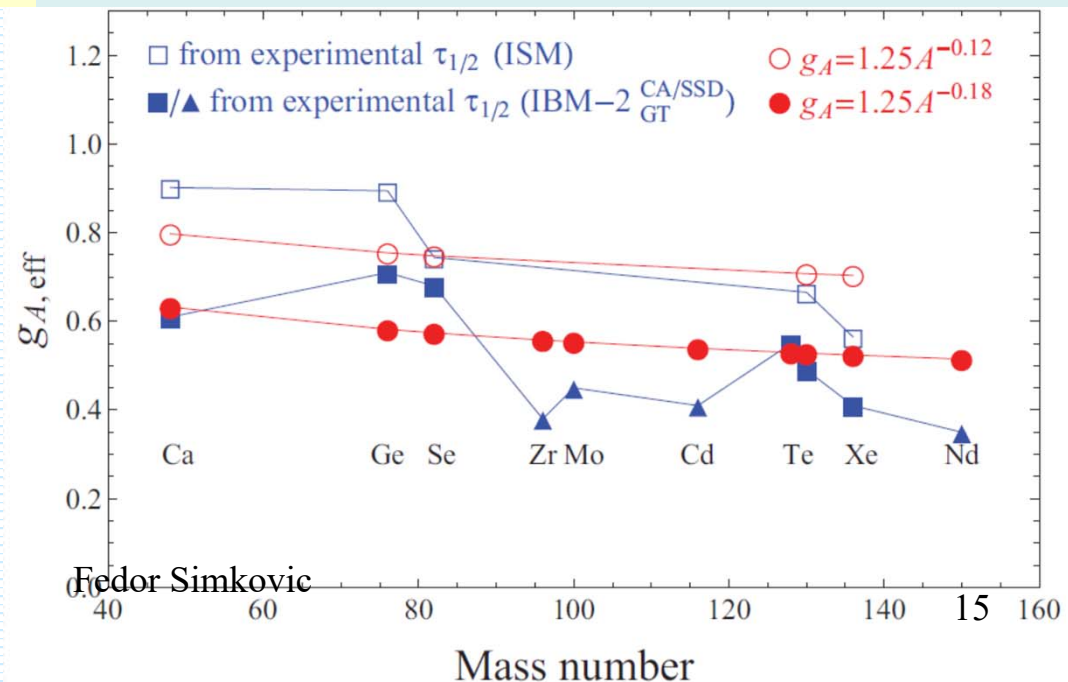
$(g_A^{\text{eff}})^4 \simeq 0.66$  ( $^{48}\text{Ca}$ ),  $0.66$  ( $^{76}\text{Ge}$ ),  $0.30$  ( $^{76}\text{Se}$ ),  $0.20$  ( $^{130}\text{Te}$ ) and  $0.11$  ( $^{136}\text{Xe}$ )

**The Interacting Shell Model (ISM)**, which describes qualitatively well energy spectra, does reproduce experimental values of  $M^{2\nu}$  only by consideration of significant quenching of the Gamow-Teller operator, typically by **0.45 to 70%**.

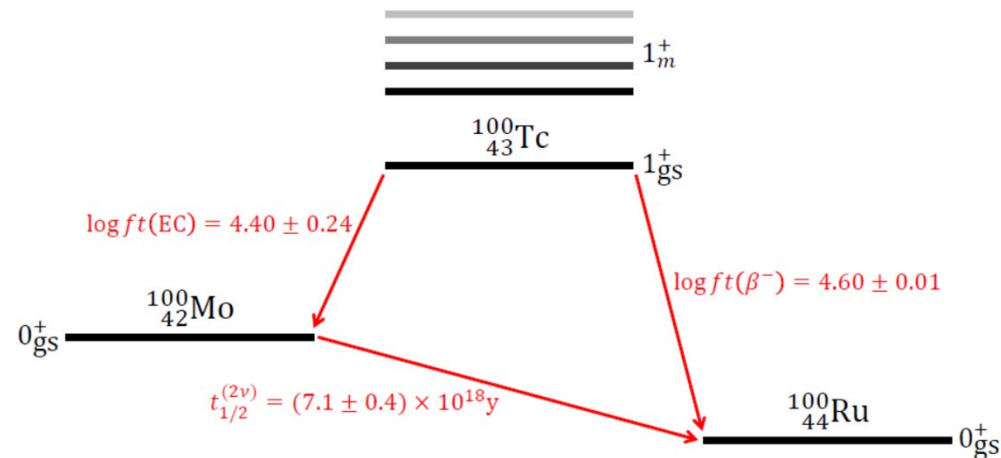
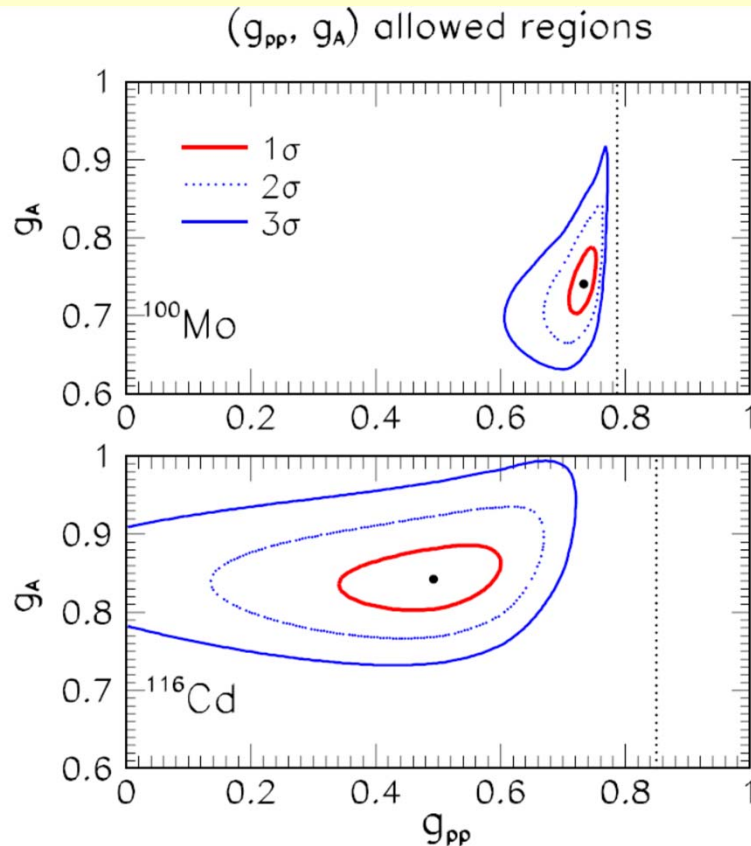
$(g_A^{\text{eff}})^4 \simeq (1.269 A^{-0.18})^4 = 0.063$  (**The Interacting Boson Model**). This is an incredible result. The quenching of the axial-vector coupling within the IBM-2 is more like **60%**.

J. Barea, J. Kotila, F. Iachello, PRC 87, 014315 (2013).

It has been determined by theoretical prediction for the  **$2\nu\beta\beta$ -decay half-lives**, which were based on within **closure approximation** calculated corresponding NMEs, with the measured half-lives.



$(g_A^{\text{eff}})^4 = 0.30$  and  $0.50$  for  $^{100}\text{Mo}$  and  $^{116}\text{Cd}$ , respectively (**The QRPA prediction**).  $g_A^{\text{eff}}$  was treated as a completely free parameter alongside  $g_{pp}$  (used to renormalize particle-particle interaction) by performing calculations within the QRPA and RQRPA. It was found that a least-squares fit of  $g_A^{\text{eff}}$  and  $g_{pp}$ , where possible, to the  **$\beta$ -decay rate** and  **$\beta$ +/**EC rate** of the  $J = 1^+$  ground state in the intermediate nuclei involved in double-beta decay in addition to the  **$2\nu\beta\beta$  rates** of the initial nuclei, leads to an effective  $g_A^{\text{eff}}$  of about **0.7** or **0.8**.**



Extended calculation also for neighbour isotopes performed by

F.F. Depisch and J. Suhonen, arXiv:1606.02908[nucl-th]

r Simkovic

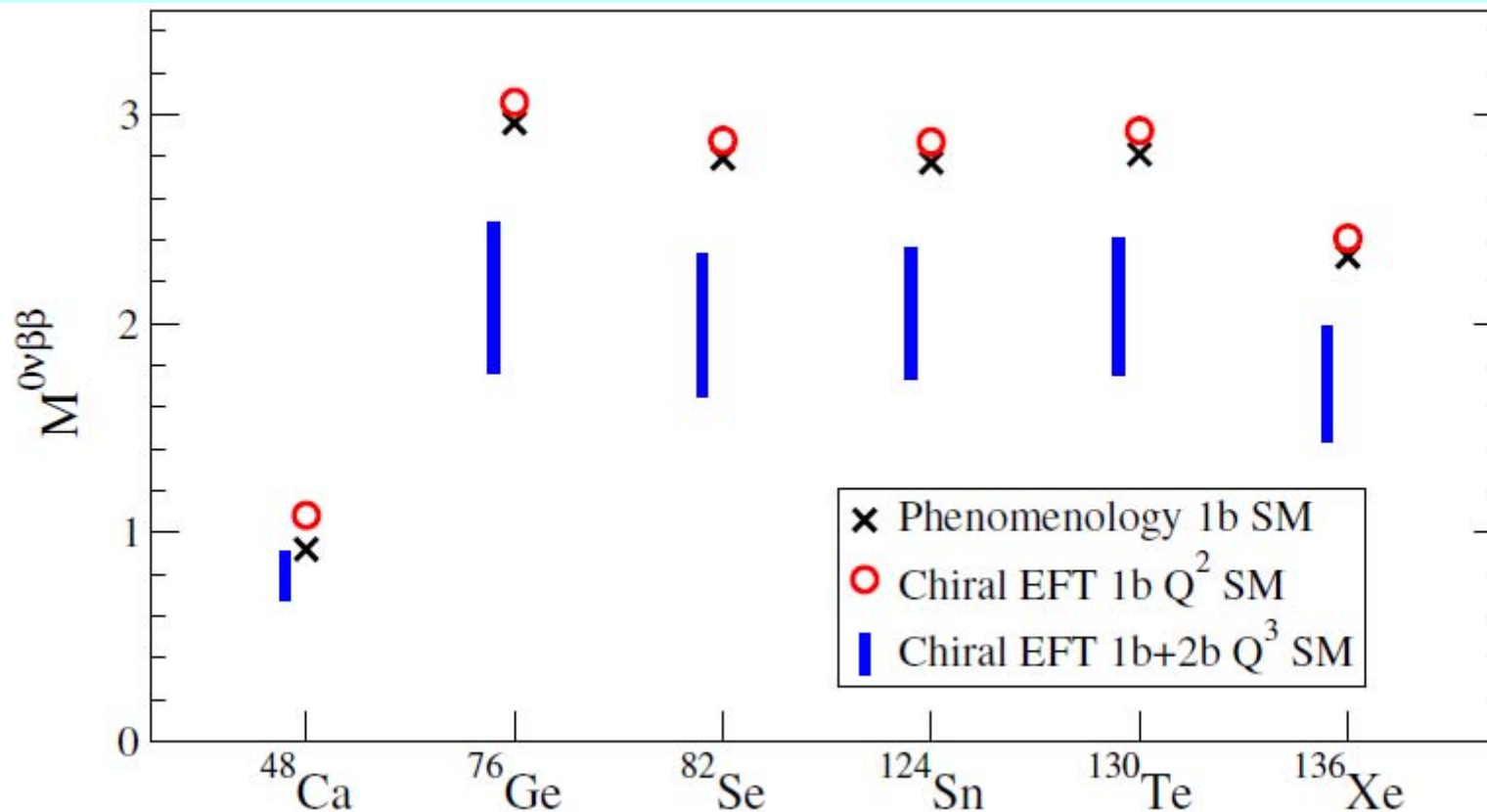
Dependence of  $g_A^{\text{eff}}$  on  $A$  was not established.

# Quenching of $g_A$ and two-body currents

Menendez, Gazit, Schwenk, *PRL* 107 (2011) 062501; MEDEX13 contribution

$$\mathbf{J}_{i,2b}^{\text{eff}} = -g_A \boldsymbol{\sigma}_i \tau_i^- \frac{\rho}{F_\pi^2} \left[ \frac{2}{3} c_3 \frac{p^2}{4m_\pi^2 + p^2} + I(\rho, P) \left( \frac{1}{3} (2c_4 - c_3) + \frac{1}{6m} \right) \right] = -g_A \delta(p) \boldsymbol{\sigma}_i \tau_i^-$$

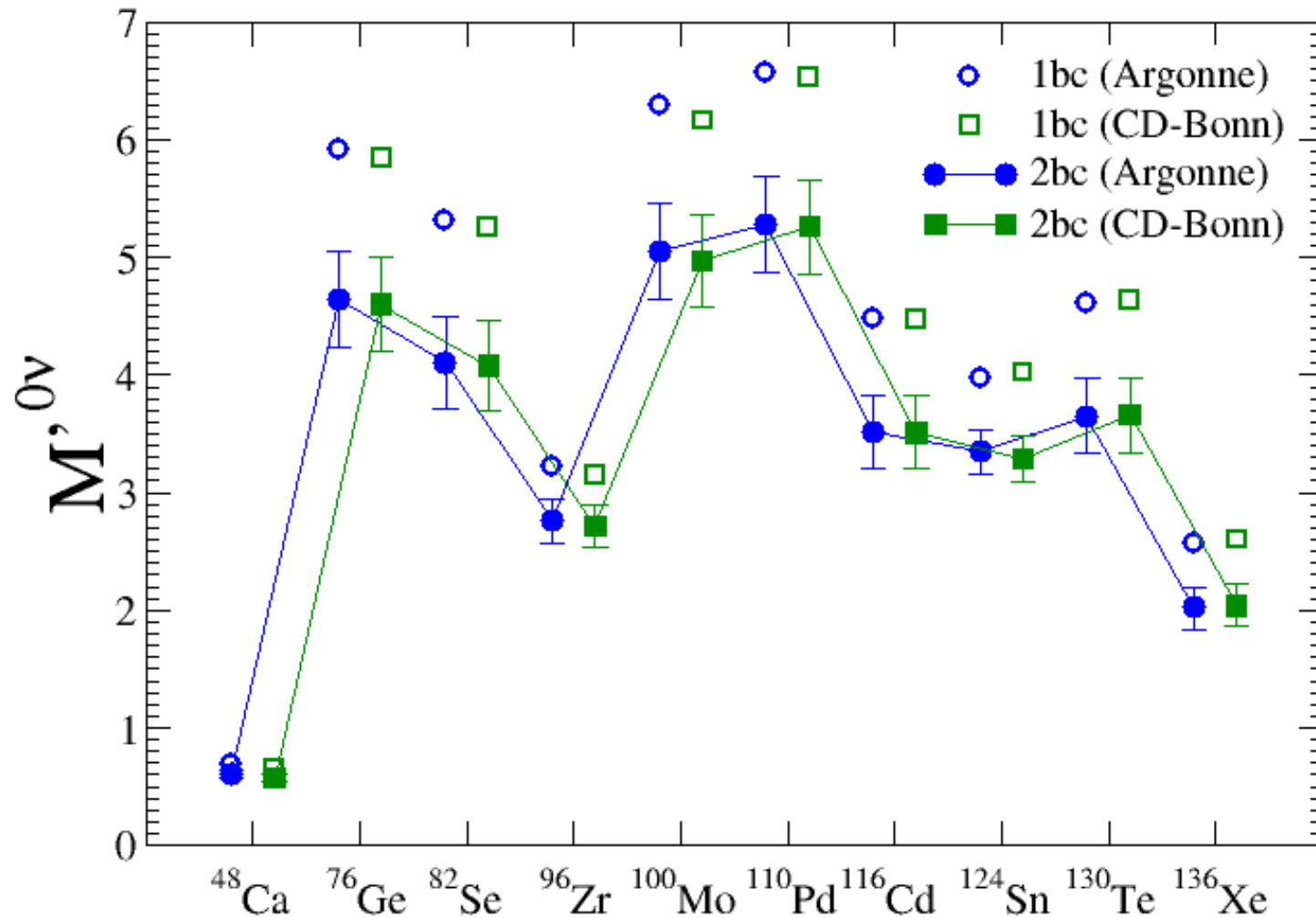
The  $0\nu\beta\beta$  operator calculated within effective field theory. Corrections appear as 2-body current predicted by EFT. The 2-body current contributions are related to the quenching of Gamow-Teller transitions found in nuclear structure calc.



# Quenching of $g_A$ , two-body currents and QRPA

(Suppression of the  $0\nu\beta\beta$ -decay NME of about 20%)

Engel, Vogel, Faessler, F.Š., PRC 89 (2014) 064308



But, a strong suppression of  $2\nu\beta\beta$ -decay half-life, ( $g_A^{\text{eff}} = g_A \delta(p=0) = 0.7-1.0$ )

# *The DBD Nuclear Matrix Elements and the SU(4) symmetry*

D. Štefánik, F.Š., A. Faessler, PRC 91, 064311 (2015)

## Suppression of the Two Neutrino Double Beta Decay by Nuclear Structure Effects

P. Vogel, M.R. Zirnbauer, PRL (1986) 3148

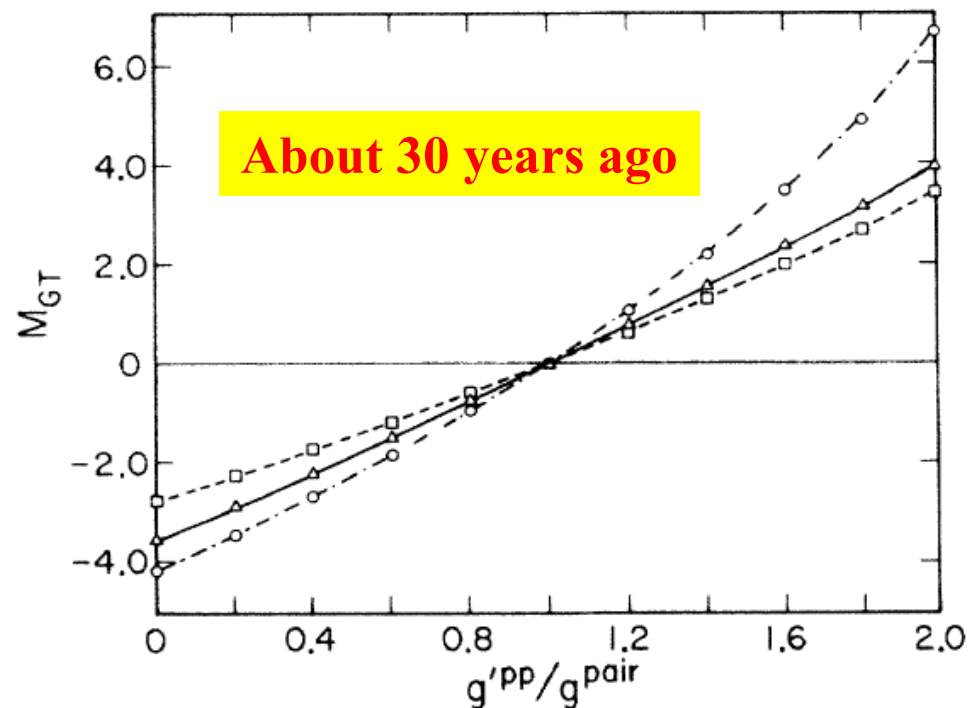
O. Civitarese, A. Faessler, T. Tomoda,  
PLB 194 (1987) 11

E. Bender, K. Muto, H.V. Klapdor,  
PLB 208 (1988) 53

...

The isospin is known to be a  
good approximation in nuclei

In heavy nuclei the SU(4) symmetry  
is strongly broken  
by the spin-orbit splitting.



What is beyond this behavior? Is it an artifact of the QRPA?

**s.p. mean-field**

**Conserves SU(4) symmetry**

$$H = \underbrace{e_n N_n + e_p N_p - g_{pair} \left( \sum_{M_T=-1,0,1} A_{0,1}^\dagger(0, M_T) A_{0,1}(0, M_T) + \sum_{M_S=-1,0,1} A_{1,0}^\dagger(M_S, 0) A_{1,0}(M_S, 0) \right)}_{H_0} + g_{ph} \sum_{a,b} E_{a,b}^\dagger E_{a,b}$$

$$+ \underbrace{(g_{pair} - g_{pp}^{T=0}) \sum_{M_S=-1,0,1} A_{1,0}^\dagger(M_S, 0) A_{1,0}(M_S, 0) + (g_{pair} - g_{pp}^{T=1}) A_{0,1}^\dagger(0, 0) A_{0,1}(0, 0)}_{H_I}.$$

**H<sub>I</sub> violates SU(4) symmetry**

**g<sub>pair</sub>** - strength of isovector like nucleon pairing (L=0, S=0, T=1, M<sub>T</sub>=±1)

**g<sub>pp</sub><sup>T=1</sup>** - strength of isovector spin-0 pairing (L=0, S=0, T=1, M<sub>T</sub>=0)

**g<sub>pp</sub><sup>T=0</sup>** - strength of isoscalar spin-1 pairing (L=0, S=1, T=0)

**g<sub>ph</sub>** - strength of particle-hole force

**M<sub>F</sub> and M<sub>GT</sub>** do not depend on the mean-field part of **H** and are governed by a weak violation of the **SU(4)** symmetry by the particle-particle interaction of **H**

$$M_F^{2\nu} = - \frac{48 \sqrt{\frac{33}{5}} (g_{pair} - g_{pp}^{T=1})}{(5g_{pair} + 3g_{ph})(10g_{pair} + 6g_{ph})}$$

$$M_{GT}^{2\nu} = \frac{144 \sqrt{\frac{33}{5}}}{5g_{pair} + 9g_{ph}} \left\{ \frac{(g_{pair} - g_{pp}^{T=0})}{(10g_{pair} + 20g_{ph})} + \frac{2g_{ph}(g_{pair} - g_{pp}^{T=1})}{(10g_{pair} + 20g_{ph})(10g_{pair} + 6g_{ph})} \right\}$$



*The  $0\nu\beta\beta$ -decay mechanisms with  
light and heavy neutrinos  
(V-A interaction)*

# Left-handed neutrinos: Majorana neutrino mass eigenstate $N$ with arbitrary mass $m_N$

Faessler, Gonzales, Kovalenko, F. Š., PRD 90 (2014) 096010

$$N = \sum_{\alpha=s,e,\mu,\tau} U_{N\alpha} \nu_\alpha$$

$$[T_{1/2}^{0\nu}]^{-1} = G^{0\nu} g_A^4 \left| \sum_N (U_{eN}^2 m_N) m_p M'^{0\nu}(m_N, g_A^{\text{eff}}) \right|^2$$

## General case

$$M'^{0\nu}(m_N, g_A^{\text{eff}}) = \frac{1}{m_p m_e} \frac{R}{2\pi^2 g_A^2} \sum_n \int d^3x d^3y d^3p \quad M'^{0\nu}(m_N \rightarrow 0, g_A^{\text{eff}}) = \frac{1}{m_p m_e} M_\nu'^{0\nu}(g_A^{\text{eff}})$$

$$\times e^{i\mathbf{p}\cdot(\mathbf{x}-\mathbf{y})} \frac{\langle 0_F^+ | J^{\mu\dagger}(\mathbf{x}) | n \rangle \langle n | J_\mu^\dagger(\mathbf{y}) | 0_I^+ \rangle}{\sqrt{p^2 + m_N^2} (\sqrt{p^2 + m_N^2} + E_n - \frac{E_I - E_F}{2})} \quad M'^{0\nu}(m_N \rightarrow \infty, g_A^{\text{eff}}) = \frac{1}{m_N^2} M_N'^{0\nu}(g_A^{\text{eff}})$$

## Particular cases

$$[T_{1/2}^{0\nu}]^{-1} = G^{0\nu} g_A^4 \times$$

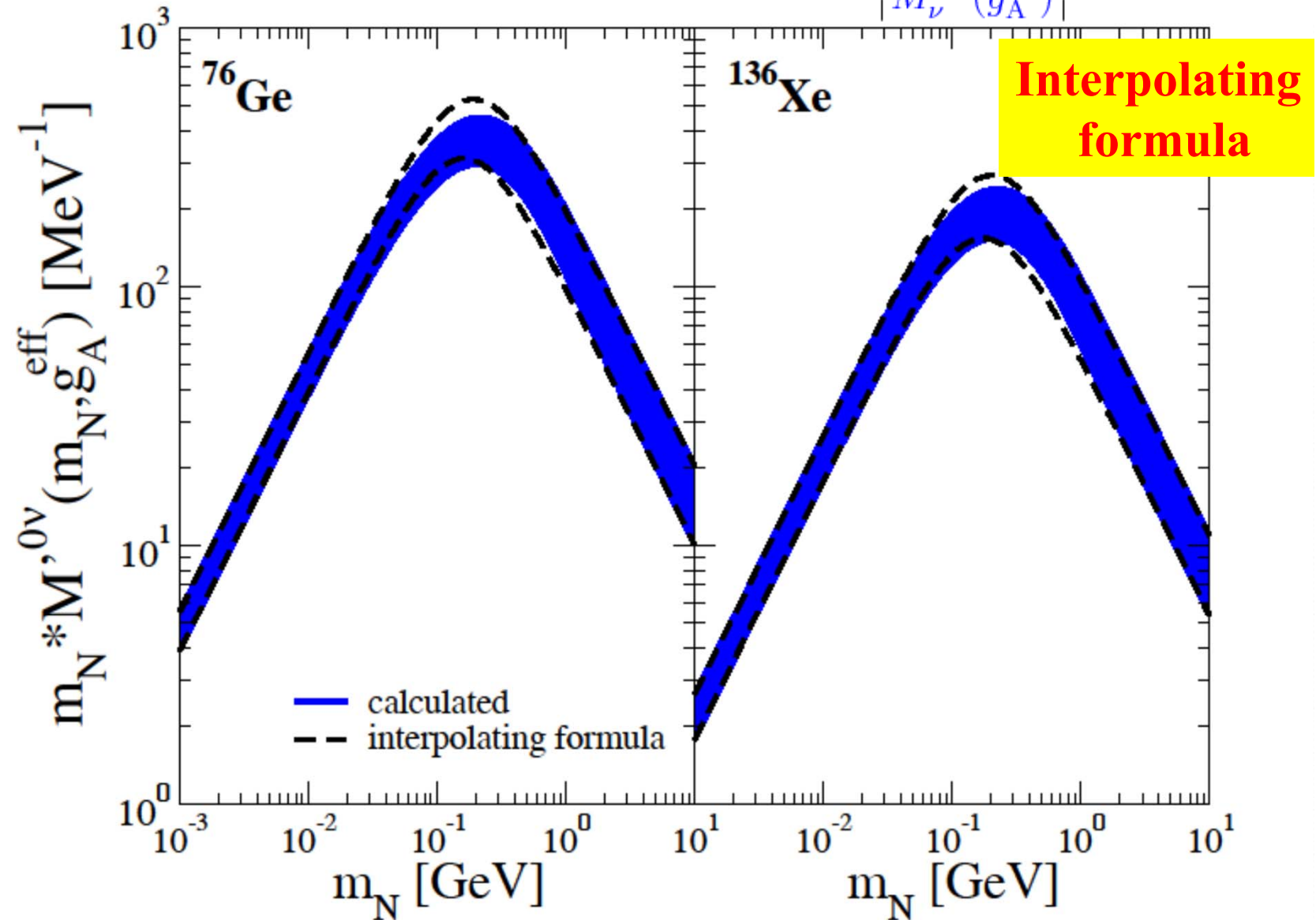
$$\times \begin{cases} \left| \frac{\langle m_\nu \rangle}{m_e} \right|^2 \left| M_\nu'^{0\nu}(g_A^{\text{eff}}) \right|^2 & \text{for } m_N \ll p_F \\ \left| \langle \frac{1}{m_N} \rangle m_p \right|^2 \left| M_N'^{0\nu}(g_A^{\text{eff}}) \right|^2 & \text{for } m_N \gg p_F \end{cases}$$

$$\langle m_\nu \rangle = \sum_N U_{eN}^2 m_N$$

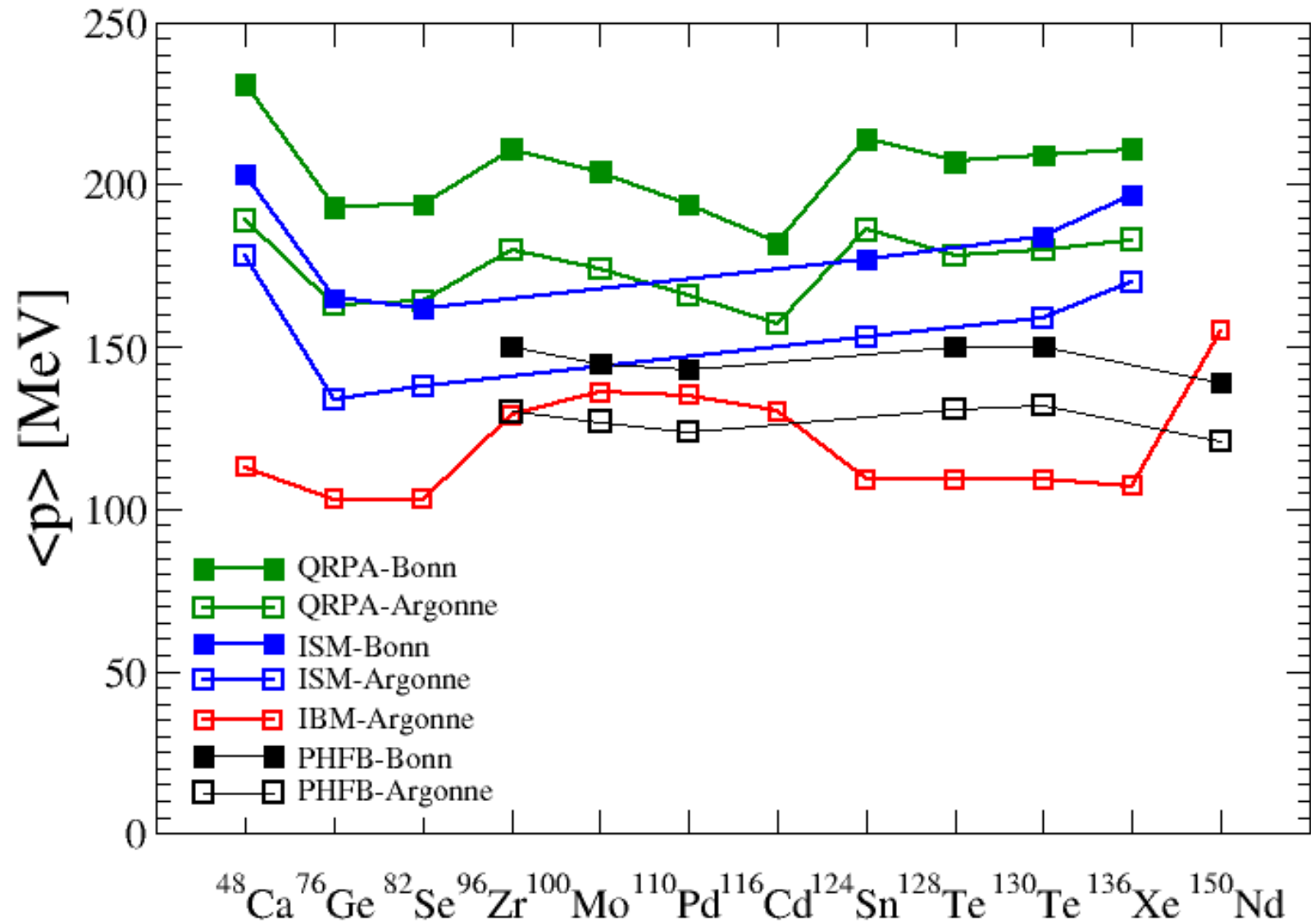
$$\left\langle \frac{1}{m_N} \right\rangle = \sum_N \frac{U_{eN}^2}{m_N}$$

$$[T_{1/2}^{0\nu}]^{-1} = \mathcal{A} \cdot \left| m_p \sum_N U_{eN}^2 \frac{m_N}{\langle p^2 \rangle + m_N^2} \right|^2, \quad \mathcal{A} = G^{0\nu} g_A^4 \left| M_N^{0\nu}(g_A^{\text{eff}}) \right|^2,$$

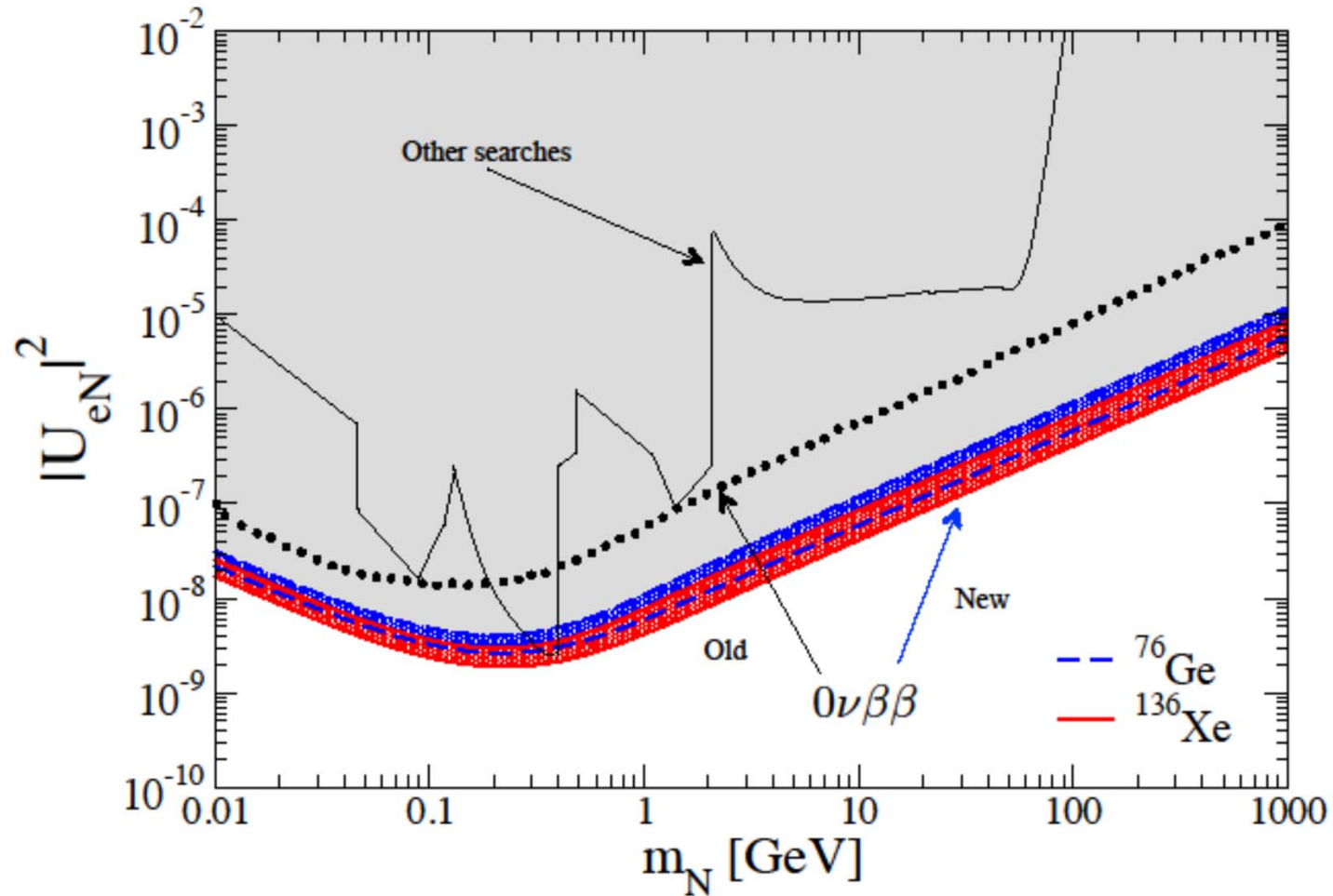
$$\langle p^2 \rangle = m_p m_e \left| \frac{M_N^{0\nu}(g_A^{\text{eff}})}{M_\nu^{0\nu}(g_A^{\text{eff}})} \right|^2 \approx 200 \text{ MeV}$$



## Averaged neutrino momentum calculated from NMEs

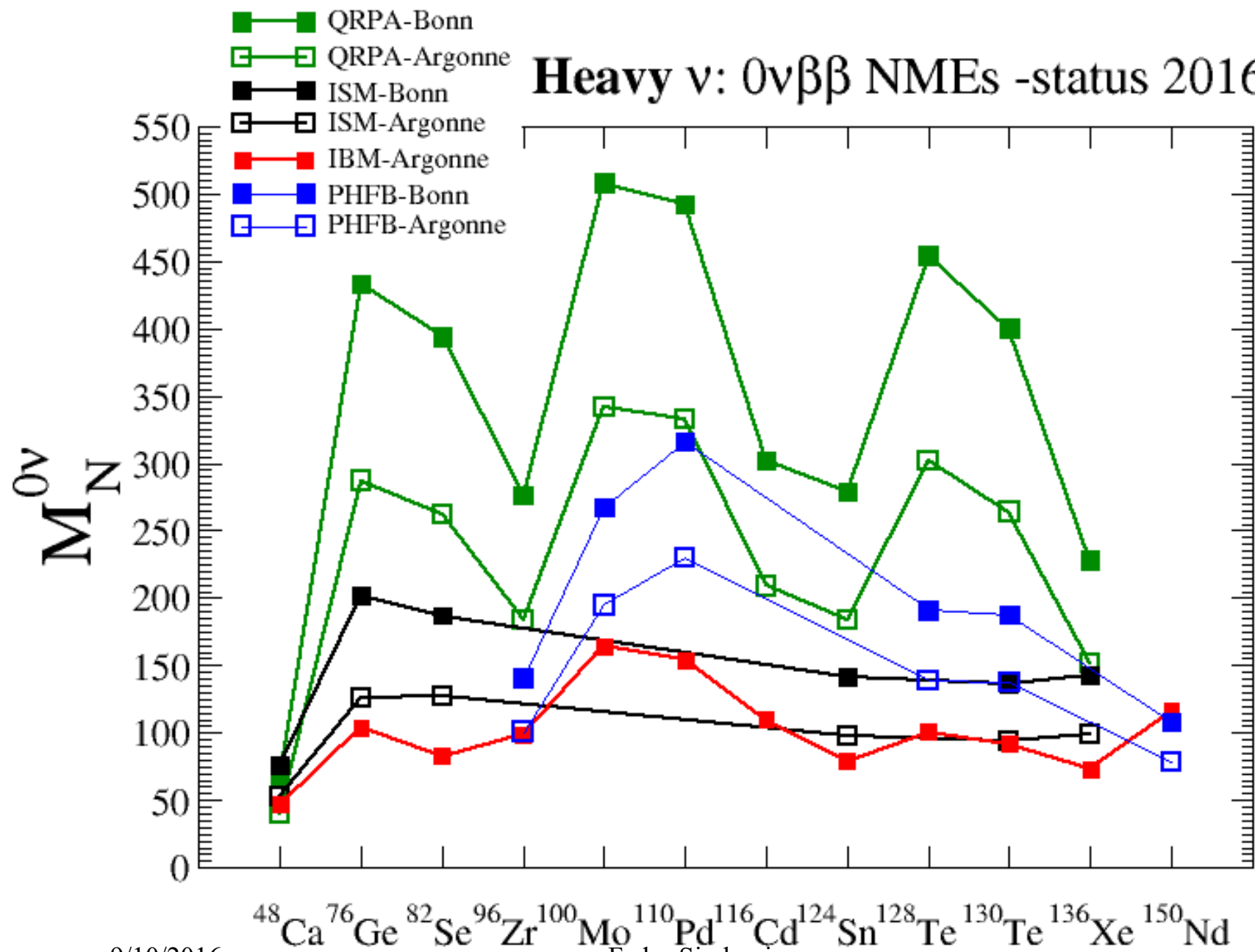


**Exclusion plot  
in  $|U_{eN}|^2 - m_N$  plane**



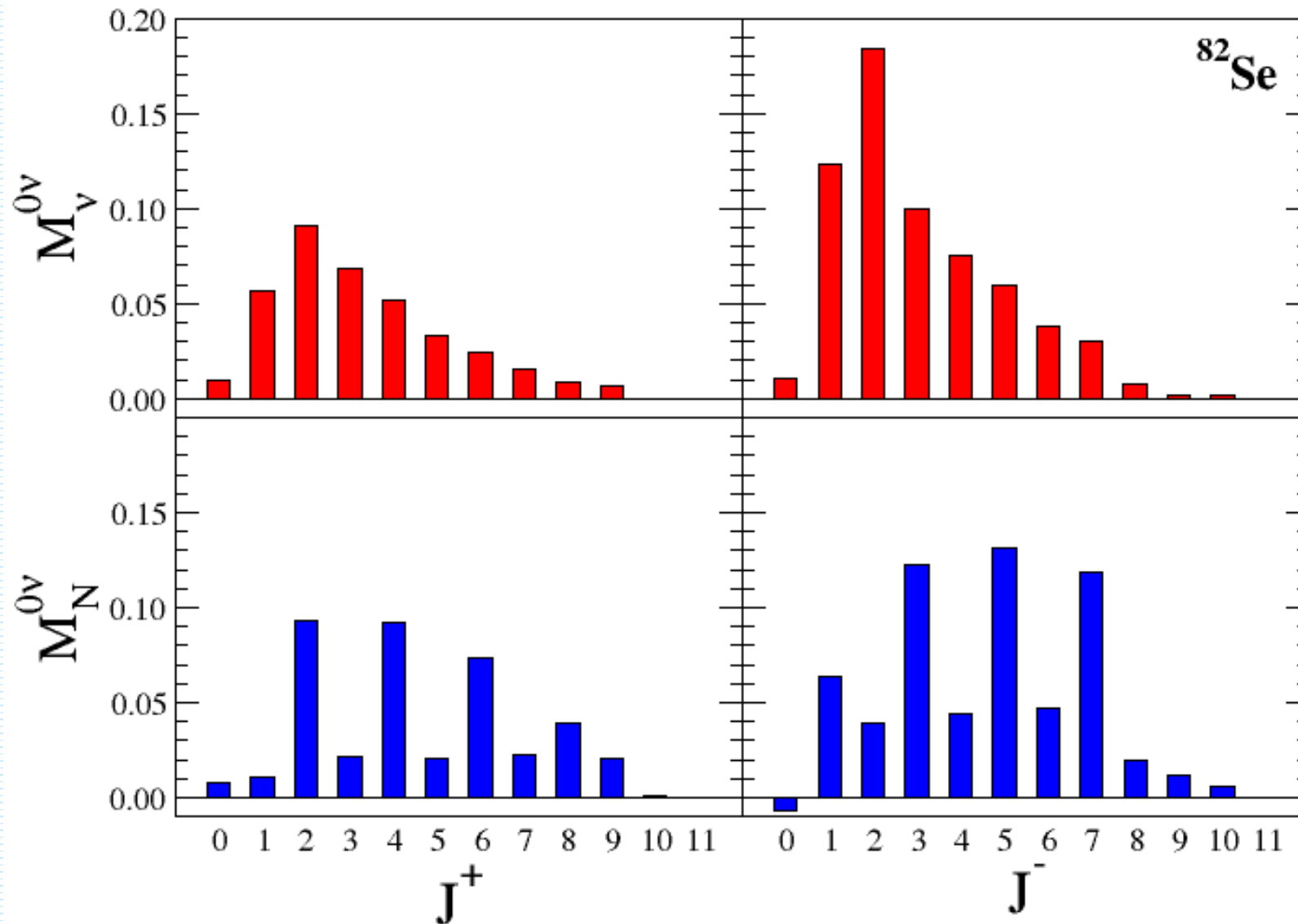
**Improvements:** i) QRPA (constrained Hamiltonian by  $2\nu\beta\beta$  half-life, self-consistent treatment of src, restoration of isospin symmetry ...),  
ii) More stringent limits on the  $0\nu\beta\beta$  half-life

# Heavy $\nu$ : $0\nu\beta\beta$ NMEs -status 2016

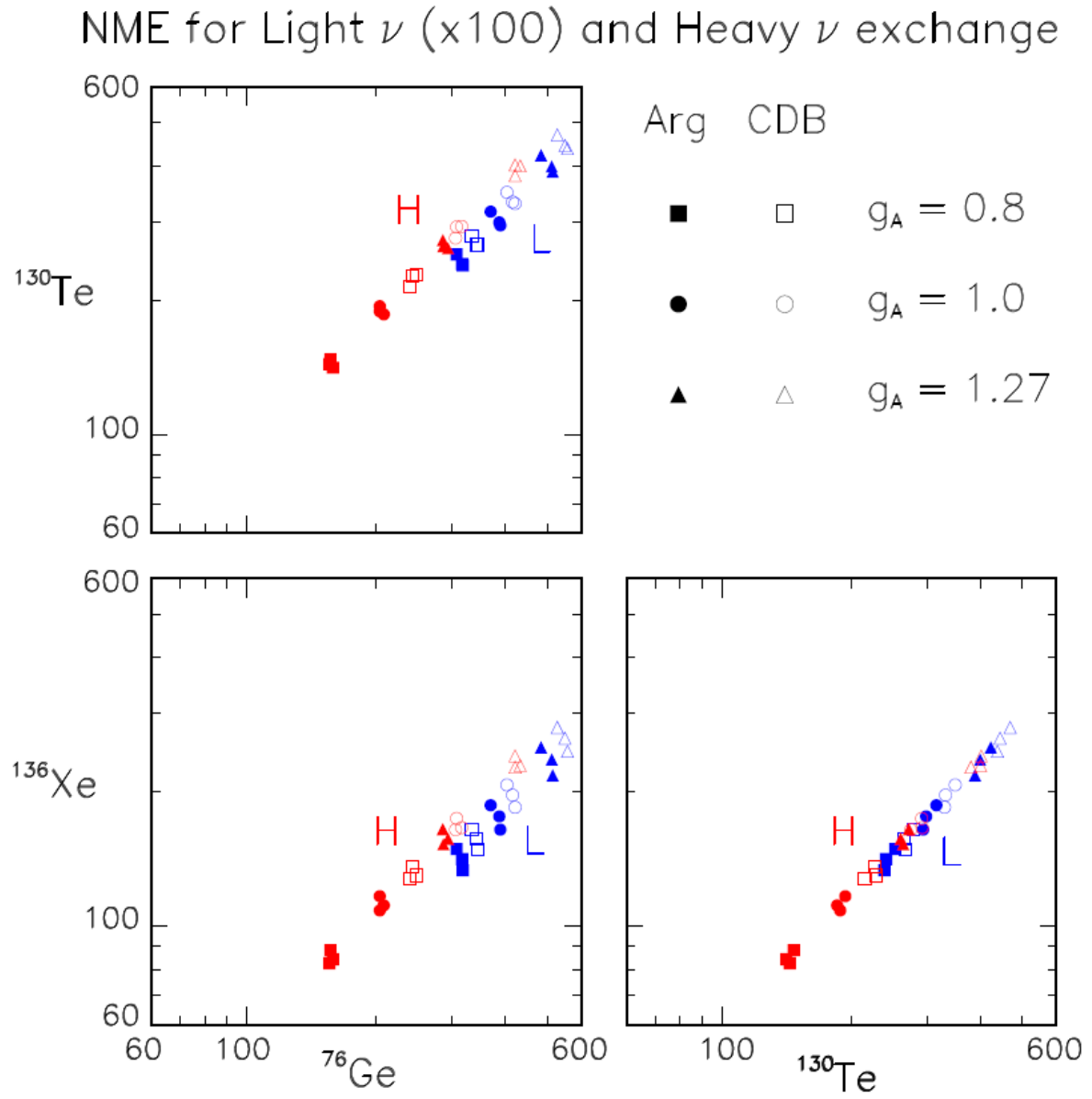




# *Multipole decomposition of NMEs normalized to unity*

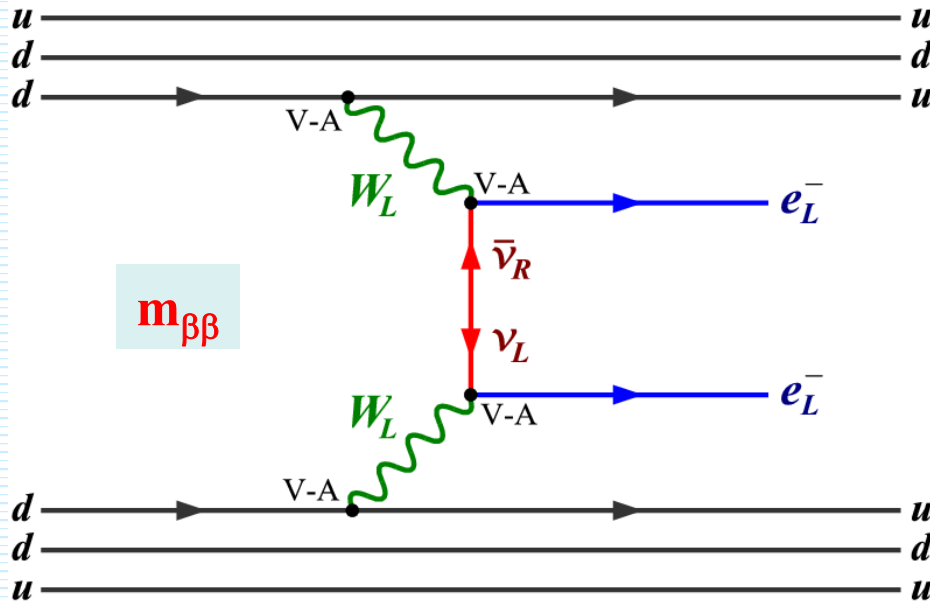


**Only positive signs:  
There is a correlation  
of errors;  
It is practically not  
possible to distinguish  
both mechanisms  
even observing  
the  $0\nu\beta\beta$ -decay for  
3 nuclei**



*The  $0\nu\beta\beta$ -decay with right-handed currents  
revisited (exchange of light neutrinos)*

**D. Štefánik, R. Dvornický, F.Š., P. Vogel, PRC 92, 055502 (2015)**



$m_{\beta\beta}$

*Left-right symmetric models SO(10)*

$$\begin{pmatrix} W_L^- \\ W_R^- \end{pmatrix} = \begin{pmatrix} \cos \zeta & \sin \zeta \\ -\sin \zeta & \cos \zeta \end{pmatrix} \begin{pmatrix} W_1^- \\ W_2^- \end{pmatrix}$$

$$\nu_{eL} = \sum_{j=1}^3 (U_{ej} \nu_{jL} + S_{ej} (N_{jR})^C)$$

$$\nu_{eR} = \sum_{j=1}^3 (T_{ej}^* (\nu_{jL})^C + V_{ej}^* N_{jR})$$

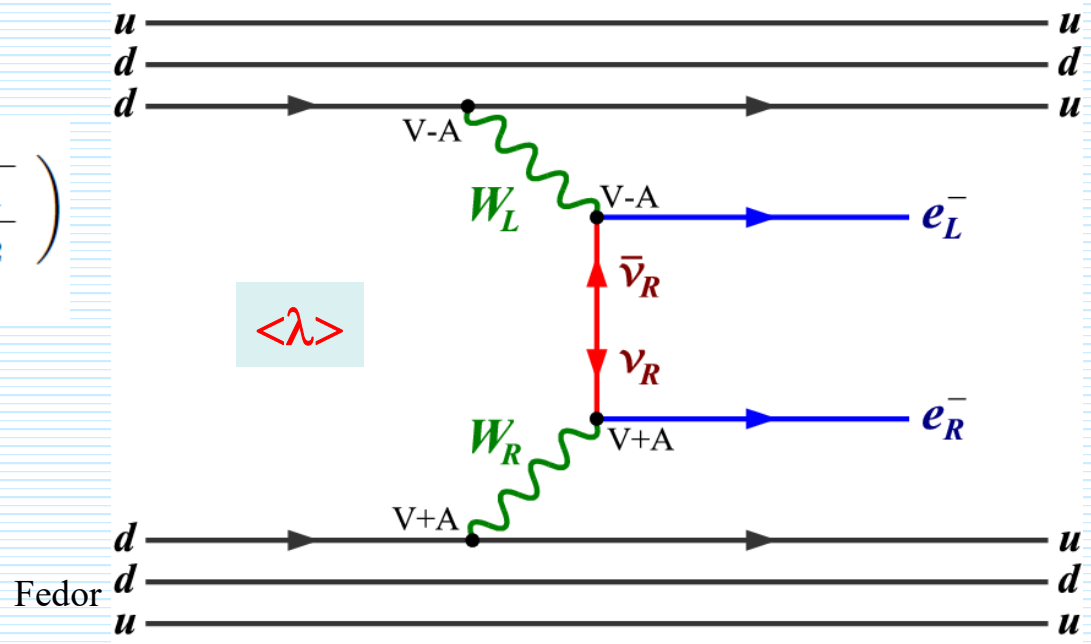
$$H^\beta = \frac{G_\beta}{\sqrt{2}} \left[ j_L^\rho J_{L\rho}^\dagger + \chi j_L^\rho J_{R\rho}^\dagger + \eta j_R^\rho J_{L\rho}^\dagger + \lambda j_R^\rho J_{R\rho}^\dagger + h.c. \right]$$

$$\eta \simeq -\tan \zeta, \quad \chi = \eta$$

$$\lambda \simeq (M_{W_1}/M_{W_2})^2.$$

$$j_L^\rho = \bar{e} \gamma_\rho (1 - \gamma_5) \nu_{eL}$$

$$j_R^\rho = \bar{e} \gamma_\rho (1 + \gamma_5) \nu_{eR}$$



$\langle \lambda \rangle$

Fedor

### 3x3 block matrices

**U, S, T, V are generalization of PMNS matrix**

Zhi-zhong Xing, Phys. Rev. D 85, 013008 (2012)

### 6x6 neutrino mass matrix

$$U = \begin{pmatrix} U & S \\ T & V \end{pmatrix}$$

### Basis

$$(\nu_L, (N_R)^C)^T$$

$$\mathcal{M} = \begin{pmatrix} M_L & M_D \\ M_D^T & M_R \end{pmatrix}$$

**15 angles, 10+5 phases**

### Decomposition

$$U = \begin{pmatrix} 1 & 0 \\ 0 & U_0 \end{pmatrix} \begin{pmatrix} A & R \\ S & B \end{pmatrix} \begin{pmatrix} V_0 & 0 \\ 0 & 1 \end{pmatrix}$$

### Type seesaw I

$$A \approx 1, B \approx 1, R \approx \frac{m_D}{m_{LNV}} \mathbf{1}, S \approx -\frac{m_D}{m_{LNV}} \mathbf{1}$$

### Approximation

$$U_0 \simeq V_0$$

### LNV parameters

$$\langle \lambda \rangle \approx (M_{W_1}/M_{W_2})^2 \frac{m_D}{m_{LNV}} |\xi|$$

$$\langle \eta \rangle \approx -\tan \zeta \frac{m_D}{m_{LNV}} |\xi|,$$

$$|\xi| = |c_{23}c_{12}^2c_{13}s_{13}^2 - c_{12}^3c_{13}^3 - c_{13}c_{23}c_{12}^2s_{13}^2 - c_{12}c_{13}(c_{13}^2s_{12}^2 + s_{13}^2)| \simeq 0.82$$

# The $0\nu\beta\beta$ -decay rate with right-handed currents

$$\begin{aligned} [T_{1/2}^{0\nu}]^{-1} &= \frac{\Gamma^{0\nu}}{\ln 2} = g_A^4 |M_{GT}|^2 \left\{ C_{mm} \left( \frac{|m_{\beta\beta}|}{m_e} \right)^2 \right. \\ &+ C_{m\lambda} \frac{|m_{\beta\beta}|}{m_e} \langle \lambda \rangle \cos \psi_1 + C_{m\eta} \frac{|m_{\beta\beta}|}{m_e} \langle \eta \rangle \cos \psi_2 \\ &\left. + C_{\lambda\lambda} \langle \lambda \rangle^2 + C_{\eta\eta} \langle \eta \rangle^2 + C_{\lambda\eta} \langle \lambda \rangle \langle \eta \rangle \cos(\psi_1 - \psi_2) \right\} \end{aligned}$$

**Two additional  
phase-space factor  $G_{010}$  and  $G_{011}$   
(For w.f. A  $G_{010}=G_{03}$ ,  $G_{011}=G_{04}$ )**

**The induced pseudoscalar term  
included**

$$\langle \lambda \rangle = \lambda \left| \sum_j U_{ej} V_{ej} (g'_V / g_V) \right|,$$

$$\langle \eta \rangle = \eta \left| \sum_j U_{ej} V'_{ej} \right|,$$

$$\psi_1 = \arg \left[ \left\{ \sum_j m_j U_{ej}^2 \right\} \left\{ \sum_j U_{ej} V_{ej} (g'_V / g_V) \right\} \right],$$

$$\psi_2 = \arg \left[ \left\{ \sum_j m_j U_{ej}^2 \right\} \left\{ \sum_j U_{ej} V'_{ej} \right\}^* \right].$$

$$C_{mm} = (1 - \chi_F + \chi_T)^2 G_{01},$$

$$C_{m\lambda} = -(1 - \chi_F + \chi_T) [\chi_{2-} G_{03} - \chi_{1+} G_{04}],$$

$$C_{m\eta} = (1 - \chi_F + \chi_T)$$

$$\times [\chi_{2+} G_{03} - \chi_{1-} G_{04} - \chi_P G_{05} + \chi_R G_{06}],$$

$$C_{\lambda\lambda} = \chi_{2-}^2 G_{02} + \frac{1}{9} \chi_{1+}^2 G_{011} - \frac{2}{9} \chi_{1+} \chi_{2-} G_{010},$$

$$C_{\eta\eta} = \chi_{2+}^2 G_{02} + \frac{1}{9} \chi_{1-}^2 G_{011} - \frac{2}{9} \chi_{1-} \chi_{2+} G_{010} + \chi_P^2 G_{08} \\ - \chi_P \chi_R G_{07} + \chi_R^2 G_{09},$$

$$C_{\lambda\eta} = -2[\chi_{2-} \chi_{2+} G_{02} - \frac{1}{9} (\chi_{1+} \chi_{2+} + \chi_{2-} \chi_{1-}) G_{010}$$

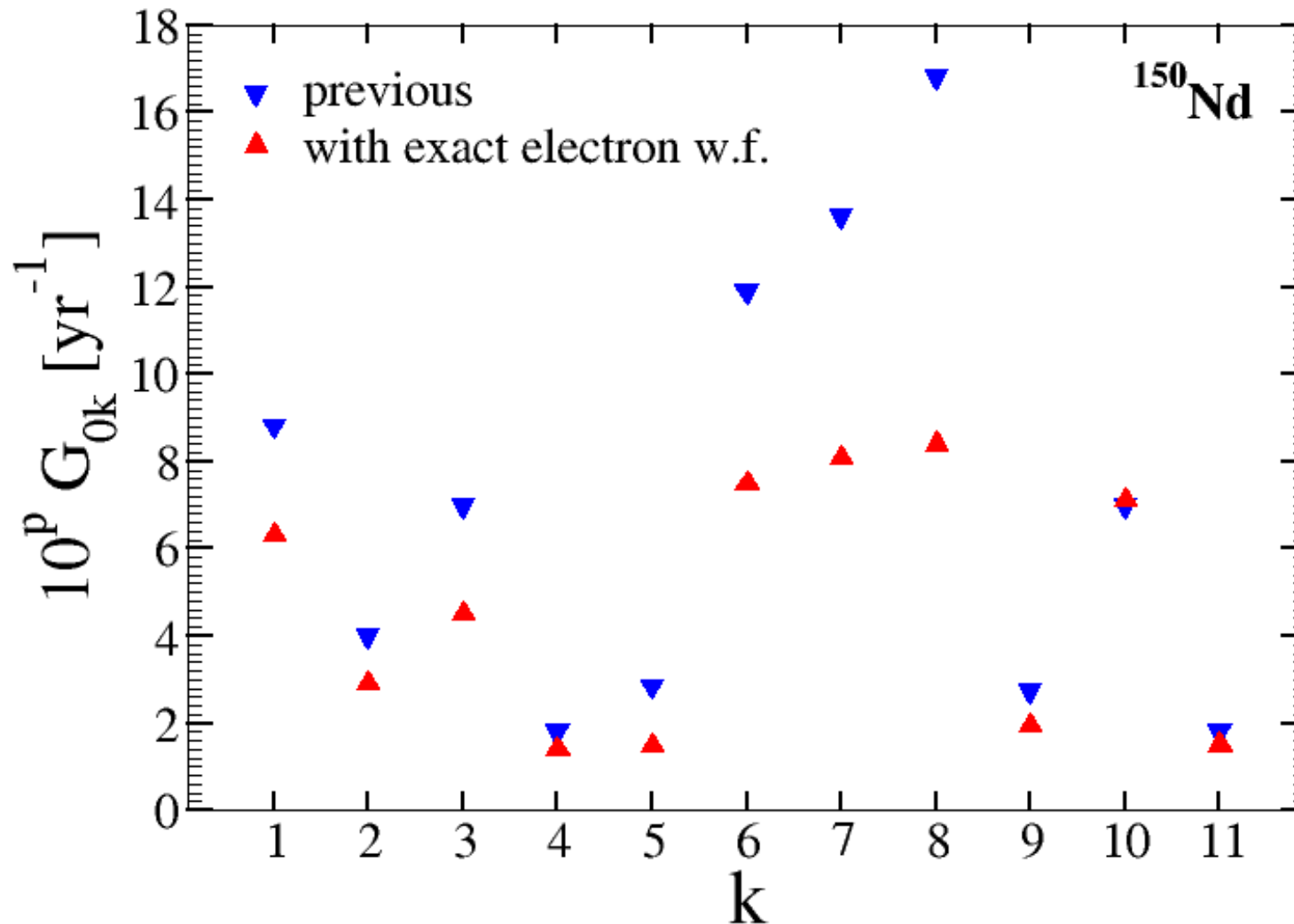
$$+ \frac{1}{9} \chi_{1+} \chi_{1-} G_{011}].$$

(37)

## Phase-space factors for $^{150}\text{Nd}$

$$\Psi(\varepsilon, \mathbf{r}) = \Psi^{(s_{1/2})}(\varepsilon, \mathbf{r}) + \Psi^{(p_{1/2})}(\varepsilon, \mathbf{r})$$

The exact Dirac wave functions with finite nuclear size corrections, which are taken into account in by a uniform charge distribution in a sphere of nucleus, and the screening of atomic electrons

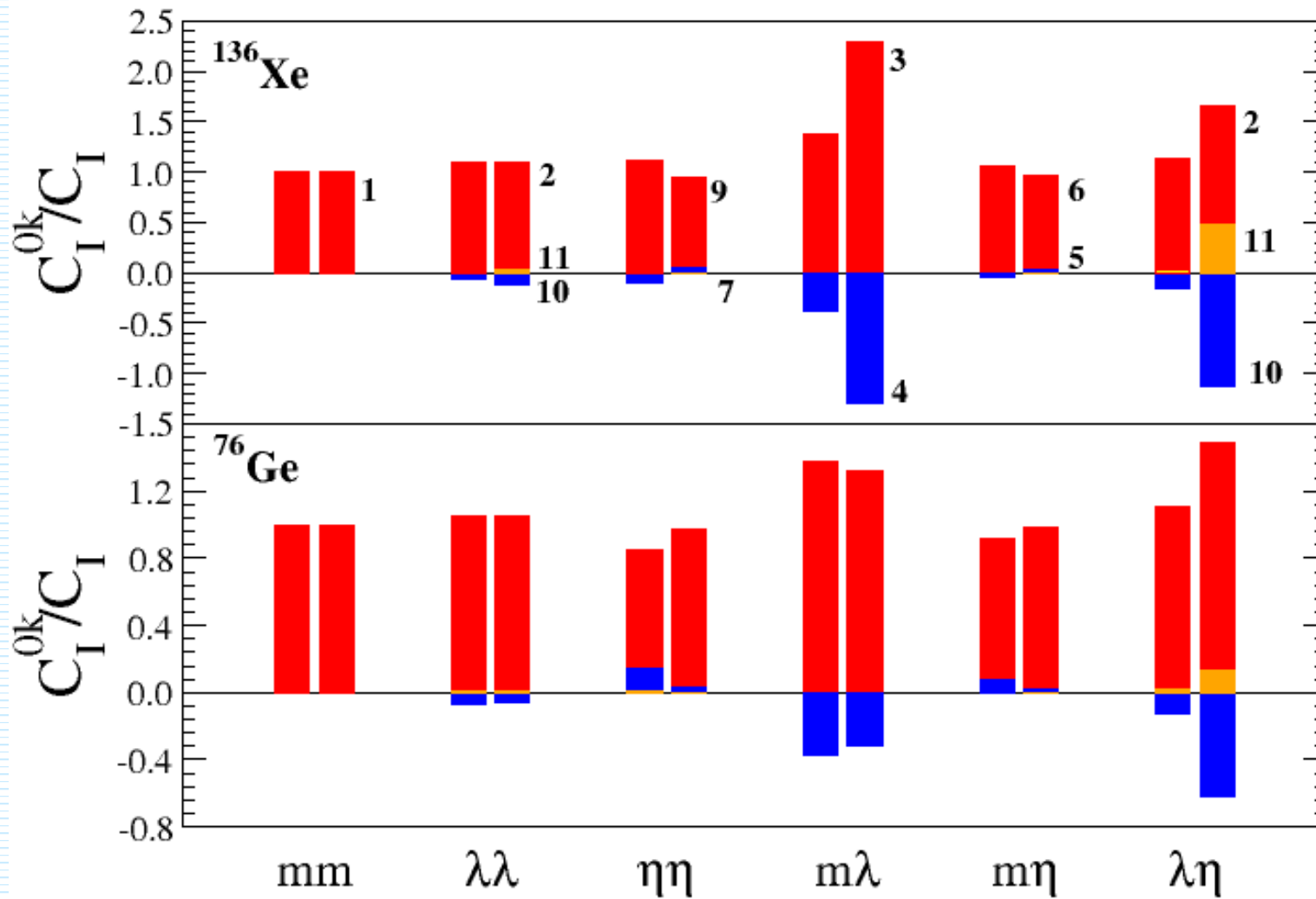




**Simplified expressions for  $T_{1/2}^{0\nu}$  for  $\langle\eta\rangle$  and  $\langle\lambda\rangle$  mech.**

$$\left(T_{1/2}^{0\nu}\right)^{-1} \approx |\langle\eta\rangle|^2 G_{09} |M_{\eta\eta}|^2$$

$$\left(T_{1/2}^{0\nu}\right)^{-1} \approx |\langle\lambda\rangle|^2 G_{02} |M_{\lambda\lambda}|^2$$



## Current constraints on the effective neutrino mass and effective right-handed current parameters

w.f.	$^{76}\text{Ge}$		$^{136}\text{Xe}$	
	A	D	A	D
	QRPA			
$ m_{\beta\beta} $ [eV]	0.321	0.333	0.285	0.315
$ m_{\beta\beta} $ [eV] (for $\langle\eta\rangle = \langle\eta\rangle = 0$ )	0.271	0.284	0.251	0.285
$\langle\eta\rangle \times 10^{-9}$	3.093	3.239	2.077	2.337
$\langle\lambda\rangle \times 10^{-7}$	4.943	5.163	3.822	4.370
	ISM			
$ m_{\beta\beta} $ [eV]	0.515	0.535	0.222	0.245
$ m_{\beta\beta} $ [eV] (for $\langle\eta\rangle = \langle\eta\rangle = 0$ )	0.436	0.458	0.193	0.220
$\langle\eta\rangle \times 10^{-9}$	6.370	6.760	2.975	3.291
$\langle\lambda\rangle \times 10^{-7}$	8.462	8.841	3.000	3.378

$$^{76}\text{Ge} \quad T_{1/2}^{0\nu} \geq 3.0 \times 10^{25}$$

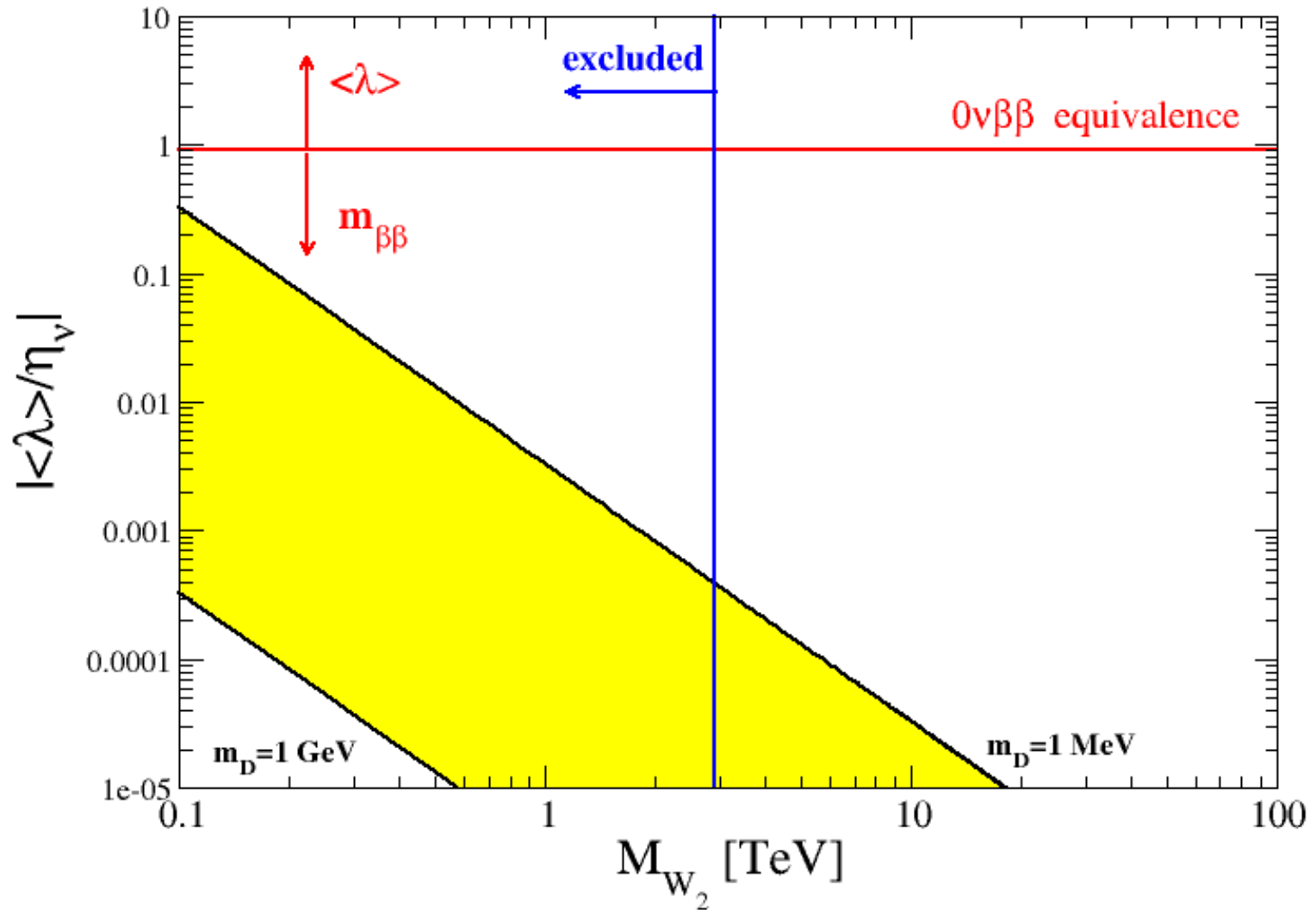
ISM: E. Caurier, F. Nowacki, A. Poves and J. Retamosa, Phys. Rev. Lett. **77**, 1954 (1996)

$$^{136}\text{Xe} \quad T_{1/2}^{0\nu} \geq 3.4 \times 10^{25}$$

QRP: K. Muto, E. Bender and H.V. Klapdor, Z. Phys. A **334**, 187 (1989)

$$\eta_\nu = \frac{m_{\beta\beta}}{m_e} = \sum_i ((U_0)_{ei})^2 \frac{m_i}{m_e} \quad |\langle \lambda \rangle| \approx \frac{m_D}{m_{LNV}} \left( \frac{M_{W_1}}{M_{W_2}} \right)^2 |\xi|$$

$$\approx \frac{m_D}{m_{LNV}} \frac{m_D}{m_e} \sum_i (U_0)_{ei}^2 \frac{m_i m_{LNV}}{m_D^2} \quad \text{if } \approx 1 \quad |\xi| = |c_{23}c_{12}^2c_{13}s_{13}^2 - c_{12}^3c_{13}^3 - c_{13}c_{23}c_{12}^2s_{13}^2 - c_{12}c_{13}c_{13}^2s_{12}^2 + s_{13}^2| \approx 0.82$$



$$\eta_\nu = \frac{m_{\beta\beta}}{m_e} = \sum_i ((U_0)_{ei})^2 \frac{m_i}{m_e}$$

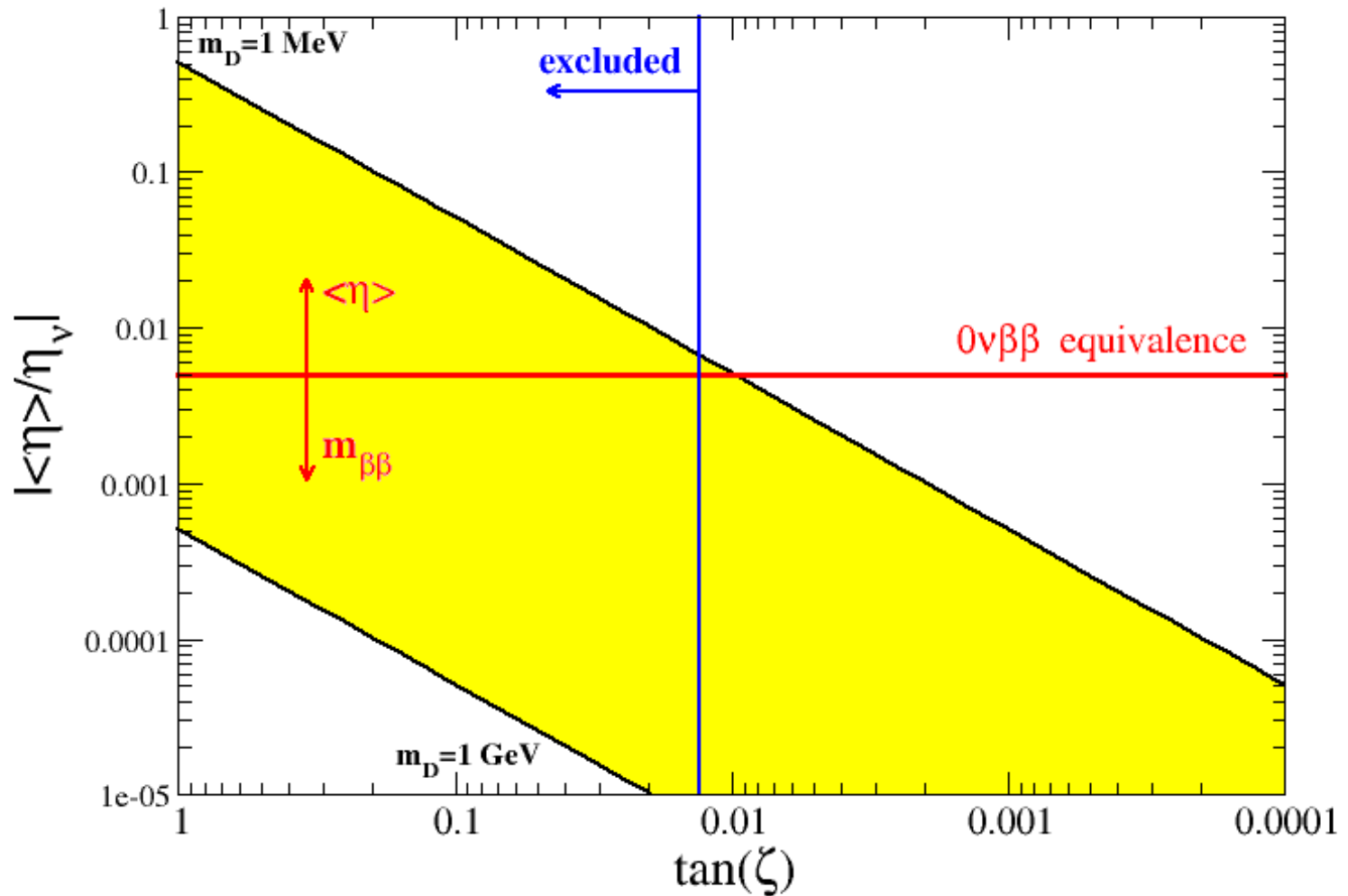
$$\approx \frac{m_D}{m_{LNV}} \frac{m_D}{m_e} \sum_i (U_0)_{ei}^2 \frac{m_i m_{LNV}}{m_D^2}$$

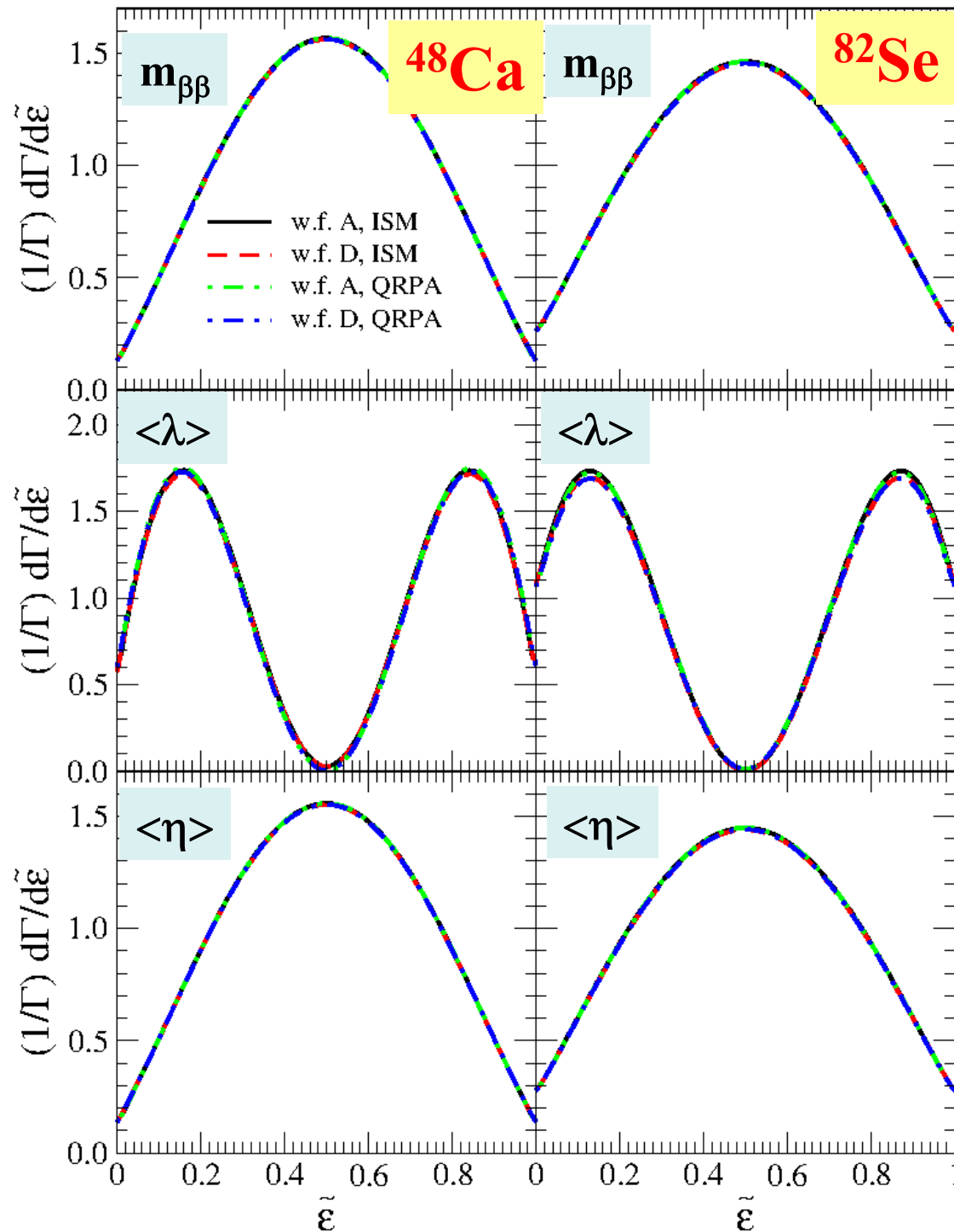
if  $\approx 1$

$$|\xi| = |c_{23}c_{12}^2c_{13}s_{13}^2 - c_{12}^3c_{13}^3 - c_{13}c_{23}c_{12}^2s_{13}^2 - c_{12}c_{13}c_{13}^2s_{12}^2 + s_{13}^2|$$

$$\approx 0.82$$

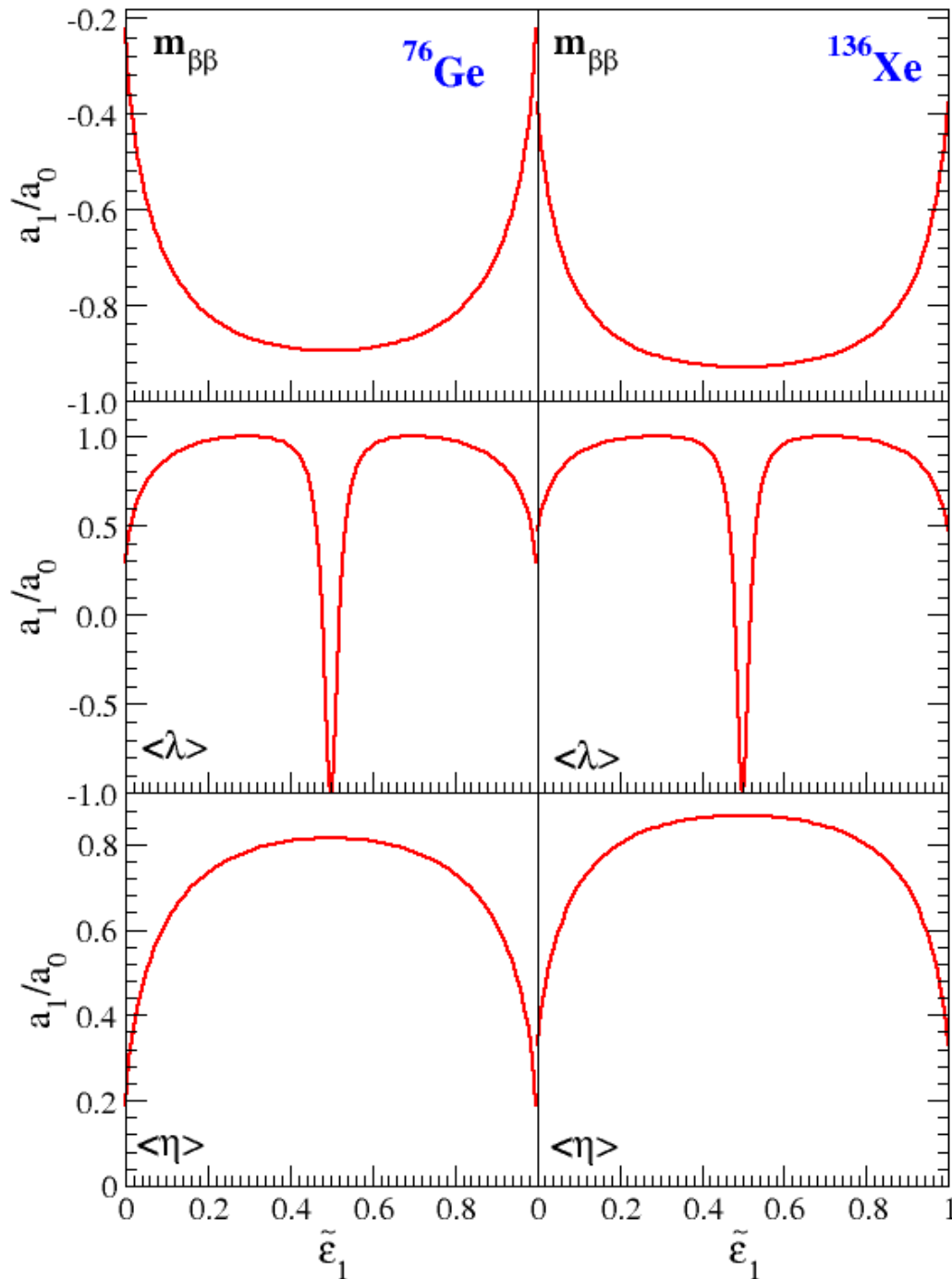
$$|\langle \eta \rangle| \approx \frac{m_D}{m_{LNV}} \tan(\zeta) |\xi|$$





The single differential  
 decay rate normalized  
 to the total decay rate  
 as function of electron energy  
 for 3 limiting cases:

**SuperNEMO experiment  
 can measure it**



Angular correlation factor  
as function of electron energy

$$\frac{d\Gamma}{d \cos \theta d\tilde{\epsilon}_1} = a_0 (1 + a_1/a_0 \cos \theta)$$

SuperNEMO experiment  
can measure it

# The $0\nu\beta\beta$ -decay with right-handed currents revisited (exchange of heavy neutrinos)

J.D.Vergados, H. Ejiri, , F.Š., submitted

$$\left(T_{1/2}^{0\nu} G^{0\nu} g_A^4\right)^{-1} = \left|\eta_\nu M_\nu^{0\nu} + \eta_N^L M_N^{0\nu}\right|^2 + \left|\eta_N^R M_N^{0\nu}\right|^2$$

$$\begin{aligned}\eta_\nu &= \frac{m_{\beta\beta}}{m_e} = \sum_i ((U_0)_{ei})^2 \frac{m_i}{m_e} \\ &\approx \frac{m_p}{m_{LNV}} \frac{m_D^2}{m_e m_p} \sum_i (U_0)_{ei}^2 \frac{m_i m_{LNV}}{m_D^2}\end{aligned}$$

$$\begin{aligned}\eta_N^R &= \frac{m_p}{m_{LNV}} \left(\frac{M_{W_1}}{M_{W_2}}\right)^2 \sum_i (U_{ei}^{22})^2 \frac{m_{LNV}}{M_i} \\ &\approx \frac{m_p}{m_{LNV}} \left(\frac{M_{W_1}}{M_{W_2}}\right)^2 \sum_i (V_0)_{ei}^2 \frac{m_{LNV}}{M_i}\end{aligned}$$

Suppressed mechanism:

$$\begin{aligned}\eta_N^L &= \frac{m_p}{m_{LNV}} \sum_i (U_{ei}^{(12)})^2 \frac{m_{LNV}}{M_i} \\ &\approx \frac{m_p}{m_{LNV}} \left(\frac{m_D}{m_{LNV}}\right)^2 \sum_i \frac{m_{LNV}}{M_i}\end{aligned}$$

Could be of comparable Importance, if e.g.

$$\begin{aligned}\sum_i (U_0)_{ei}^2 \frac{m_i m_{LNV}}{m_D^2} &\simeq \sum_i (V_0)_{ei}^2 \frac{m_{LNV}}{M_i} \\ \frac{m_D^2}{m_e m_p} M_\nu^{0\nu} &\simeq \left(\frac{M_{W_1}}{M_{W_2}}\right)^2 M_N^{0\nu}\end{aligned}$$



# Two non-interfering mechanisms of the $0\nu\beta\beta$ -decay (light LH and heavy RH neutrino exchange)

**Half-life:**

$$\frac{1}{T_{1/2,i}^{0\nu} G_i^{0\nu}(E, Z)} \cong |\eta_\nu|^2 |M'_{i,\nu}{}^{0\nu}|^2 + |\eta_R|^2 |M'_{i,N}{}^{0\nu}|^2$$

**Set of equations:**

$$\frac{1}{T_1 G_1} = |\eta_\nu|^2 |M'_{1,\nu}{}^{0\nu}|^2 + |\eta_R|^2 |M'_{1,N}{}^{0\nu}|^2$$

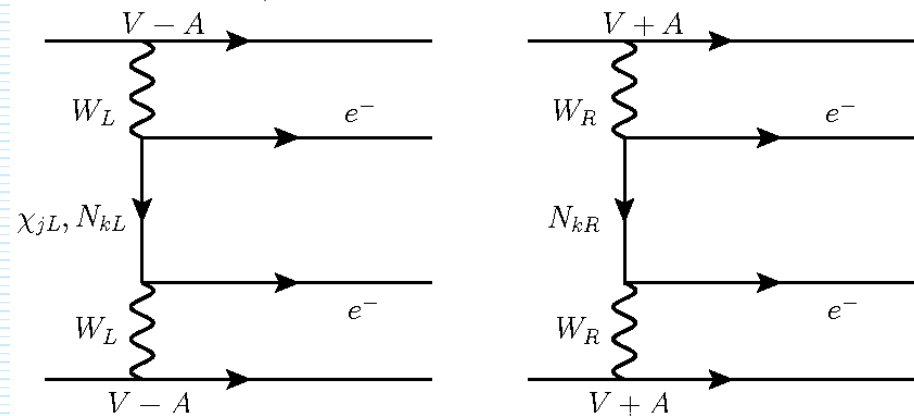
$$\frac{1}{T_2 G_2} = |\eta_\nu|^2 |M'_{2,\nu}{}^{0\nu}|^2 + |\eta_R|^2 |M'_{2,N}{}^{0\nu}|^2$$

**Solutions:**

$$|\eta_\nu|^2 = \frac{|M'_{2,N}{}^{0\nu}|^2 / T_1 G_1 - |M'_{1,N}{}^{0\nu}|^2 / T_2 G_2}{|M'_{1,\nu}{}^{0\nu}|^2 |M'_{2,N}{}^{0\nu}|^2 - |M'_{1,N}{}^{0\nu}|^2 |M'_{2,\nu}{}^{0\nu}|^2}$$

$$|\eta_R|^2 = \frac{|M'_{1,\nu}{}^{0\nu}|^2 / T_2 G_2 - |M'_{2,\nu}{}^{0\nu}|^2 / T_1 G_1}{|M'_{1,\nu}{}^{0\nu}|^2 |M'_{2,N}{}^{0\nu}|^2 - |M'_{1,N}{}^{0\nu}|^2 |M'_{2,\nu}{}^{0\nu}|^2}$$

$$\eta_\nu = \frac{m_{\beta\beta}}{m_e}$$



$$\eta_N^R = \left( \frac{M_W}{M_{WR}} \right)^4 \sum_k^{\text{heavy}} V_{ek}^2 \frac{m_p}{M_k}$$

**Two non-interfering mechanisms of the  $0\nu\beta\beta$ -decay**  
(light LH and heavy RH neutrino exchange)

Pure  $m_{\beta\beta}$  mech.

The positivity condition:

$$\frac{T_1 G_1 |M'_{1,N}|^2}{G_2 |M'_{2,N}|^2} \leq T_2 \leq \frac{T_1 G_1 |M'_{1,\nu}|^2}{G_2 |M'_{2,\nu}|^2}$$

Very narrow ranges!

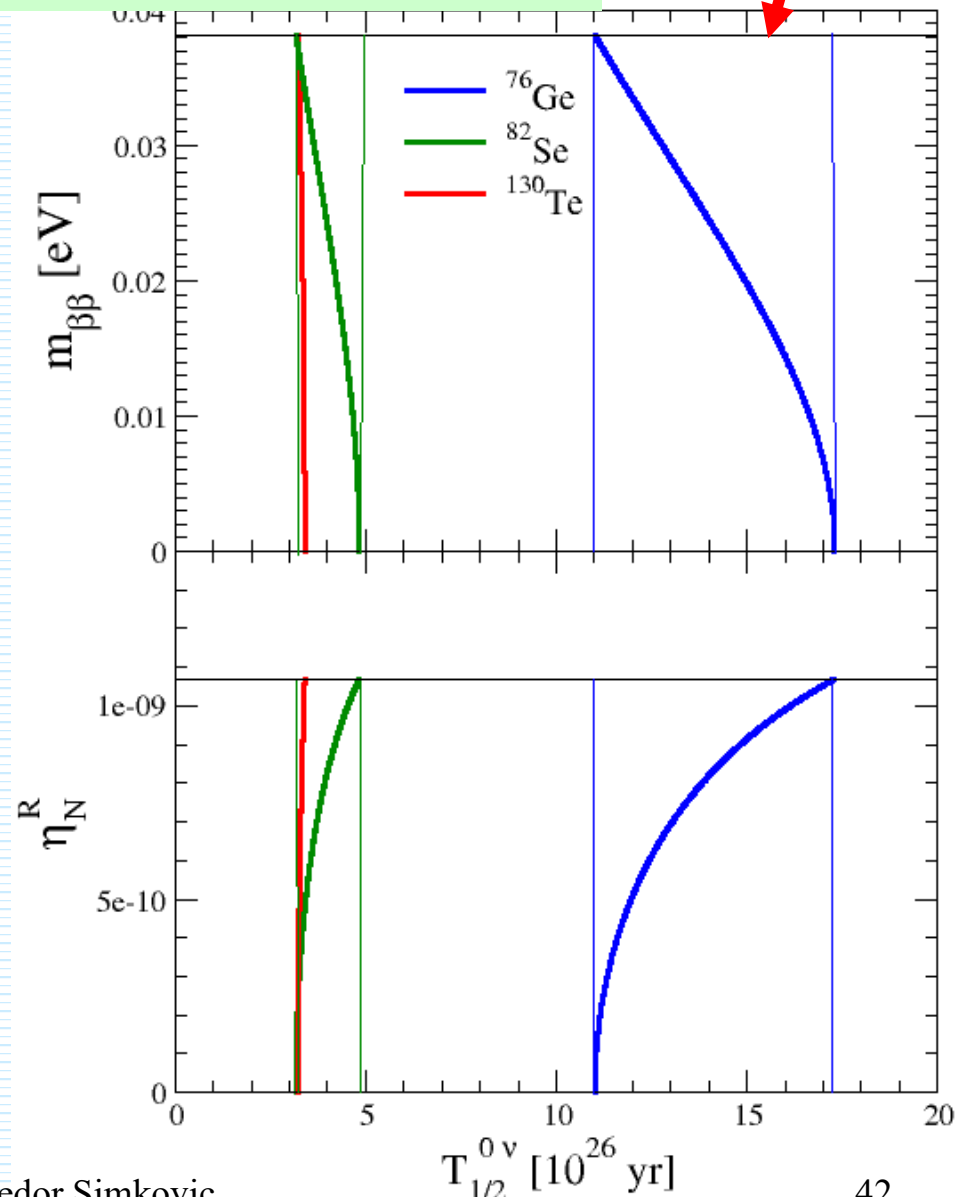
$$1.10 \leq \frac{T_{1/2}^{0\nu}(^{76}\text{Ge})}{T_{1/2}^{0\nu}(^{136}\text{Xe})} \leq 1.73$$

$$3.17 \leq \frac{T_{1/2}^{0\nu}(^{82}\text{Se})}{T_{1/2}^{0\nu}(^{136}\text{Xe})} \leq 4.83$$

$$3.22 \leq \frac{T_{1/2}^{0\nu}(^{130}\text{Te})}{T_{1/2}^{0\nu}(^{136}\text{Xe})} \leq 3.40$$

Assumption:

$$T_{1/2}^{0\nu}(^{136}\text{Xe}) = 1.0 \cdot 10^{27} \text{ yr}$$

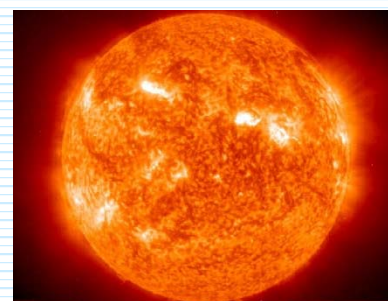
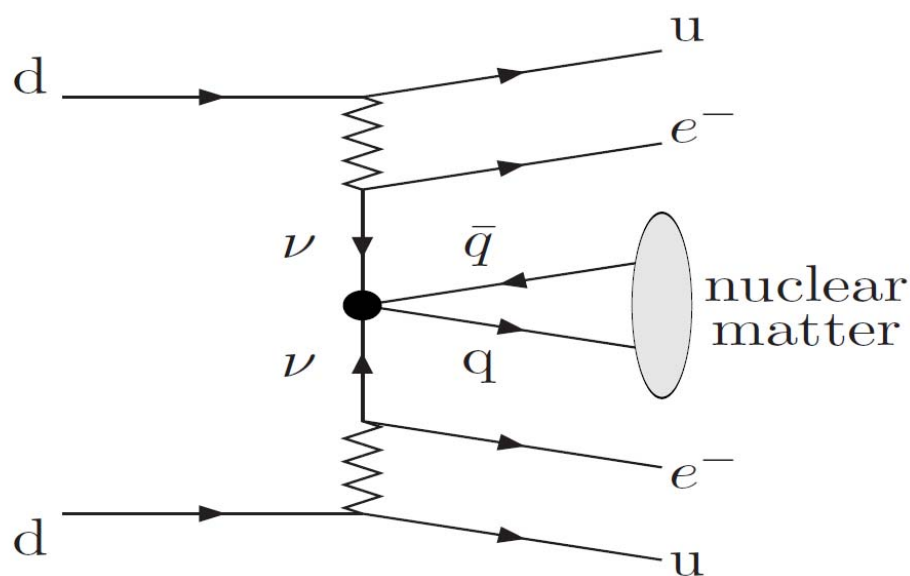


# Nuclear medium effect on the light neutrino mass exchange mechanism of the $0\nu\beta\beta$ decay

S.G. Kovalenko, M.I. Krivoruchenko, F. Š., Phys. Rev. Lett. 112 (2014) 142503

A novel effect in  $0\nu\beta\beta$  decay related with the fact, that its underlying mechanisms take place in the nuclear matter environment:

- + Low energy 4-fermion  $\Delta L \neq 0$  Lagrangian
- + In-medium Majorana mass of neutrino
- +  $0\nu\beta\beta$  constraints on the universal scalar couplings

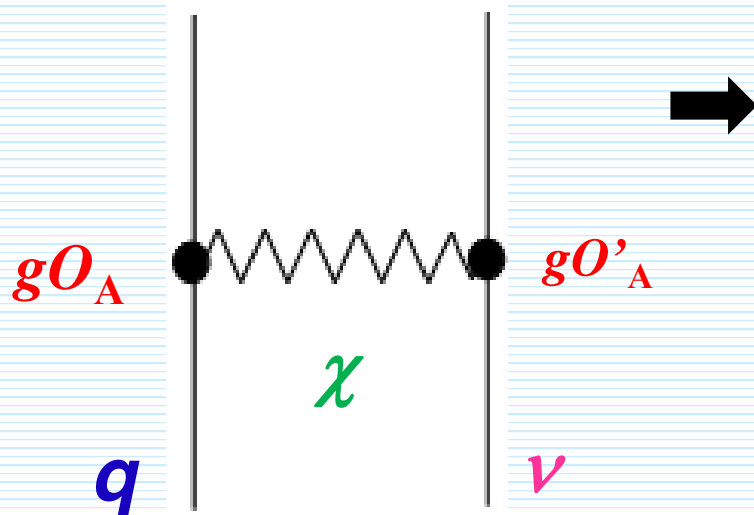


Non-standard  $\nu$ -int. discussed e.g., in the context of  $\nu$ -osc. at Sun

$$\begin{aligned}\rho_{\text{Sun}} &= 1.4 \text{ g/cm}^3 \\ \rho_{\text{Earth}} &= 5.5 \text{ g/cm}^3 \\ \rho_{\text{nucleus}} &= 2.3 \cdot 10^{14} \text{ g/cm}^3\end{aligned}$$

imkovic

**Non-standard interactions might be easily detected in nucleus rather than in vacuum**



**Low energy 4-fermion**  
 $\Delta L \neq 0$  **Lagrangian**

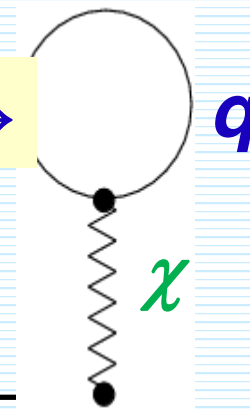
$$L_{\text{eff}} = \frac{g^2}{m_\chi^2} \sum_A (\bar{q} O_A q) (\bar{\nu} O'_A \nu),$$

$$m_\chi \gtrsim M_W.$$

oscillation experiments  
 tritium  $\beta$ -decay, cosmology

**$0\nu\beta\beta$ -decay**

**density**  $\rightarrow$



$$\sum_\nu^{\text{vac}} = -\times-$$

$$\sum_\nu^{\text{medium}} = -\times- +$$

## Classification of the vertices $gO_A$ and $gO'_A$

$$\mathcal{L}_{\text{free},\nu} = \frac{1}{4} \sum_i \bar{\nu}_i i \gamma^\mu \overleftrightarrow{\partial}_\mu \nu_i - \frac{1}{2} \sum_i m_i \bar{\nu}_i \nu_i.$$

$$\mathcal{L}_{\text{eff}} = \frac{g_\chi}{m_\chi^2} \bar{q} q \sum_{a=1}^6 \sum_{ij} g_{ij}^a J_{ij}^a$$

**In nuclei, mean fields are created by scalar and vector currents ( $\sigma, \omega$ ).  
Vector currents do not flip the spin of neutrinos  
and do not contribute to the  $0\nu\beta\beta$  decay.**

### Symmetric and antisymmetric scalar neutrino currents $J_{ij}^a$

$a$	S	$a$	S	$a$	A
1	$\bar{\nu}_i^c \nu_j$	3	$\partial_\mu (\bar{\nu}_i^c \gamma_5 \gamma^\mu \nu_j)$	5	$\partial_\mu (\bar{\nu}_i^c \gamma^\mu \nu_j)$
2	$\bar{\nu}_i^c i \gamma_5 \nu_j$	4	$\bar{\nu}_i^c \gamma^\mu i \overleftrightarrow{\partial}_\mu \nu_j$	6	$\bar{\nu}_i^c \gamma_5 \gamma^\mu i \overleftrightarrow{\partial}_\mu \nu_j$

**$g_{ij}^a$  are real symmetric for  $a = 1, 2, 3, 4$  and imaginary antisymmetric for  $a = 5, 6$ . In the limit of  $R = \infty$ , the currents  $a = 3, 5$  vanish.**

Mean field:

$$\bar{q}q \rightarrow \langle \bar{q}q \rangle$$

and

$$\langle \bar{q}q \rangle \approx 0.5 \langle q^\dagger q \rangle \approx 0.25 \text{ fm}^{-3}$$

The effect depends on

$$\langle \chi \rangle = -\frac{g_\chi}{m_\chi^2} \langle \bar{q}q \rangle$$

A comparison with  $G_F$ :

$$\frac{g_\chi g_{ij}^a}{m_\chi^2} = \frac{G_F}{\sqrt{2}} \varepsilon_{ij}^a$$

Typical scale:

$$\langle \chi \rangle g_{ij}^a = -\frac{G_F}{\sqrt{2}} \langle \bar{q}q \rangle \varepsilon_{ij}^a \approx -25 \varepsilon_{ij}^a \text{ eV}$$

We expect:

$$25 \varepsilon_{ij}^a < 1 \rightarrow m_\chi^2 > 25 \frac{g_\chi g_{ij}^a \sqrt{2}}{G_F} \sim 1 \text{ TeV}^2$$

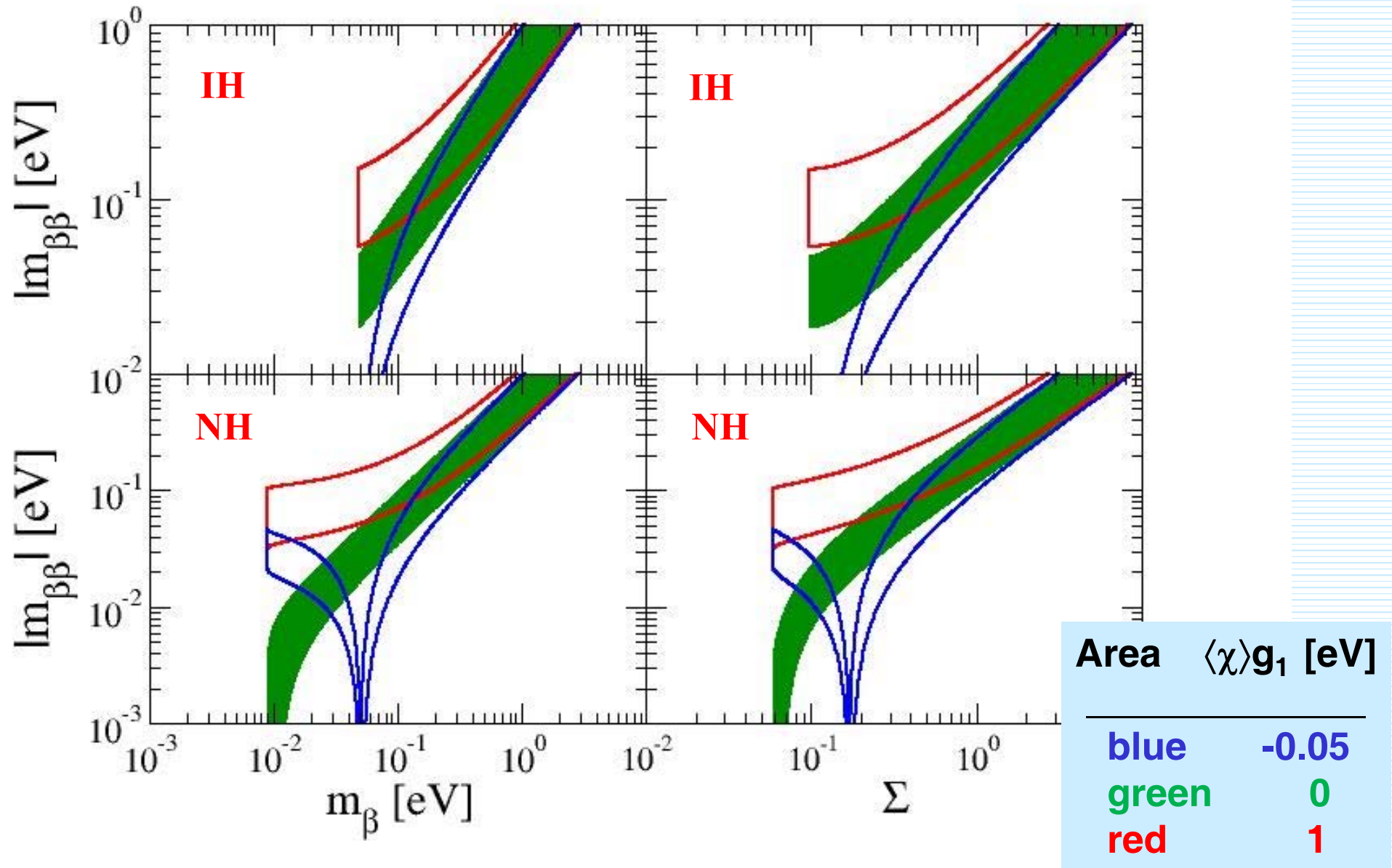
Universal scalar interaction

$$g_{ij}^a = \delta_{ij} g_a \quad \varepsilon_{ij}^a = \delta_{ij} \varepsilon_a$$

In medium  
effective  
Majorana  $\nu$  mass

$$m_{\beta\beta} = \sum_{i=1}^n U_{ei}^2 \xi_i \frac{\sqrt{(m_i + \langle \chi \rangle g_1)^2 + (\langle \chi \rangle g_2)^2}}{(1 - \langle \chi \rangle g_4)^2}$$

**Complementarity between  $\beta$ -decay,  $0\nu\beta\beta$  -decay and cosmological measurements might be spoiled**





## Instead of Conclusions



**We are at the beginning of the Road...**

**The observation will prove Majorana nature of neutrinos.  
The spectrum of neutrino masses might remain undetermined.**